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Optimization of Cooled Shields in Insulations

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ABSTRACT

A relatively simple method has been developed to optimize the location, temperature, and heat dissipation rate of each cooled shield inside an insulation layer. The method is based on the minimization of the entropy production rate which is proportional to the heat leak across the insulation. The results show that the maximum number of shields to be used in most practical applications is three. However, cooled shields are useful only at low values of the overall, cold wall to hot wall absolute temperature ratio. The performance of the insulation system is relatively insensitive to deviations from the optimum values of temperature and location of the cooling shields.

Design curves are presented for rapid estimates of the locations and temperatures of cooling shields in various types of insulations, and an equation is given for calculating the cooling loads for the shields.

NOMENCLATURE

A	Area of heat flow, m^2
C_p	Specific heat of the boiloff vapor, $kJ/kg \cdot K$
D	Functional defined by Eq. (14)
F	Functional defined by Eq. (13)
h_{fg}	Latent heat of vaporization of the boiloff liquid, kJ/kg
k	Thermal conductivity, $W/m \cdot K$; with subscripts, coefficients in Eq. (1)
L	Overall thickness of insulation, m^*
m,n	Exponents in conductivity function, Eq. (1)
P	T_S/T_C , temperature ratio
q	Heat flow rate, W
R	T_C/T_H , overall temperature ratio
s	Dimensionless entropy production rate defined by Eq. (5)
\dot{S}	Entropy production rate, W/K
t	Thickness between walls with single shield between, m^*
T	Absolute temperature, K
x	Distance from cold wall, m^*
x'	Distance from cold wall in a multi-shield configuration, m^*
X	x/t , dimensionless distance*
X'	x'/L , dimensionless distance*
γ	Defined by Eq. (8)

Subscripts

C	Cold wall
H	Hot wall
i	i-th shield
min	Minimum
opt	Optimum
S	Shield

*For systems with single shield $L = t$, $x = x'$, $X = X'$.

INTRODUCTION

The search for the ultimate, energy efficient insulation system has led in the past few years to a fascinating rediscovery and application of some fundamental concepts of thermodynamics: specifically, the second law and the use of entropy production rates and availability (or exergy) for design optimization purposes. The classical approach has been to minimize the heat flow between surfaces at different temperatures.

The concept of a single vapor-cooled shield in an insulation has been treated theoretically as far back as 1959 in Scott's classic textbook on cryogenics [1] and designs employing them were described not much later [2]. Paivanas, et al., obtained a patent [3] and later reported on the use of uniformly spaced multiple shields which were cooled by the boil-off from the insulated dewar [4]. Eyssa and Okasha [5] considered only radiative heat exchange between shields and minimized the total refrigeration power required. Hilal, et al., [6,7] used a similar minimization of refrigeration power as the design basis. Related works were reported by Bejan, et al., [8-11].

Recently, Bejan [12] proposed a new point of view, based on the second law of thermodynamics, which considers thermal insulations as dissipators of useful mechanical power (i.e. the availability or exergy) or, alternately, as generators of irreversibility or entropy. Thus, in this method, optimization of an insulation corresponds to minimization of either the entropy production rate or the irreversibility, or the decrease of availability. Various applications of this concept to insulation systems have been documented subsequently [13,14].

Our work grew out of an examination of Cunningham's paper [13] who utilized a numerical technique to find optimum temperatures at given locations for one and two shields for a thermal conductivity function of the form

$k_1 T^{0.6}$. Although several equations seemed to be incorrectly printed we have found two of the design curves to be essentially correct. Thus, our purpose was

1. To develop a simple optimization technique;
2. To generalize the results to a broader class of insulations; and
3. To develop simple design methods for cooled shields.

The essentials of this report were already published [15].

ANALYSIS

We accept the previously developed concept that to optimize an insulation system is equivalent to minimizing the entropy production rate. In addition, we assume one-dimensional heat flow and that the heat capacity of the boil-off gas is adequate to do the cooling for all shields and does not impose a restriction on the optimization. In contrast to Rejan [9,11] who has developed a constrained optimization based on the heat capacity of the boiloff we employ the argument that in all practical systems the boil-off is generated by cooling of some equipment in addition to the heat leakage across the insulation.

Parallel heat paths, e.g. supports, have not been considered. However, each path can be optimized separately using its own thermal conductivity function. Then a design decision has to be made whether the two structures should be independently cooled at their respective optimum conditions.

We examine the general situation of an insulation where equivalent thermal conductivity, k , can be expressed as a two-term function of the absolute temperature

$$k = k_1 T^m + k_2 T^n \quad (1)$$

where, typically, the first term represents actual conduction with $m \geq 1$ and the second term represents radiation with $n \geq 3$. In the following, m and n can be any value except -1.

The heat flow across a layer of insulation can be expressed in terms of Fourier's law

$$q \, dx = Ak \, dT \quad (2)$$

Substituting k from Eq. (1) and integrating across a layer from one end at 1, to the other at 2, yields

$$q = \frac{A}{x_2 - x_1} \left[\frac{k_1}{m+1} (T_2^{m+1} - T_1^{m+1}) + \frac{k_2}{n+1} (T_2^{n+1} - T_1^{n+1}) \right]. \quad (3)$$

Now consider the insulation with a cooled shield at T_S located at x between a hot surface at T_H and a cold one at T_C , separated by the insulation thickness, t , as shown in Fig. 1a. The entropy production rate for the insulation can be determined from the heat flows and temperatures as follows

$$\dot{S} = -\frac{q_H}{T_H} + \frac{q_C}{T_C} + \frac{q_S}{T_S} \quad (4)$$

where $q_S = q_H - q_C$.

The heat flow terms can be expressed in the form of Eq. (3) and the resulting expression can be non-dimensionalized using the following terms

$$s \equiv \frac{\dot{S}t}{Ak_H} \text{ where } k_H = k \text{ at } T_H, \quad (5)$$

$$P \equiv \frac{T_S}{T_C}, \quad (6)$$

$$R \equiv \frac{T_C}{T_H}, \quad (7)$$

$$\gamma \equiv \frac{k_2(m+1)}{k_1(n+1)} T_H^{n-m}, \quad (8)$$

and

$$X \equiv \frac{x}{t}. \quad (9)$$

The resulting equation is

$$\begin{aligned}
 & s(m+1) \left(1 + \gamma \frac{n+1}{m+1}\right) \\
 &= \frac{1}{1-X} \{[(PR)^{m+1} - (PR)^m - 1 + (PR)^{-1}] \\
 &+ \gamma [(PR)^{n+1} - (PR)^n - 1 + (PR)^{-1}]\} \\
 &+ \frac{1}{X} \{R^m [P^{m+1} - P^m - 1 + P^{-1}] \\
 &+ \gamma R^n [P^{n+1} - P^n - 1 + P^{-1}]\} \quad (10)
 \end{aligned}$$

Since R , the overall temperature ratio, is generally known, s is a function of P and X , and its extreme value can be found by differentiating it with respect to each variable separately and setting the results equal to zero. This procedure yields two equations to be solved simultaneously: $\partial s / \partial P = 0$ and $\partial s / \partial X = 0$. Because of the regular form of the expressions, one of the final two equations contains only a single unknown as follows:

$$\begin{aligned}
 & \frac{R^m F(m,P) + \gamma R^n F(n,P)}{[R^{m-1} D(m,P) + \gamma R^{n-1} D(n,P)]^2} \\
 &= \frac{F(m,PR) + \gamma F(n,PR)}{[D(m,PR) + \gamma D(n,PR)]^2} \quad (11)
 \end{aligned}$$

$$\frac{X}{1-X} = - \frac{R^{m-1} D(m,P) + \gamma R^{n-1} D(n,P)}{D(m,PR) + \gamma D(n,PR)} \quad (12)$$

where the following functionals were used:

$$F(b,B) \equiv R^{b+1} - B^b - 1 + B^{-1} \quad (13)$$

$$D(b,B) \equiv (b+1) B^b - bB^{b-1} - B^{-2}. \quad (14)$$

Thus, to find the optimum temperature and location for a shield, Eq. (11) can be solved for P , and then X can be calculated from Eq. (12). The heat to be removed by the shield, $q_s = q_H - q_C$, can be found, as before, from Eq. (3). In dimensionless form the equation becomes

$$\begin{aligned} \frac{q_s t}{Ak_H T_H} (m+1) \left(1 + \gamma \frac{n+1}{m+1}\right) \\ = \frac{1 - (PR)^{m+1} + \gamma[1 - (PR)^{n+1}]}{1 - X} \\ = \frac{(PR)^{m+1} - R^{m+1} + \gamma[(PR)^{n+1} - R^{n+1}]}{X}. \end{aligned} \quad (15)$$

For multiple shields t_i represents the distance between the two surfaces surrounding the i -th shield on either side, $T_{H,i}$ and $T_{C,i}$ are the temperatures of these two surfaces, $X_i = x_i/t_i$ is the location of the shield relative to t_i , and x_i' is the location of the shield relative to the cold wall as shown in Fig. 1b. To determine the optimum temperatures and locations for multiple shields, first we assumed a temperature for the first shield next to the cold wall, then we used Eqs. (11) and (12) to find the temperature and location of the second shield. This process was repeated for the rest of the shields and the hot wall. Thus, each shield was optimized consecutively with respect to the two surfaces on either side. With given values of the overall temperature ratio, R , and of the number of shields, the process requires iterative solution.

To put the results into proper perspective, the entropy production rates can be compared to the thermodynamically minimum rate obtainable through spatially continuous cooling. According to Bejan [12], this rate is

$$\dot{S}_{\min} = \frac{A}{t} \left[\int_{T_C}^{T_H} (k)^{1/2} T^{-1} dT \right]^2. \quad (16)$$

This expression was evaluated analytically for the single-term functions of k , i.e. for $\gamma = 0$, and numerically otherwise.

RESULTS AND DISCUSSION

The first set of curves, Figs 2 through 9, show the relative entropy production rates for various thermal conductivity functions and for up to four optimally cooled shields as functions of the overall temperature ratio $R \equiv T_C/T_H$. The curves show that the entropy production rate increases with decreasing values of the temperature ratio, R , and with increasing values of the exponent, m and n . Adding shields, of course, reduces the entropy production rate; but for most of the practical temperature range, say $0.01 < R < 0.4$, only three shields contribute to significant decreases and adding a fourth shield can be considered unnecessary. No shields are useful at high values of R ; but this "high" range is strongly dependent on the exponent of the temperature. The curves developed with $k = k_1 T^{0.6}$ for one and two shields were very close to those given by Cunningham [13], converted appropriately.

Study of the results of two-term conductivities reveals that the curves fall between those obtained for each of the two terms alone. If γ is small the first term, T^m , dominates; whereas if γ is large (>10), the second term, T^n , controls. Thus, general conclusions can be drawn from examining the results of the single-term conductivities.

The second set of curves, Figs. 10 through 31, show the optimum temperature ratios, T_S/T_H , and optimum locations, x'/L , of cooled shields as functions of the overall temperature ratio, T_C/T_H , for various thermal conductivity functions and with different number of cooled shields.

Figures 10 and 11 show the optimum single shield temperature ratios, $PR = T_S/T_H$, and locations, $X = x/L$, for five conductivity functions. Both of these functions generally decrease with decreasing R . The other figures in this set show shield temperatures and locations for systems with up to three

shields and for both single-term and two-term conductivities. The results are strongly non-linear. For example, for $k_1 T^3$ and $R = 0.01$, the optimum temperature ratios for three shields are about 0.09, 0.3, and 0.6 and the optimum locations are about 0.05, 0.2, and 0.5. As is to be expected, our unconstrained optimization yields a somewhat better performance per shield than Bejan's [9,11] constrained method.

The sensitivities of the entropy production rates to deviations from the optimum values of PR and X are demonstrated in the last set of curves, Figs. 32 through 35, for single shields. The sensitivity increases with the value of the exponents, m and n , but the curves are relatively flat near the minima. A ± 20 percent change from optimum, for example, has negligible effect. Thus, the system is relatively tolerant of deviations from the optimum design conditions.

Calculations with two different conductivities on the two sides of a cooled shield show that using the better insulator on both sides always yields the optimum condition. However, if for some reason two types of insulations have to be used, then the better insulator should be placed on the warm side of the shield.

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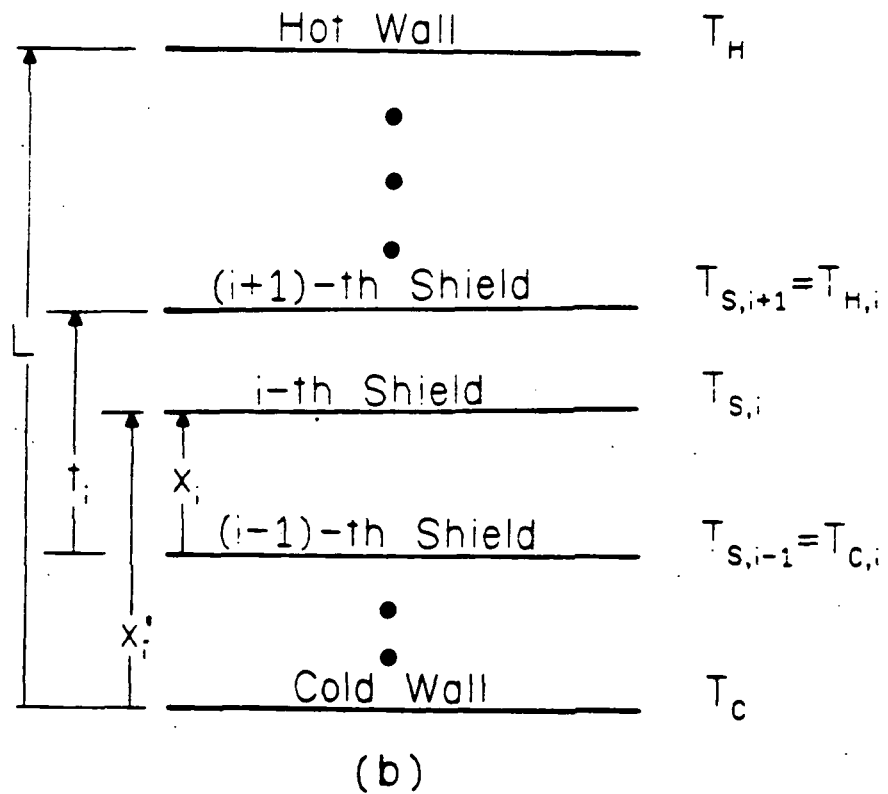
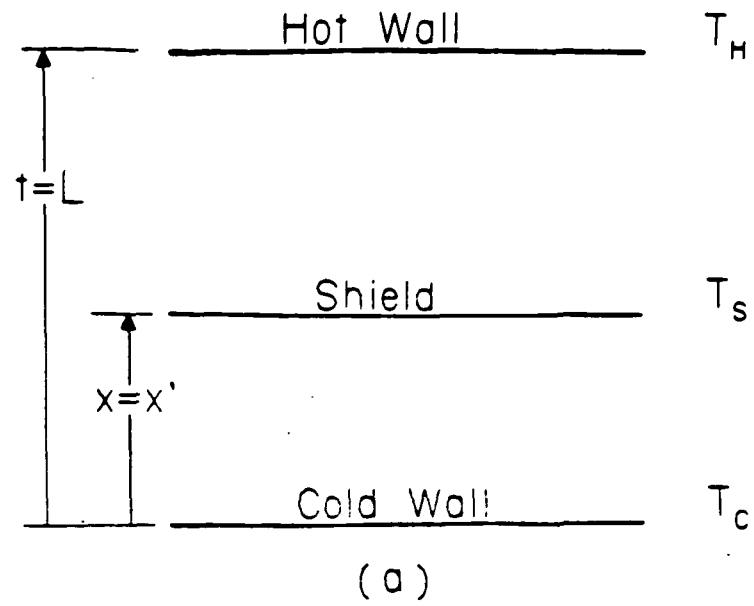


Figure 1 Schematic of the Nomenclature for (a) Single and (b) Multiple Shields

Curve Set 1: Figures 2 through 9

The effect of optimally cooled shields on
the entropy production rate for various thermal conductivities.

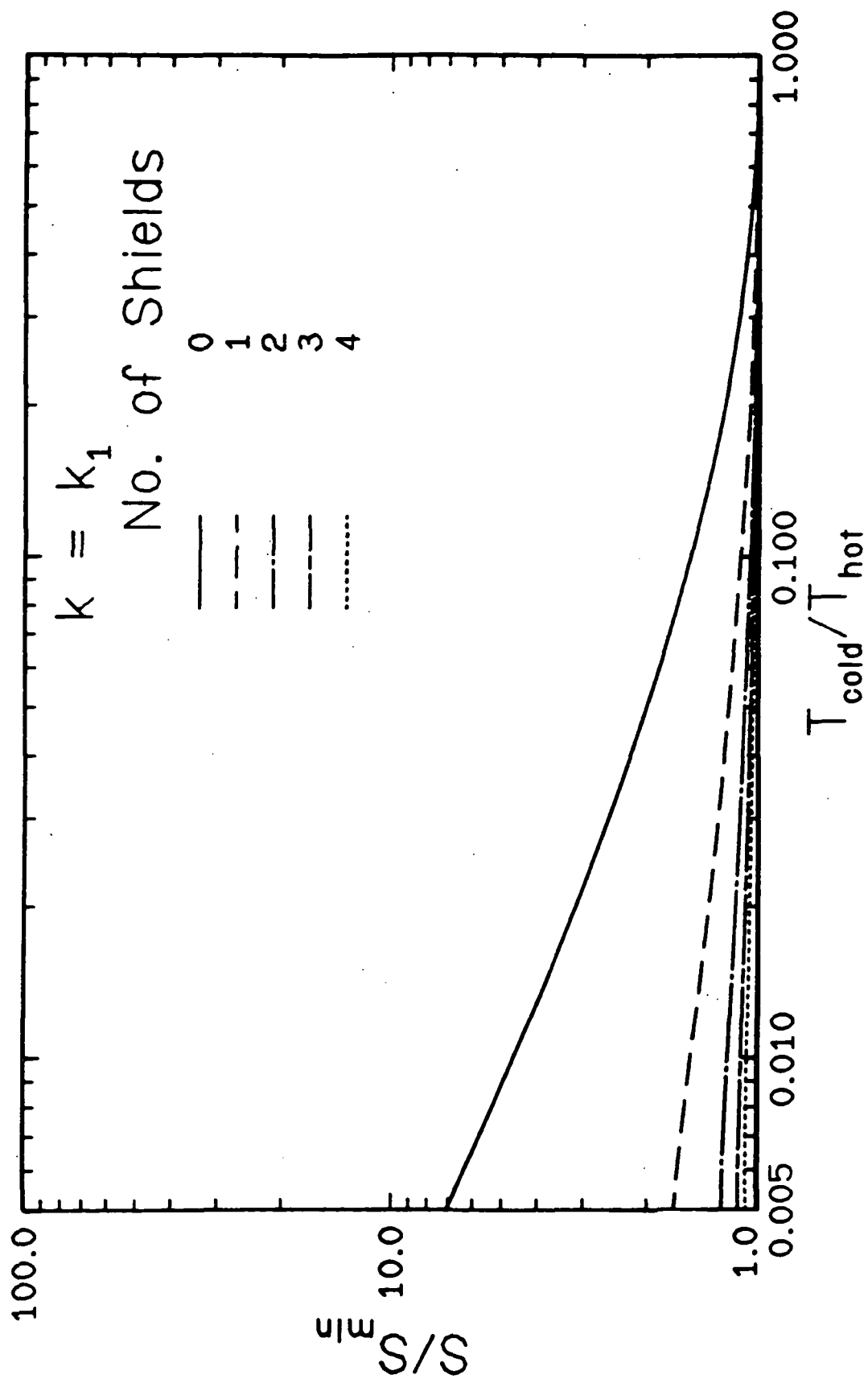


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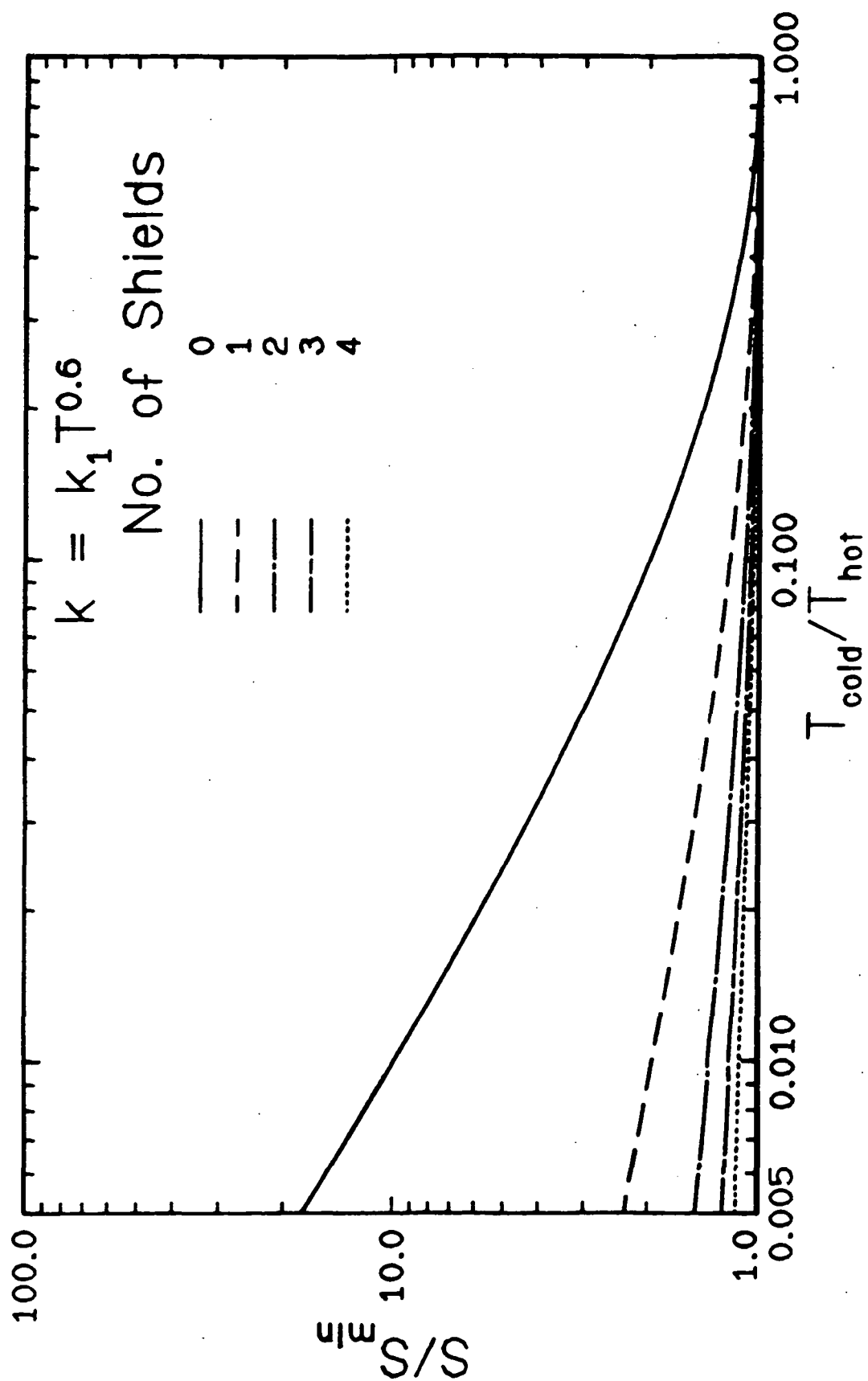


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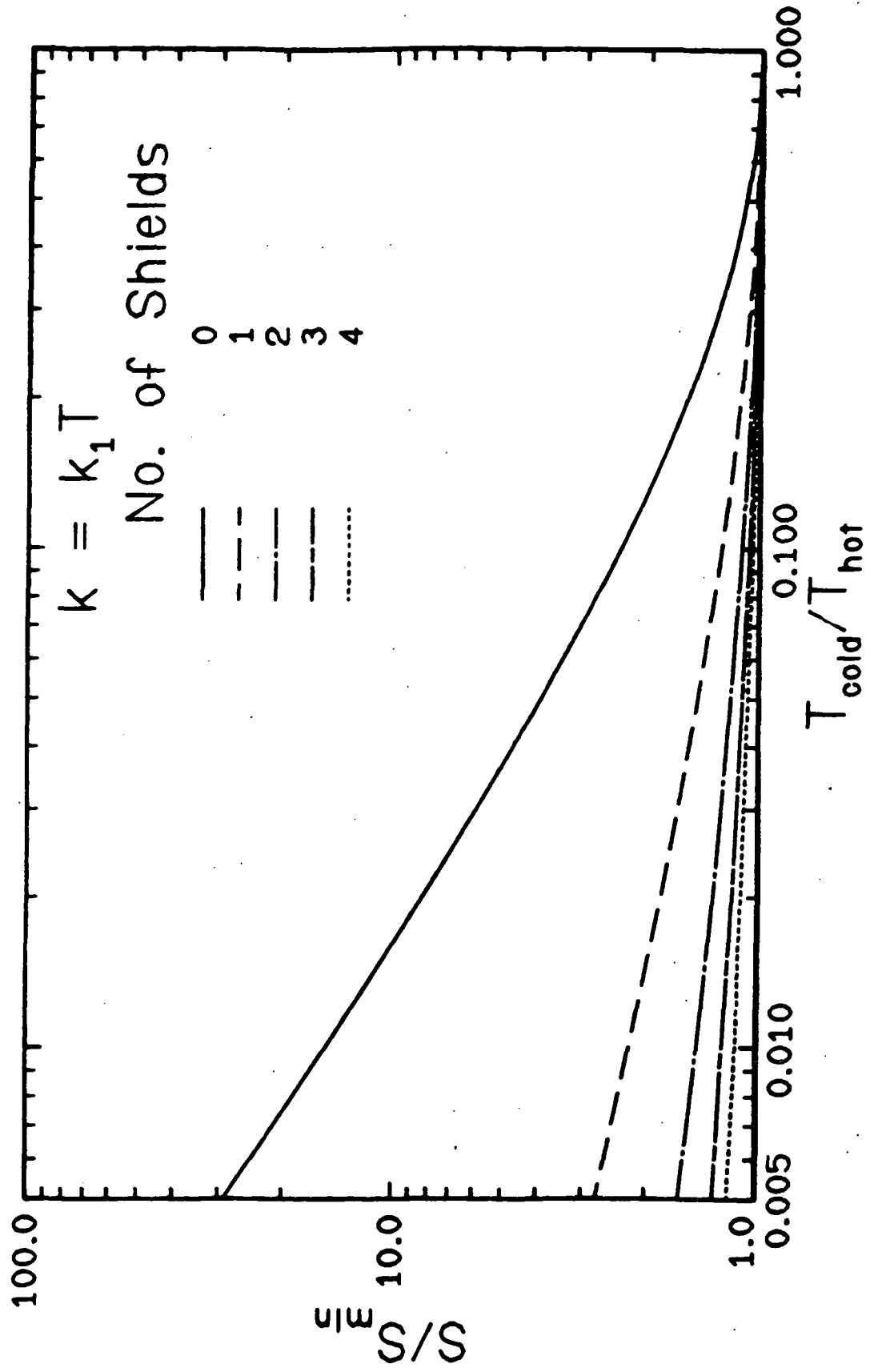


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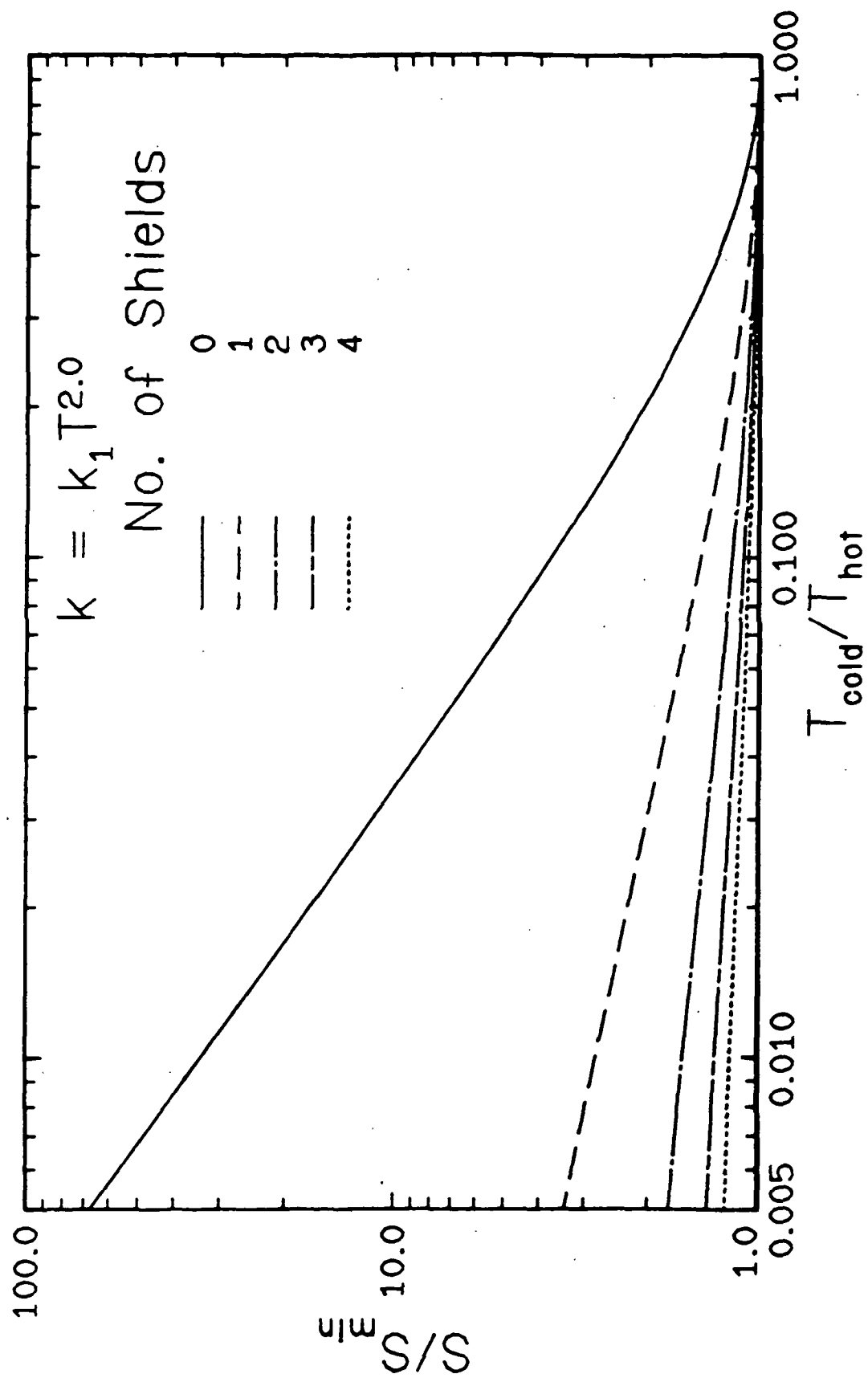


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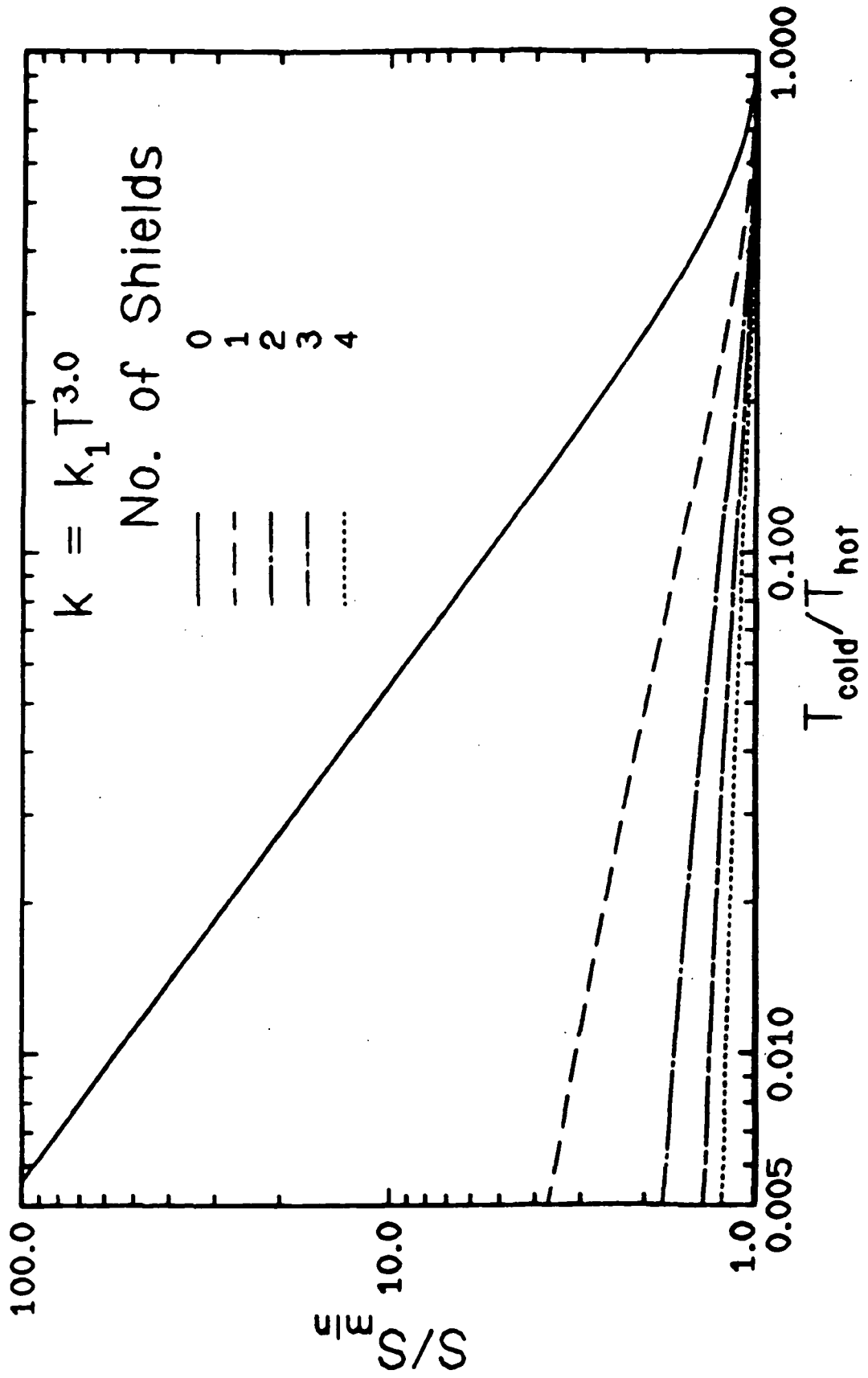


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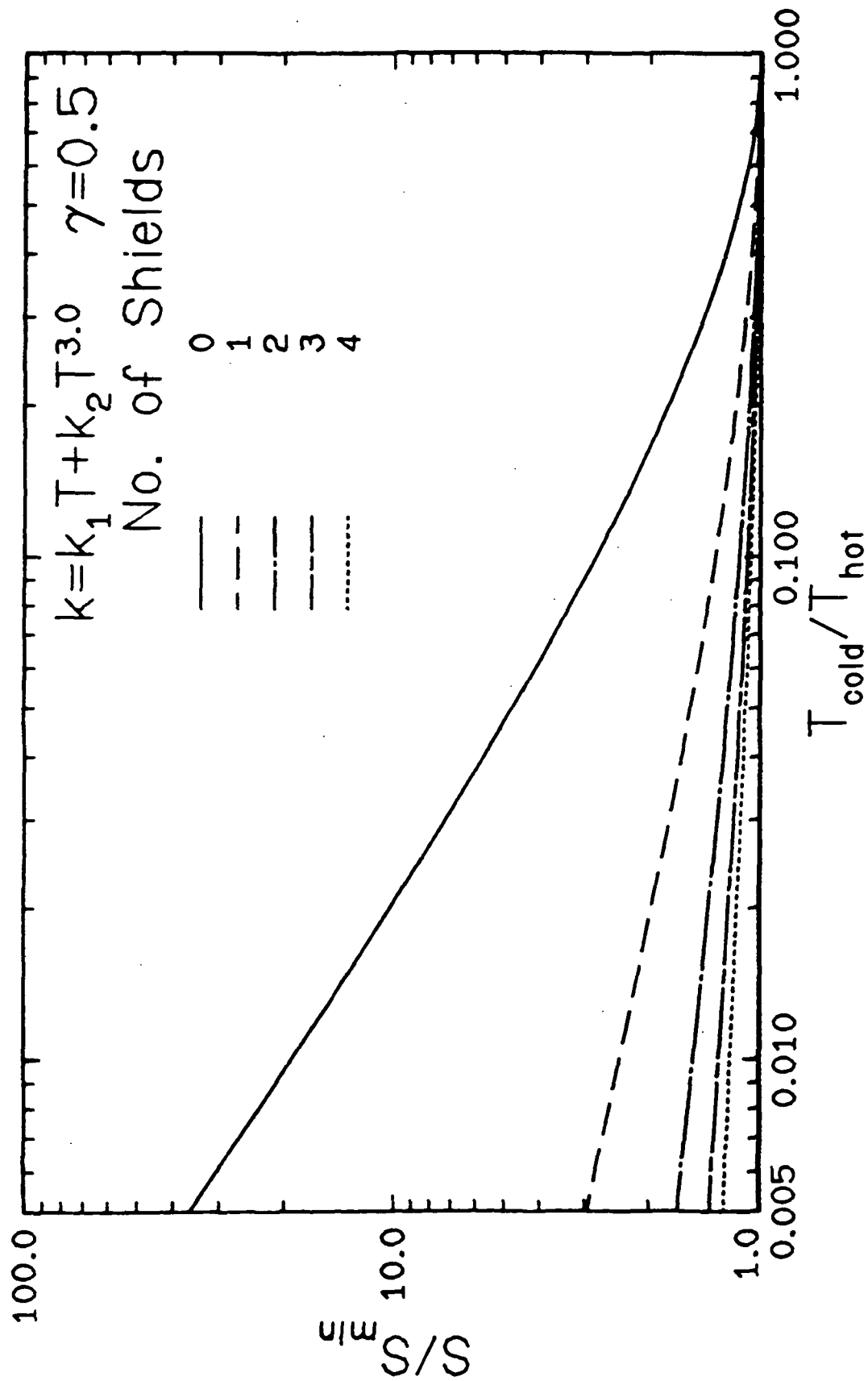


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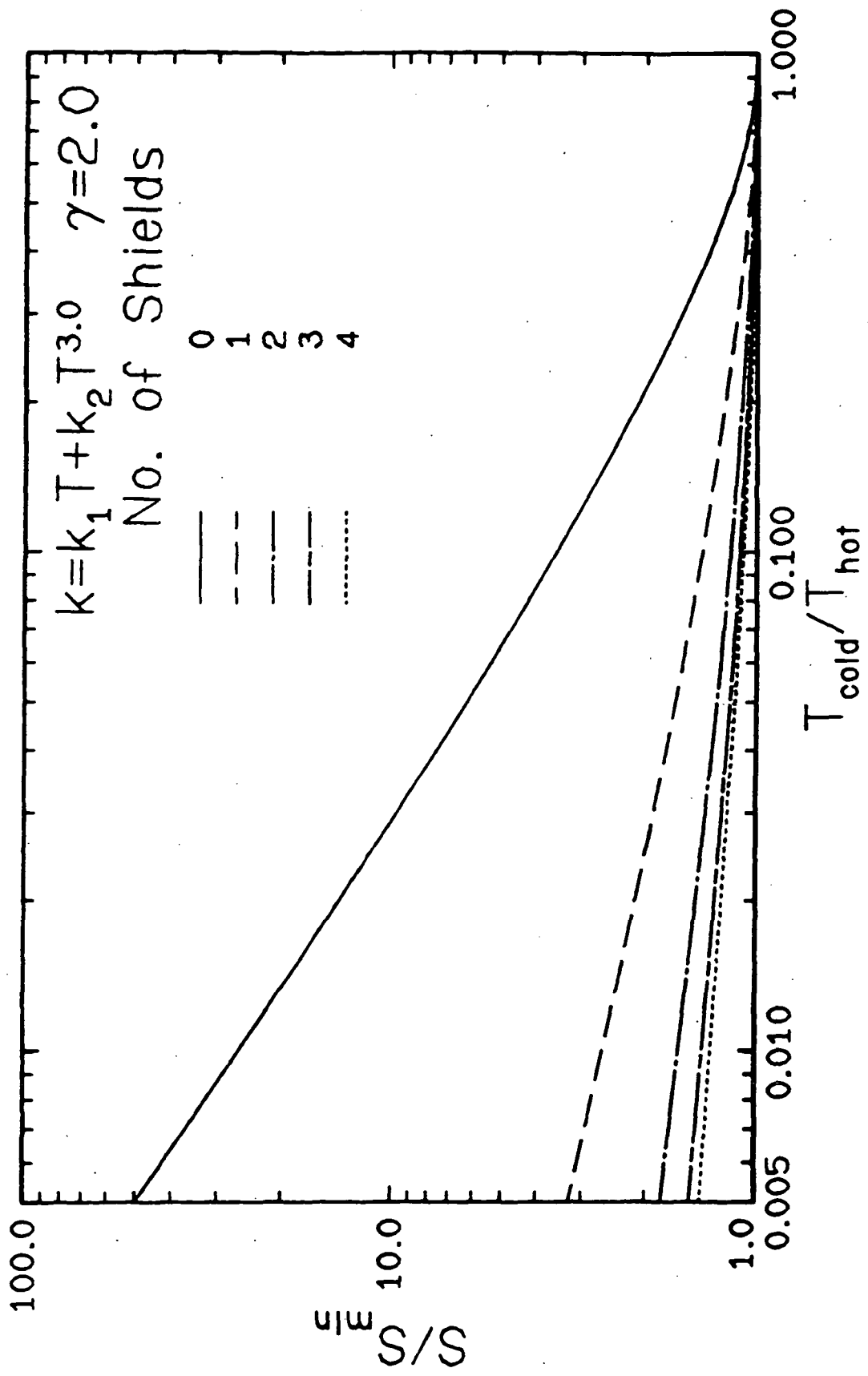


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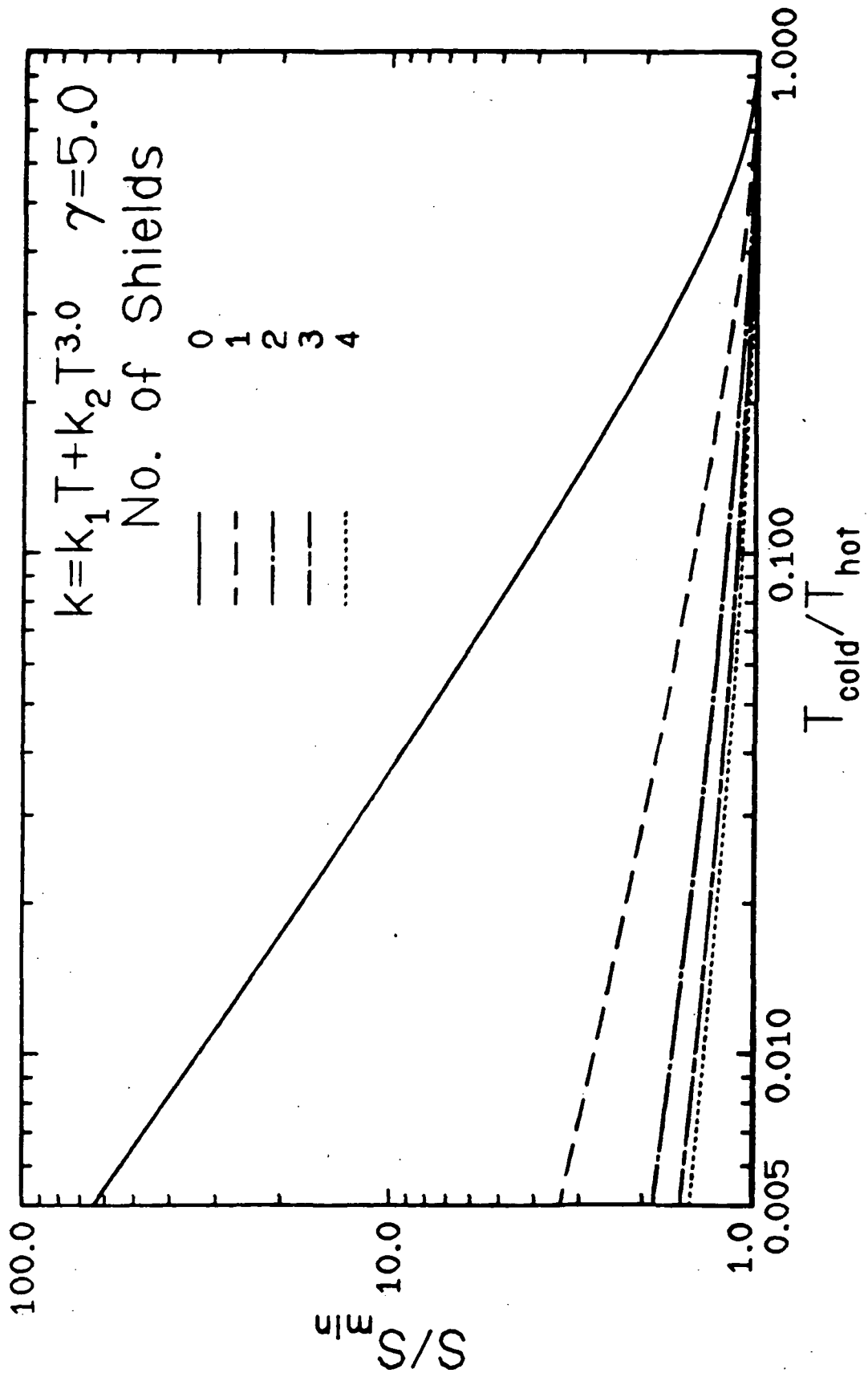


Figure 9

Curve Set 2: Figures 10 through 31

Optimal shield temperatures and locations for various thermal conductivity functions with different number of shields.

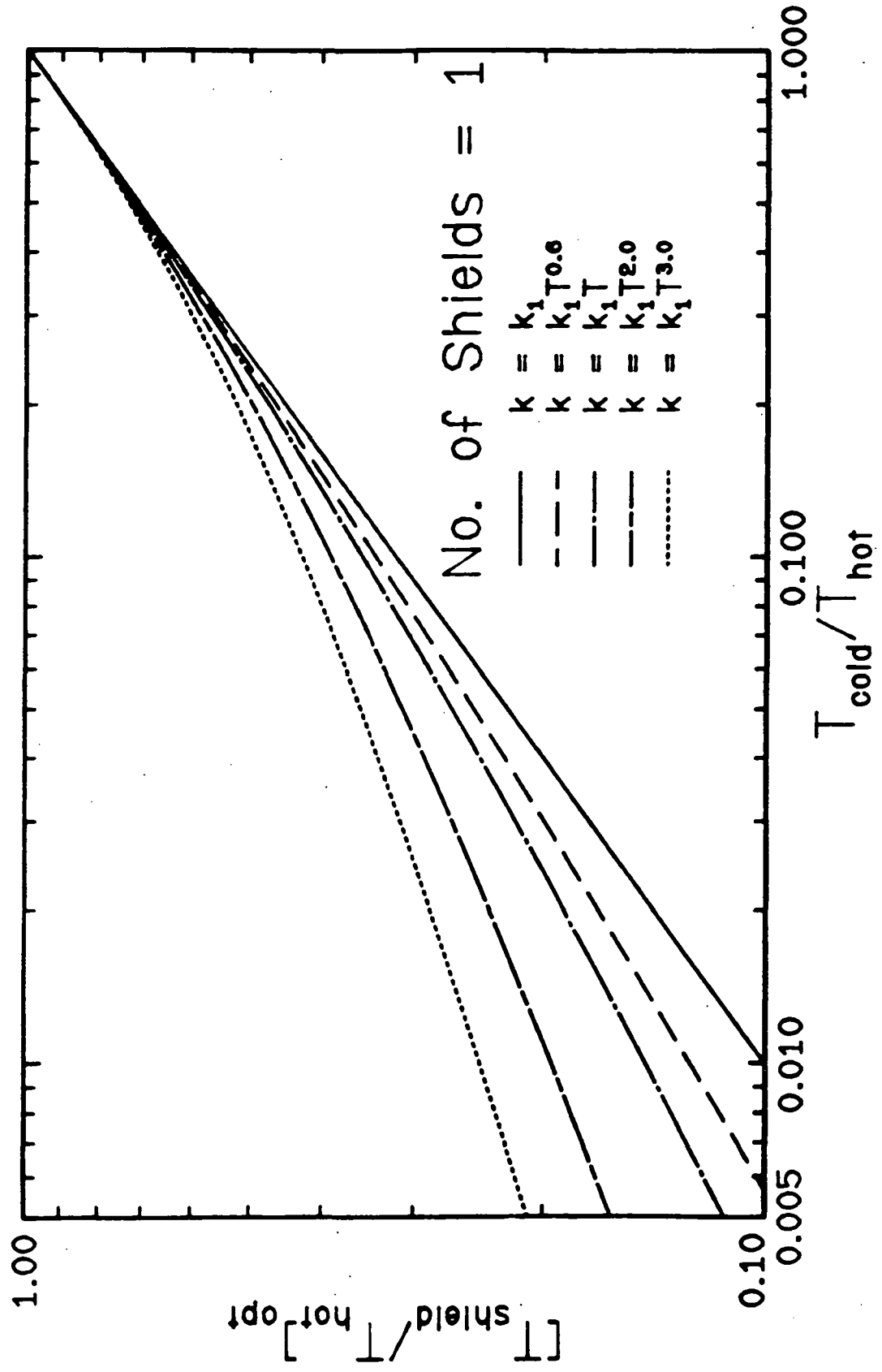


Figure 10

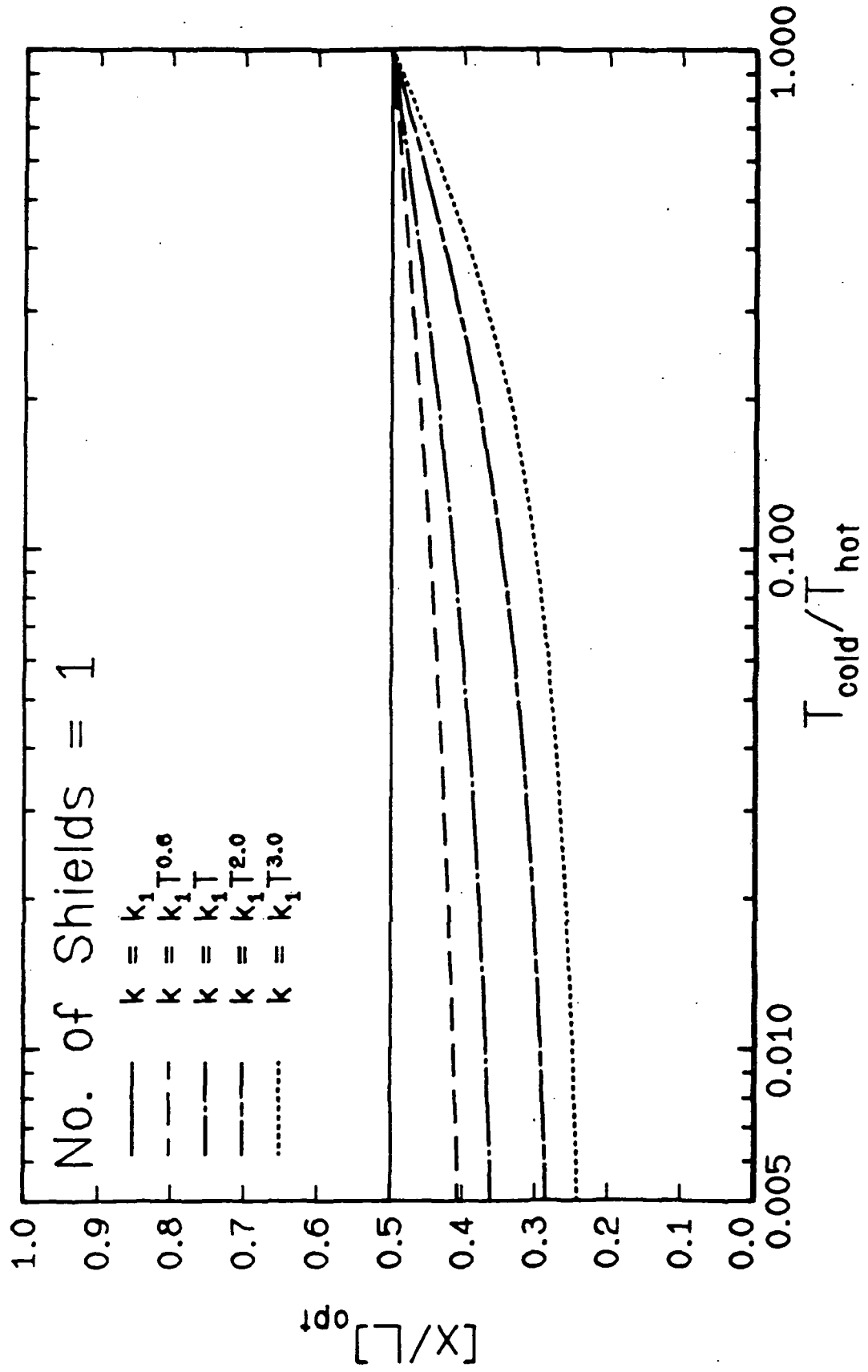


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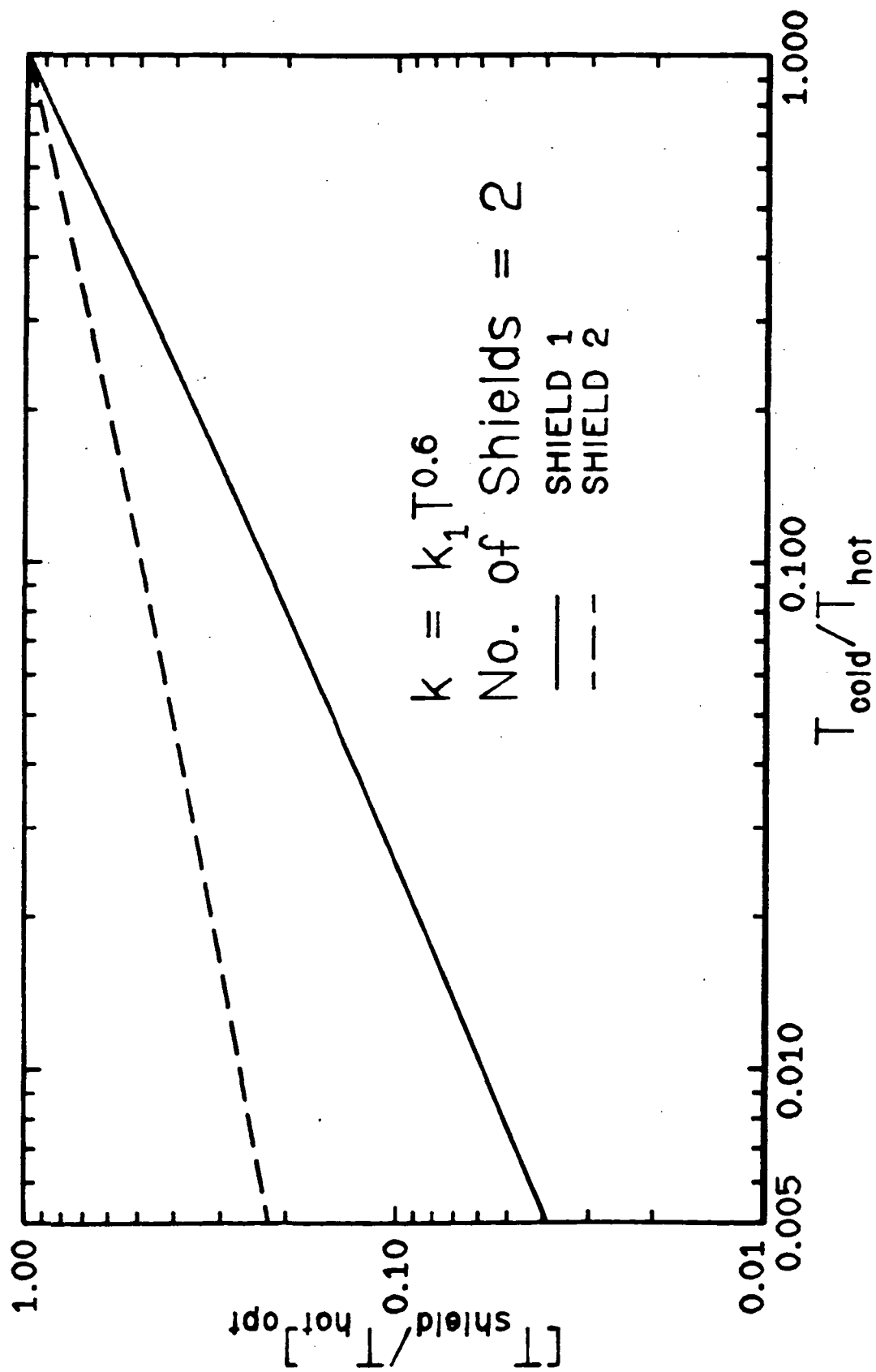


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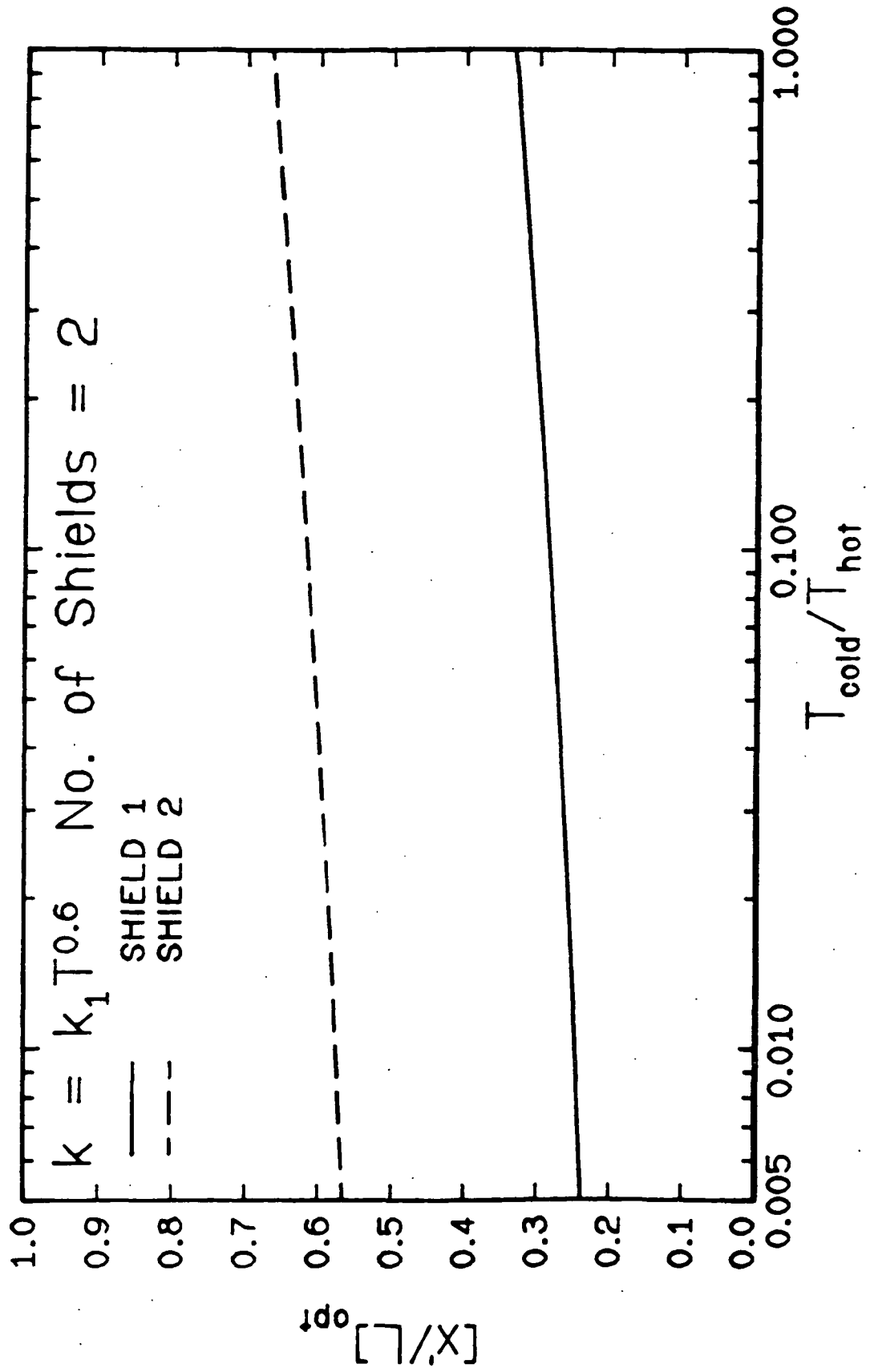


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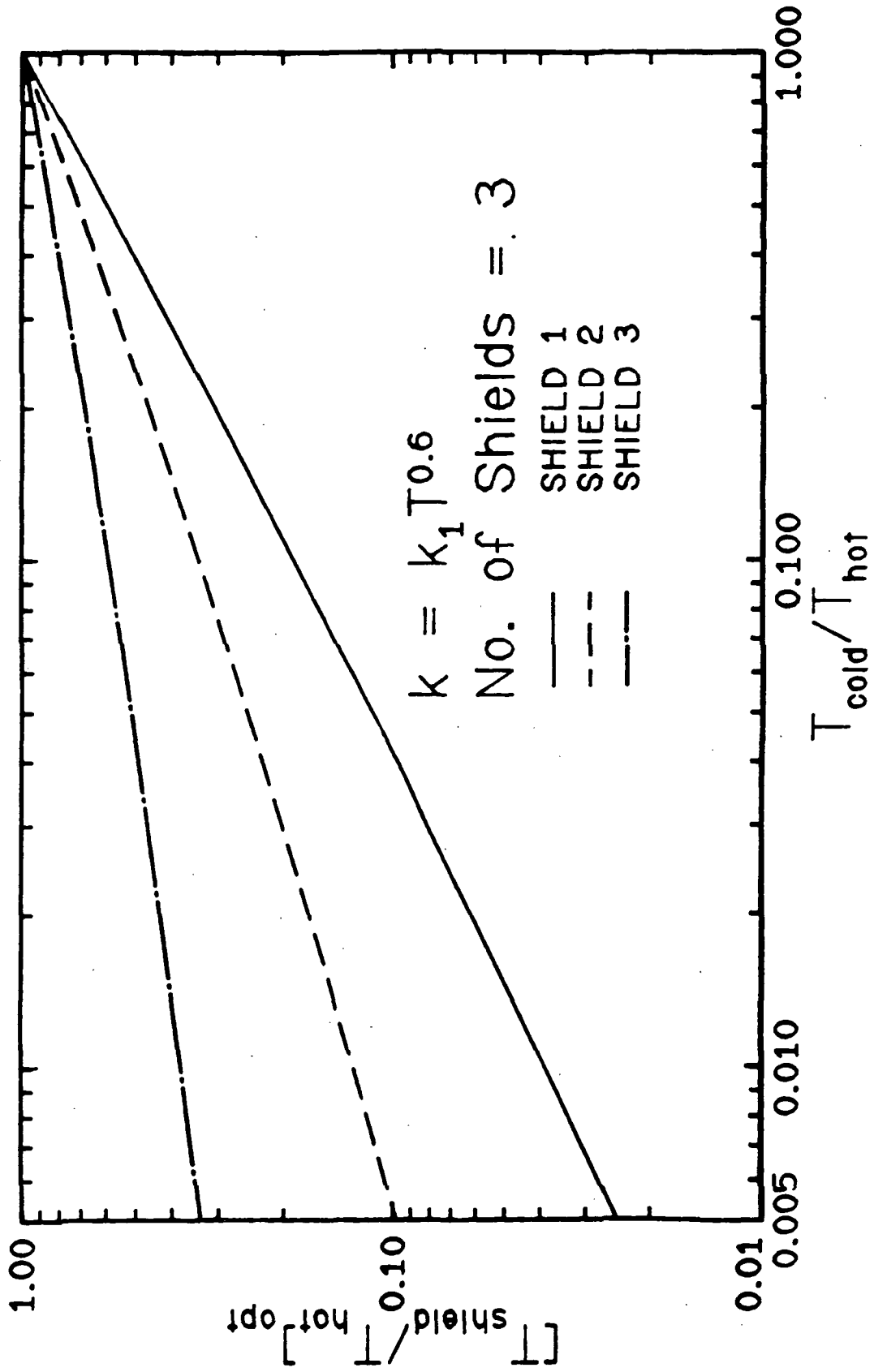


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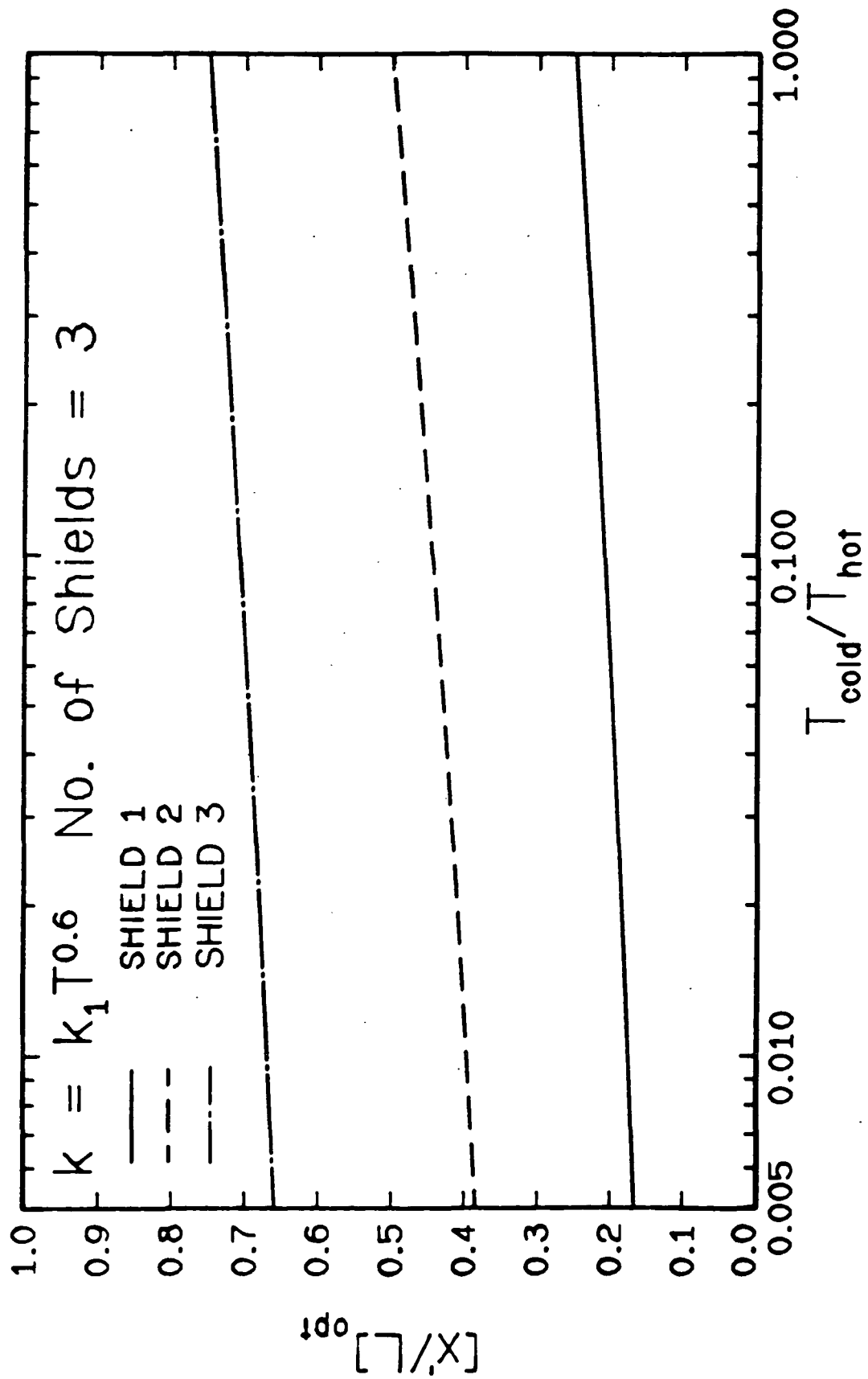


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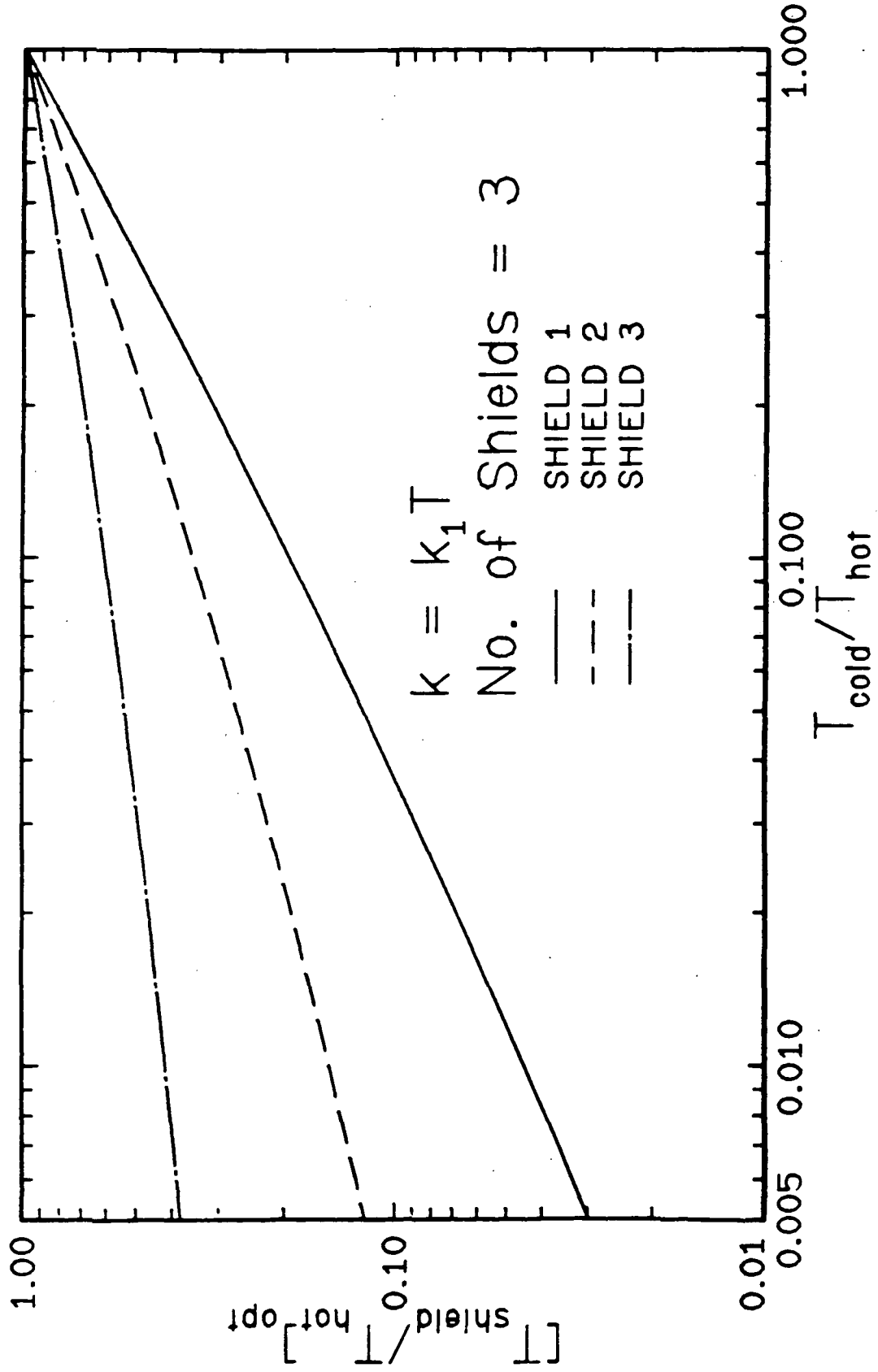


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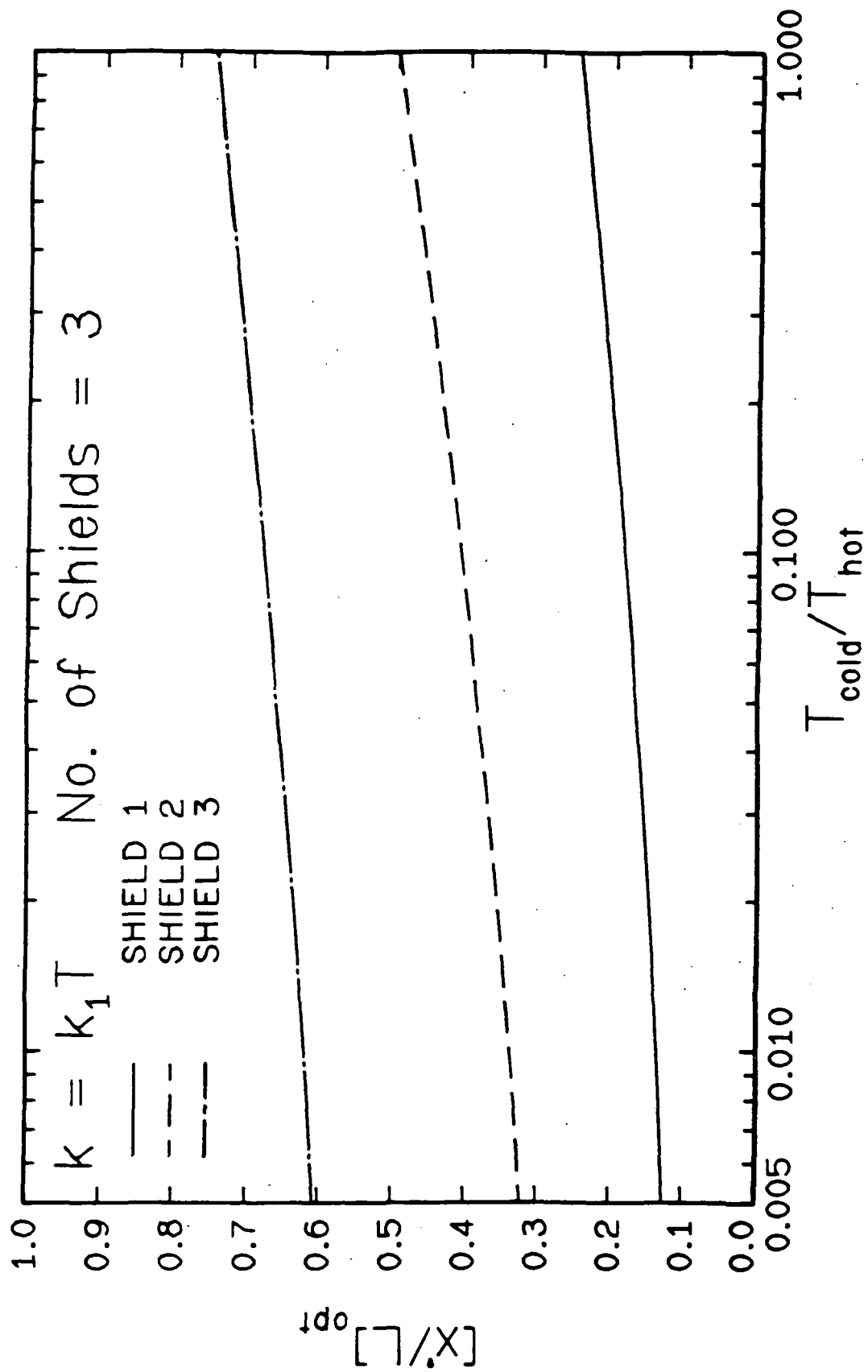


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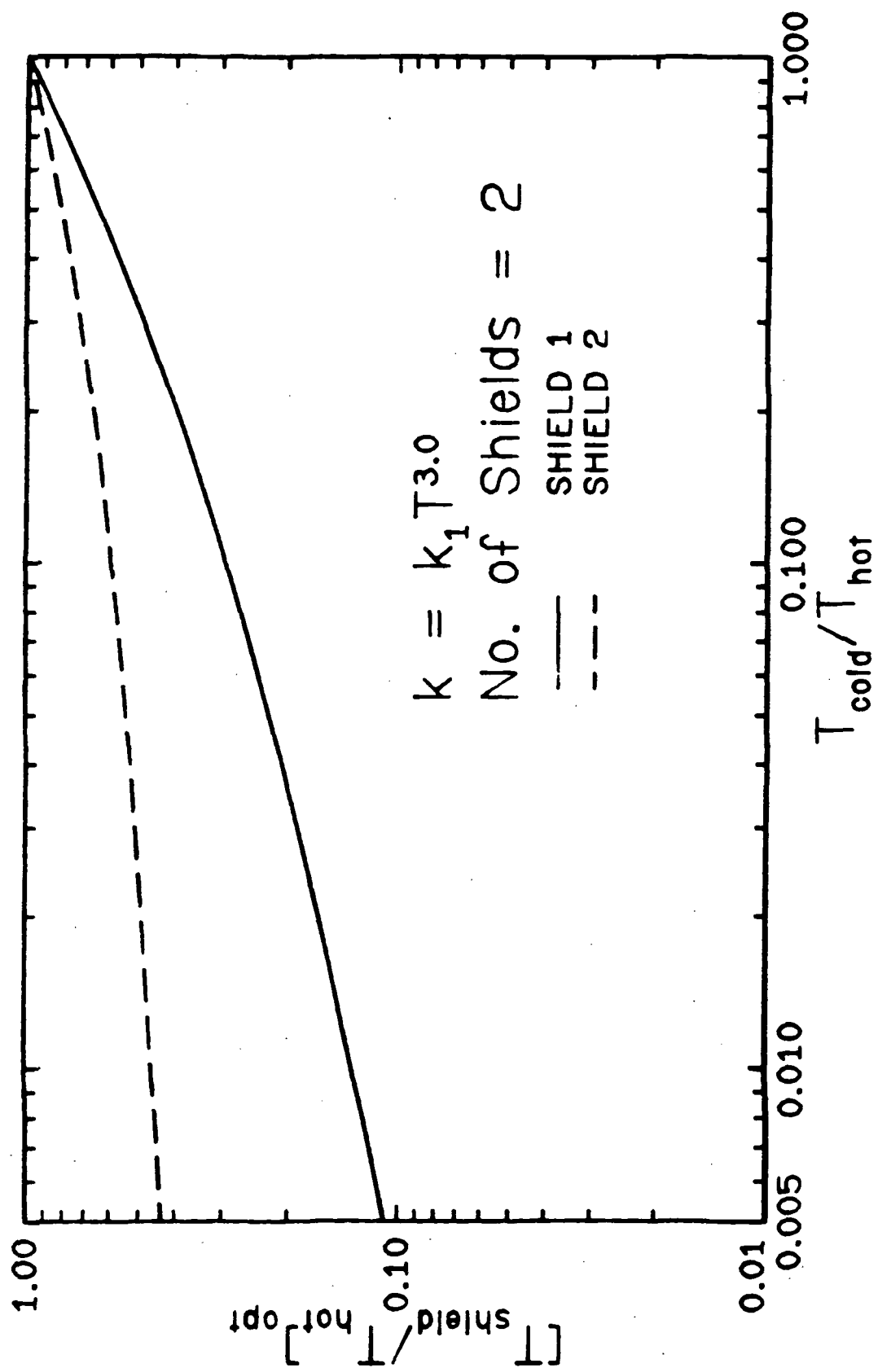


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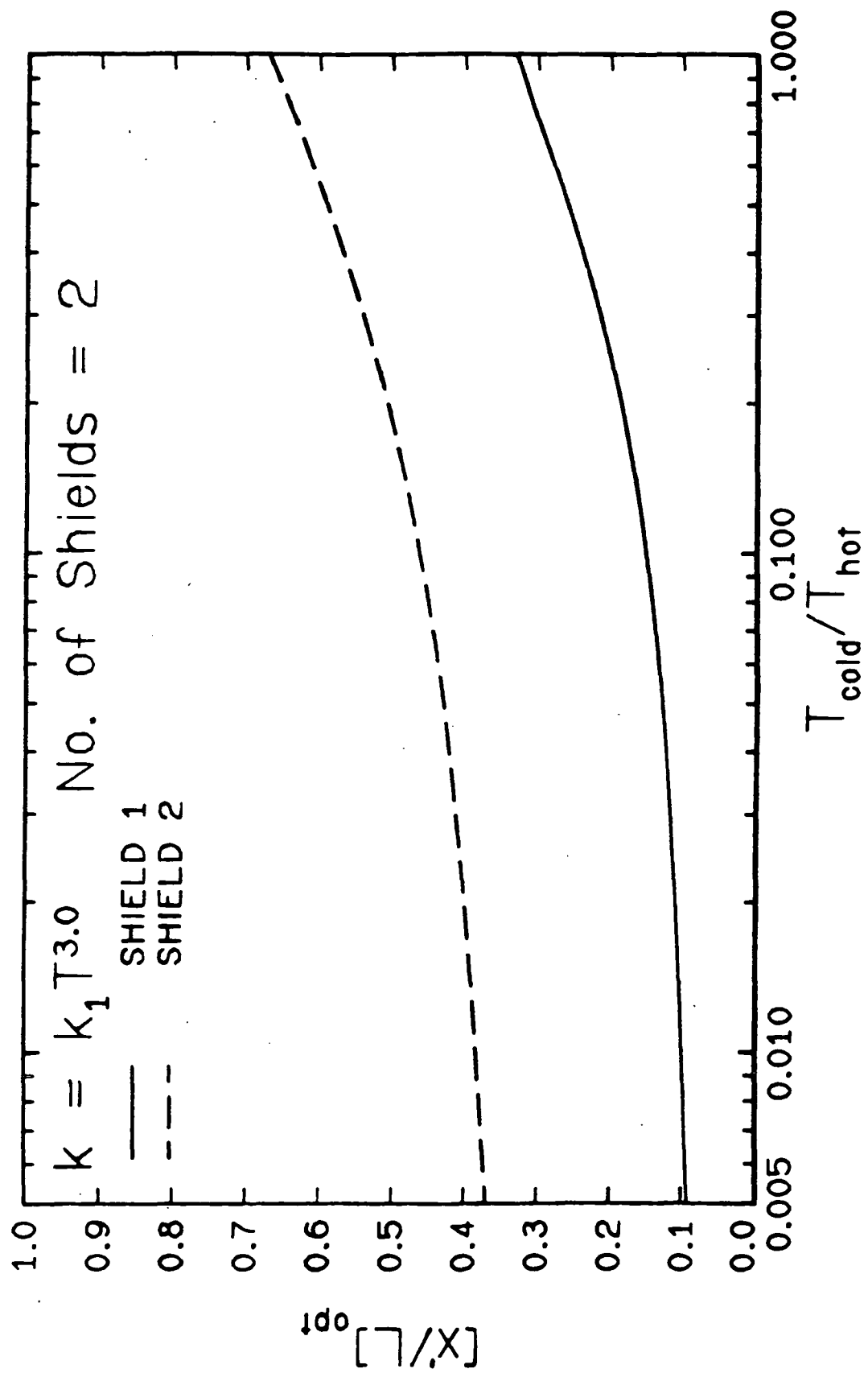


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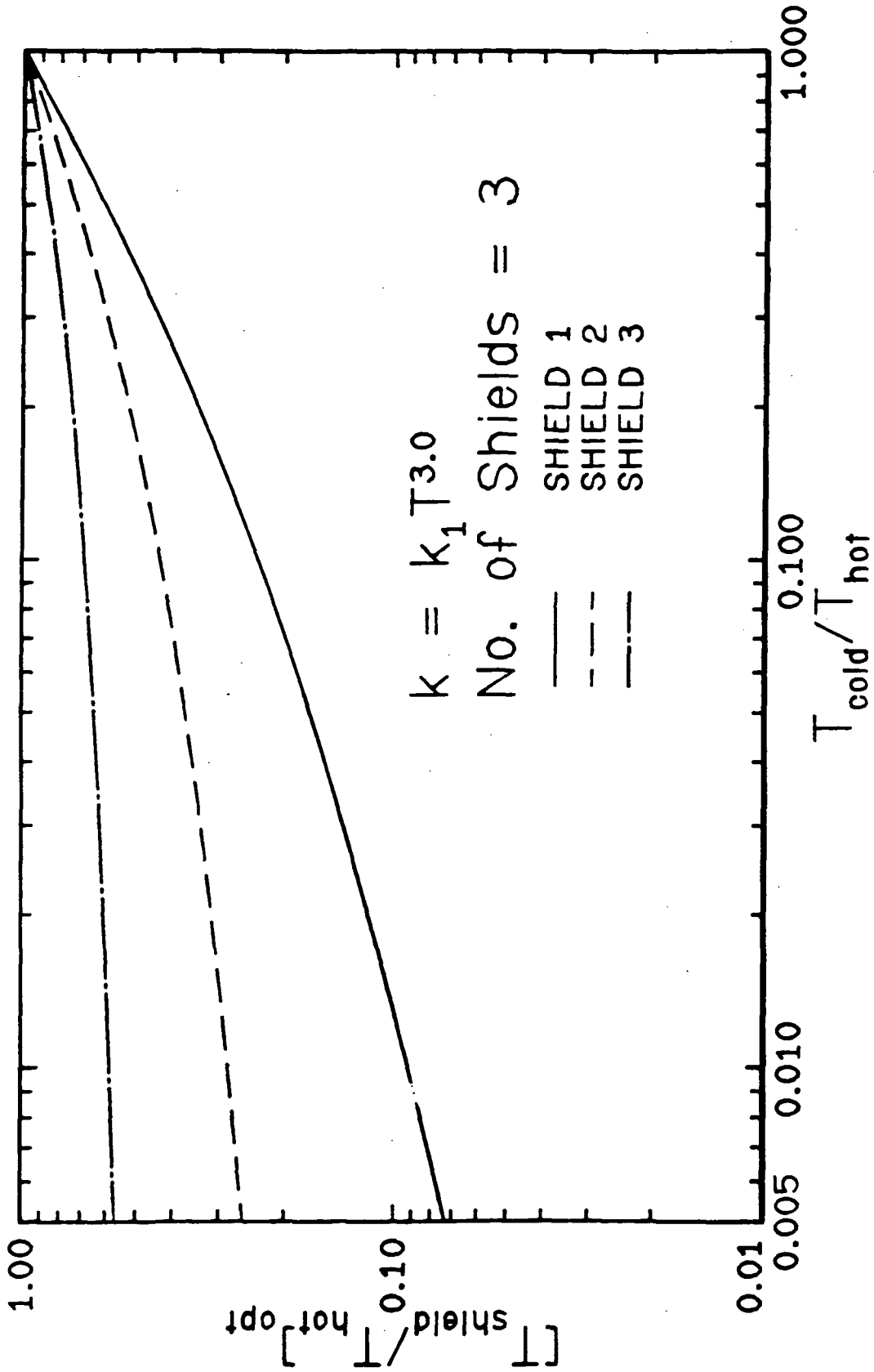


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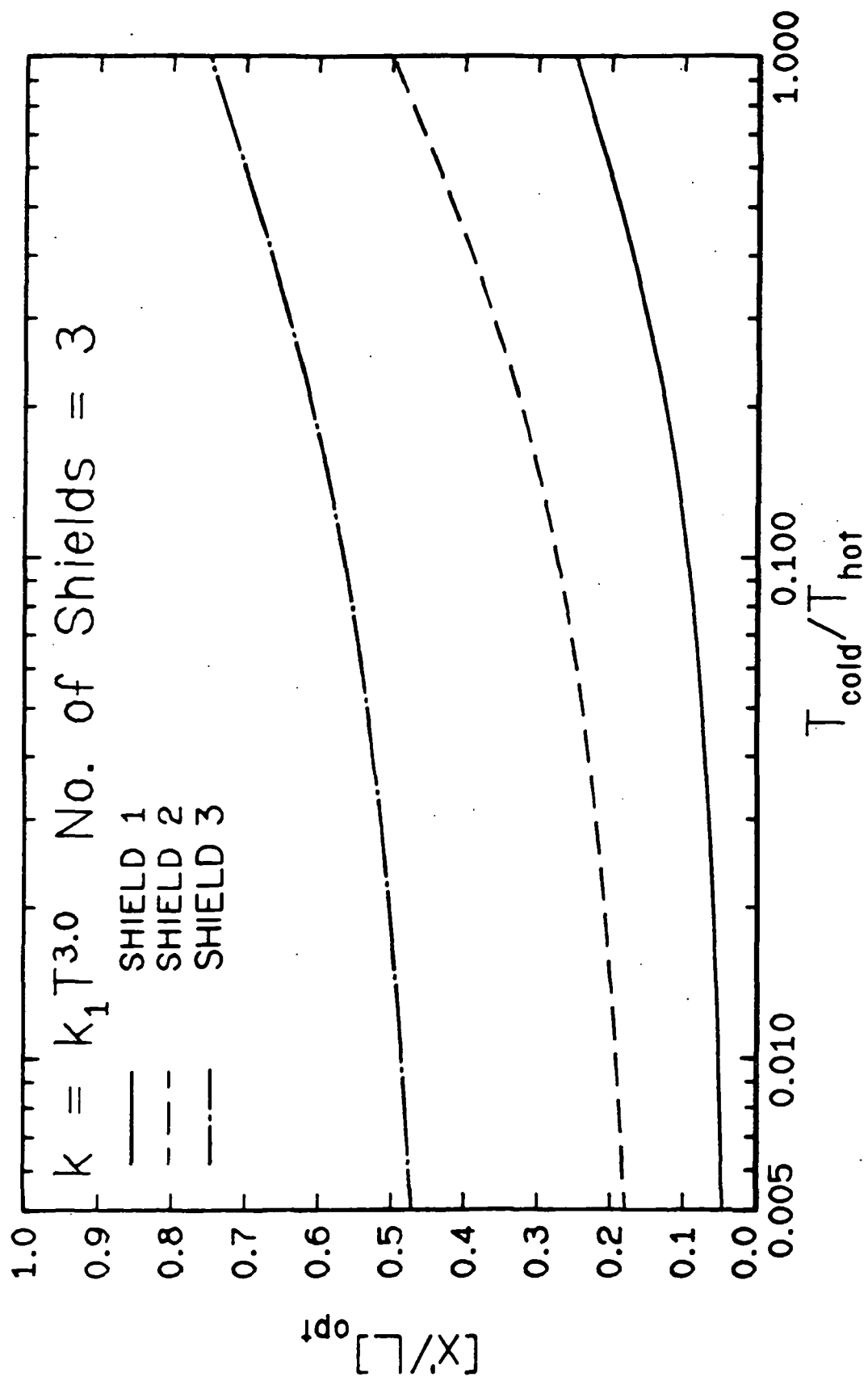


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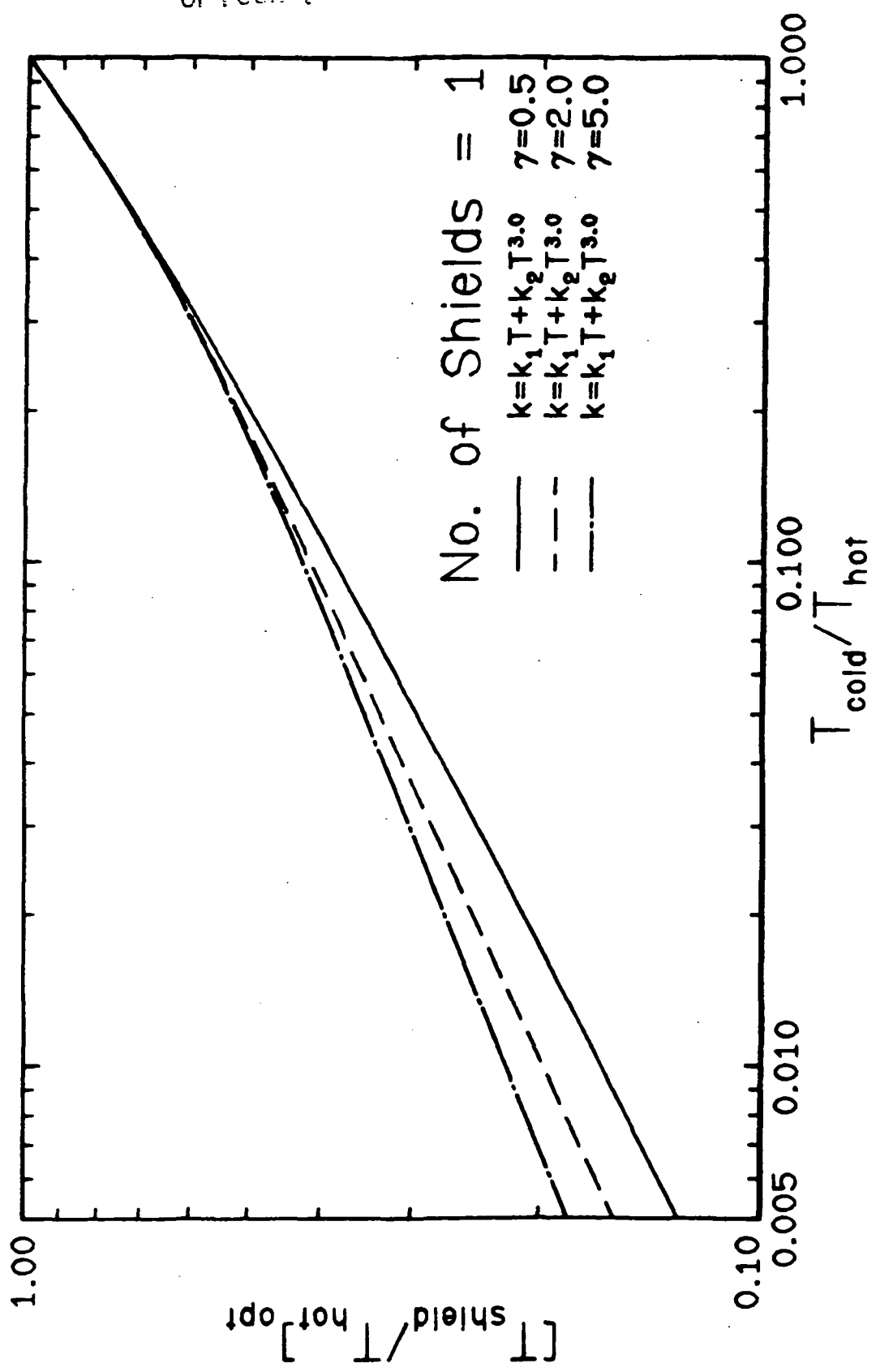


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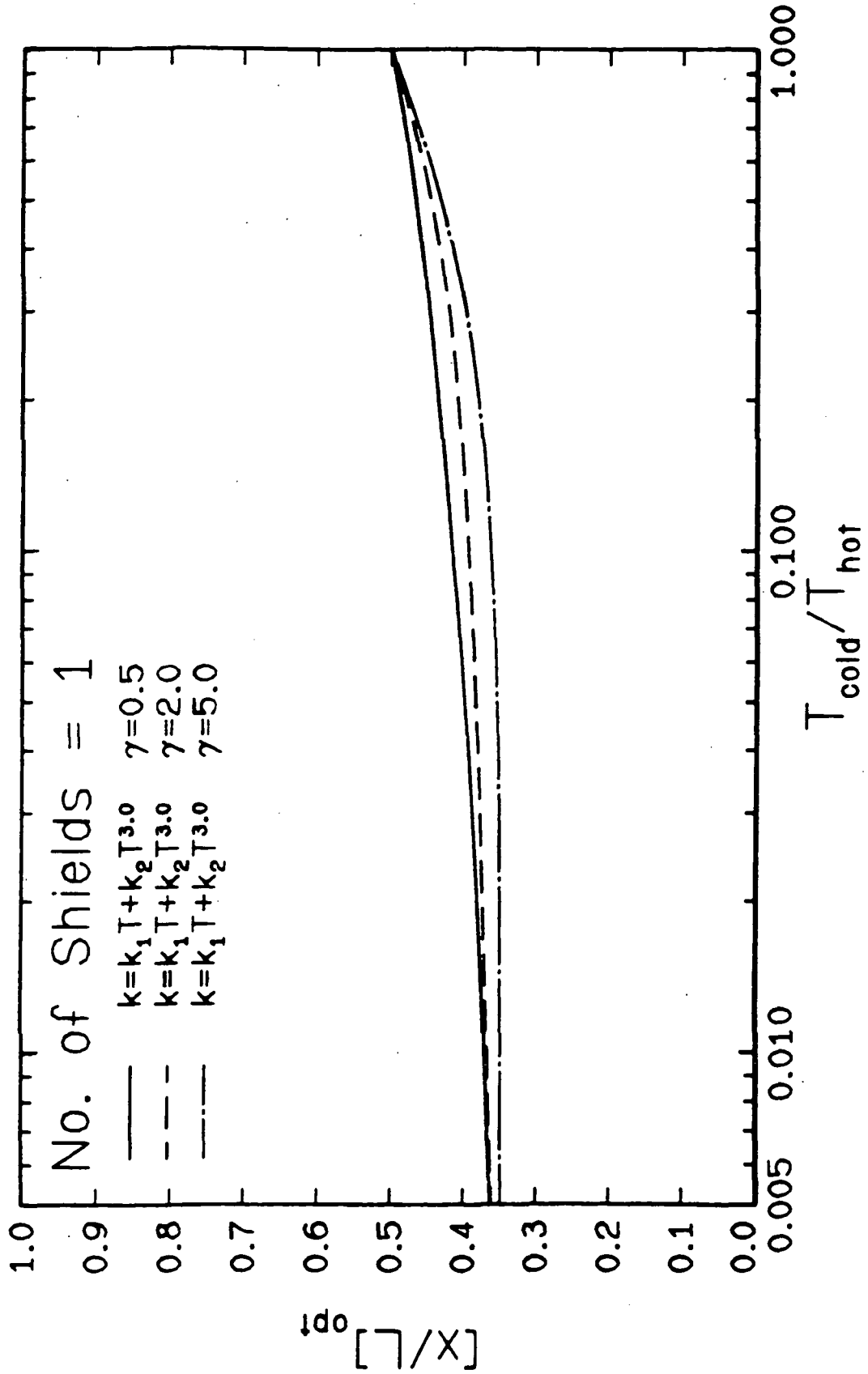


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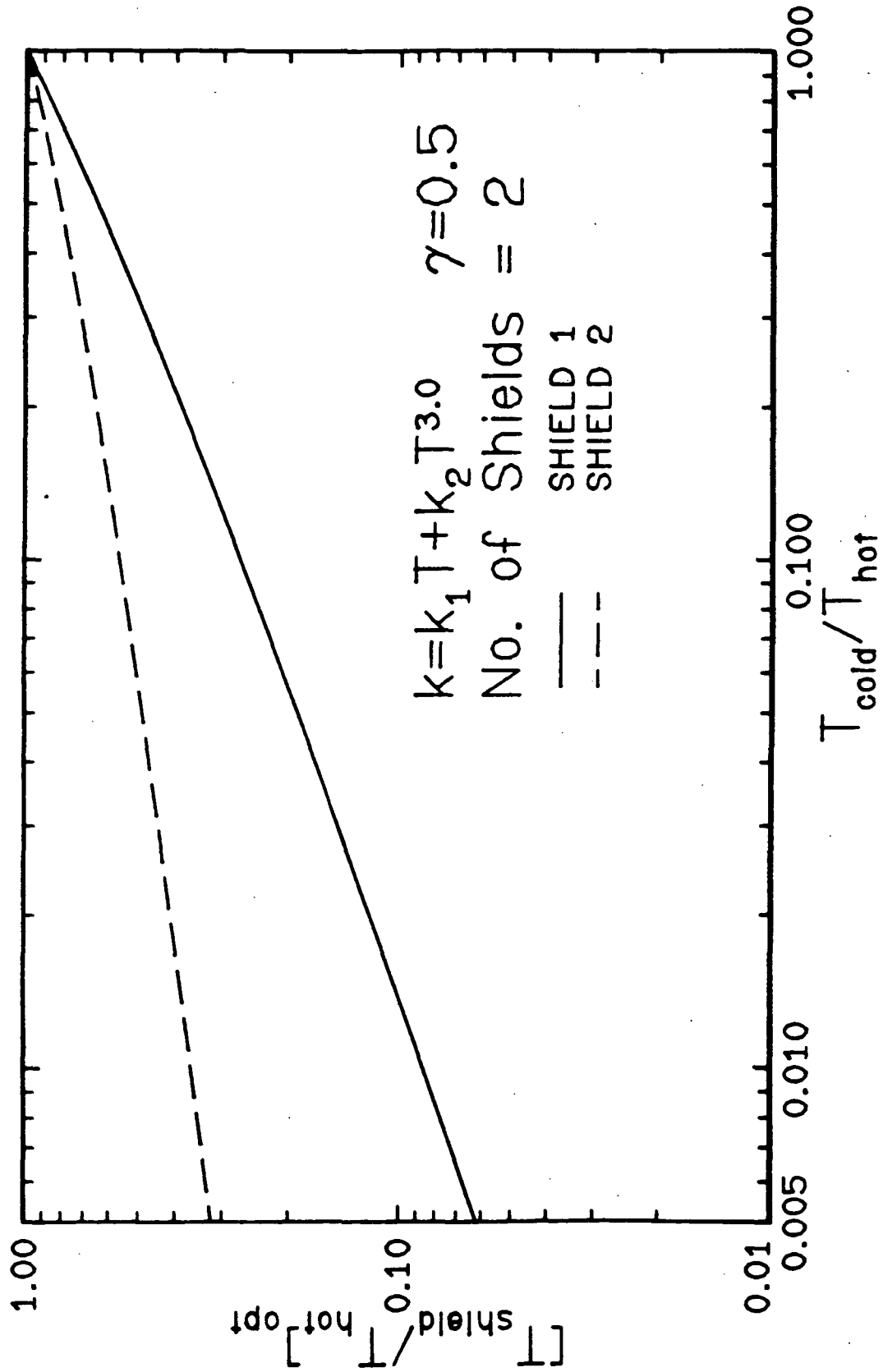


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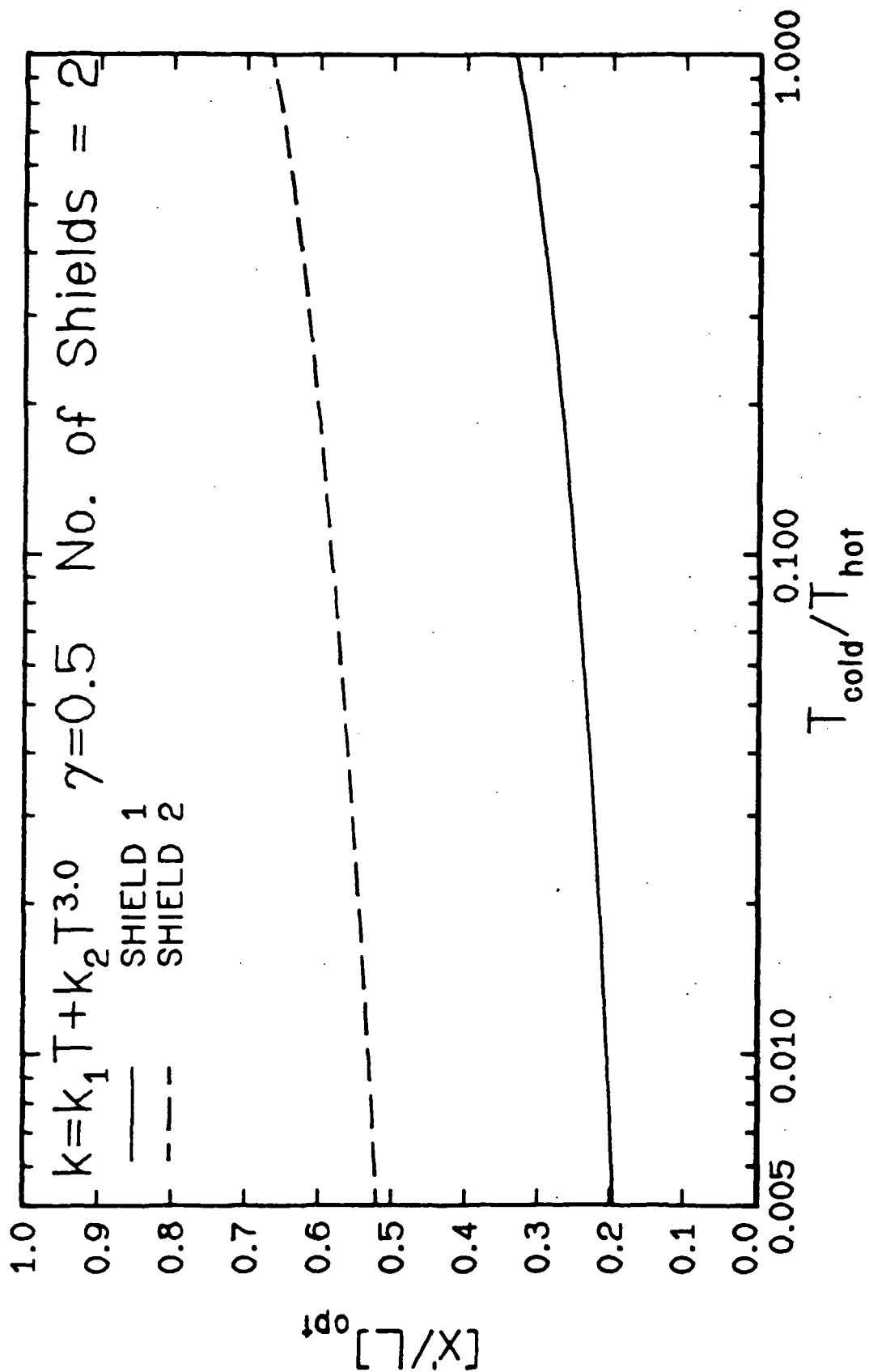


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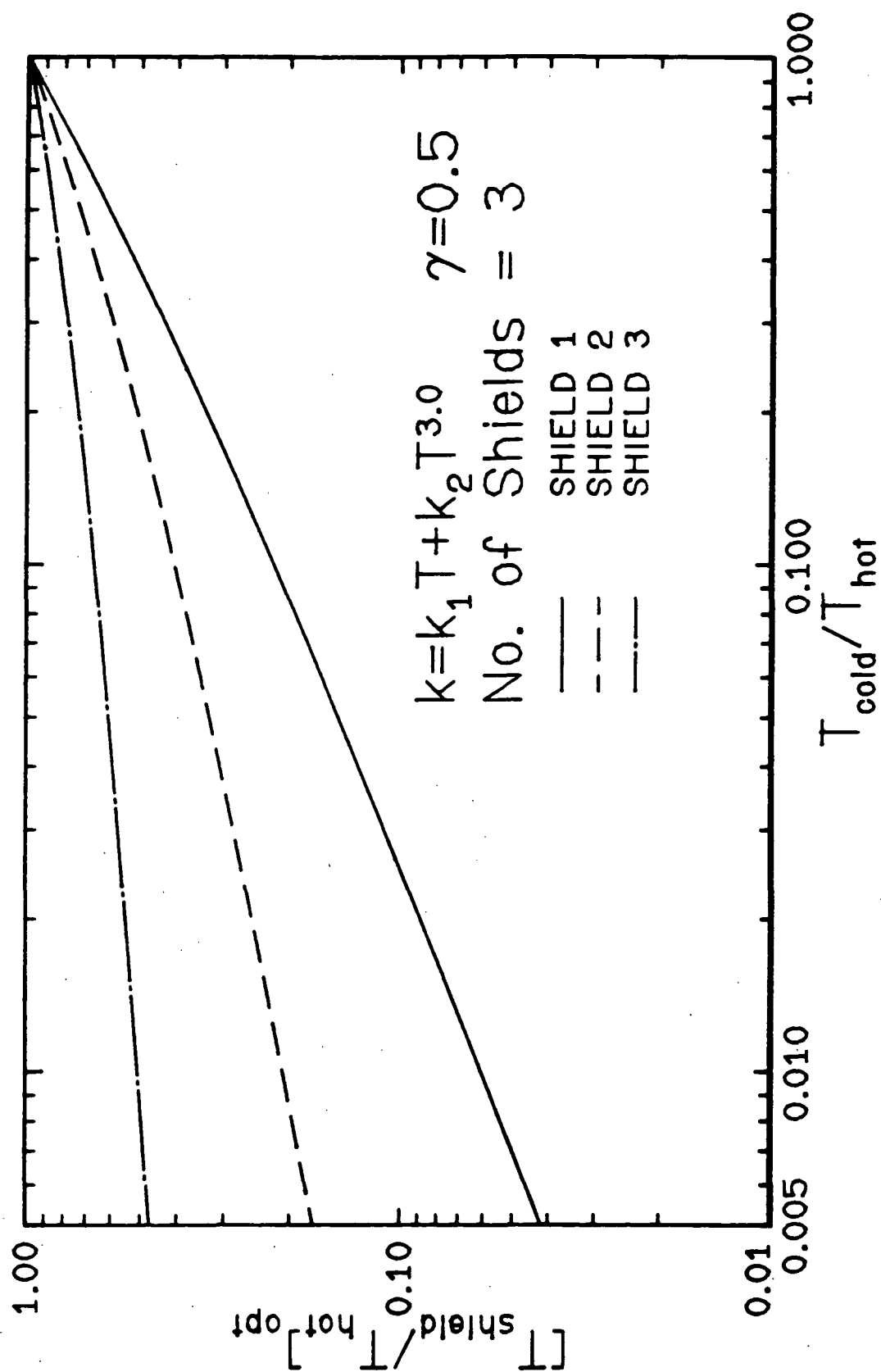


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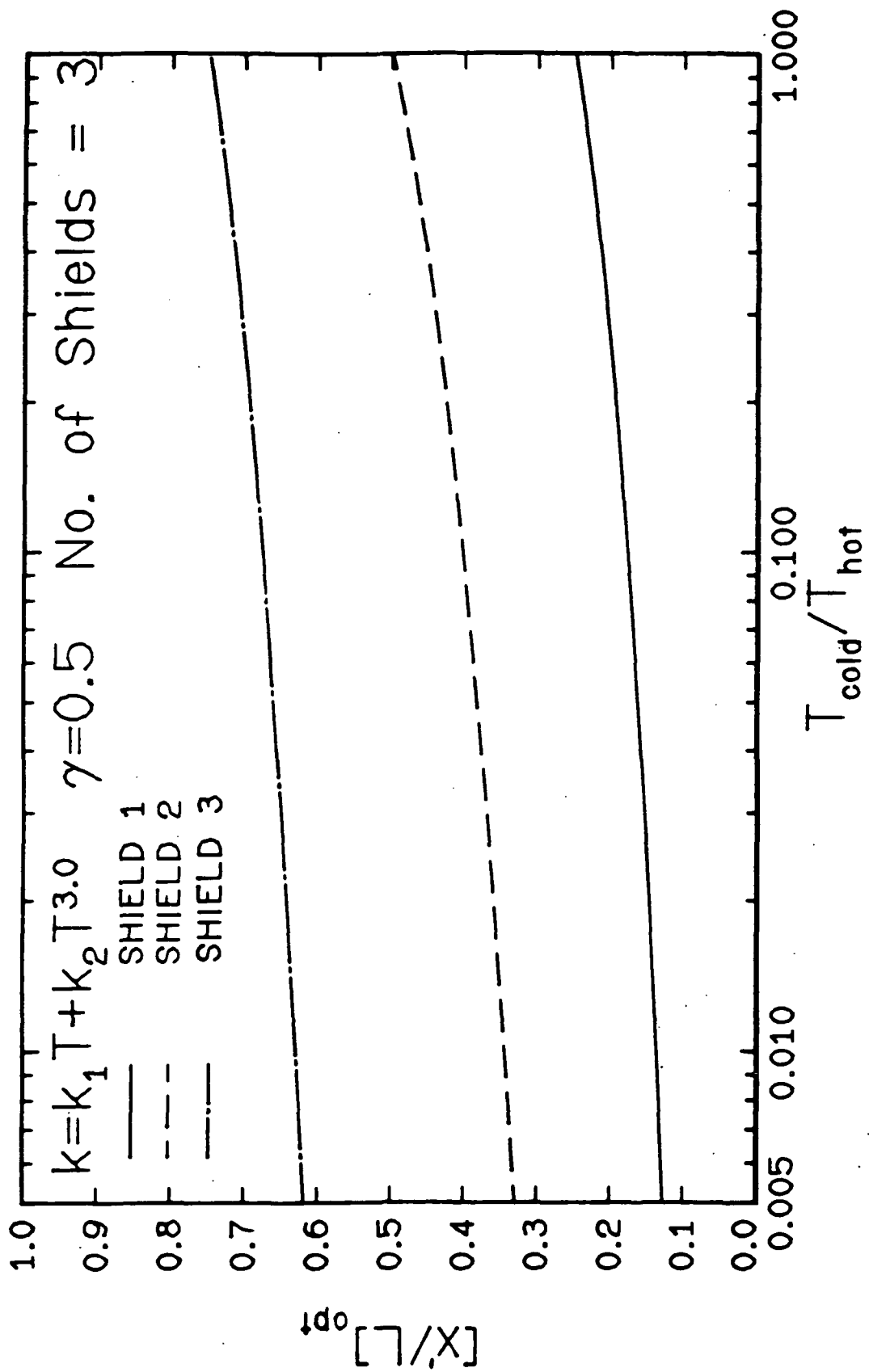


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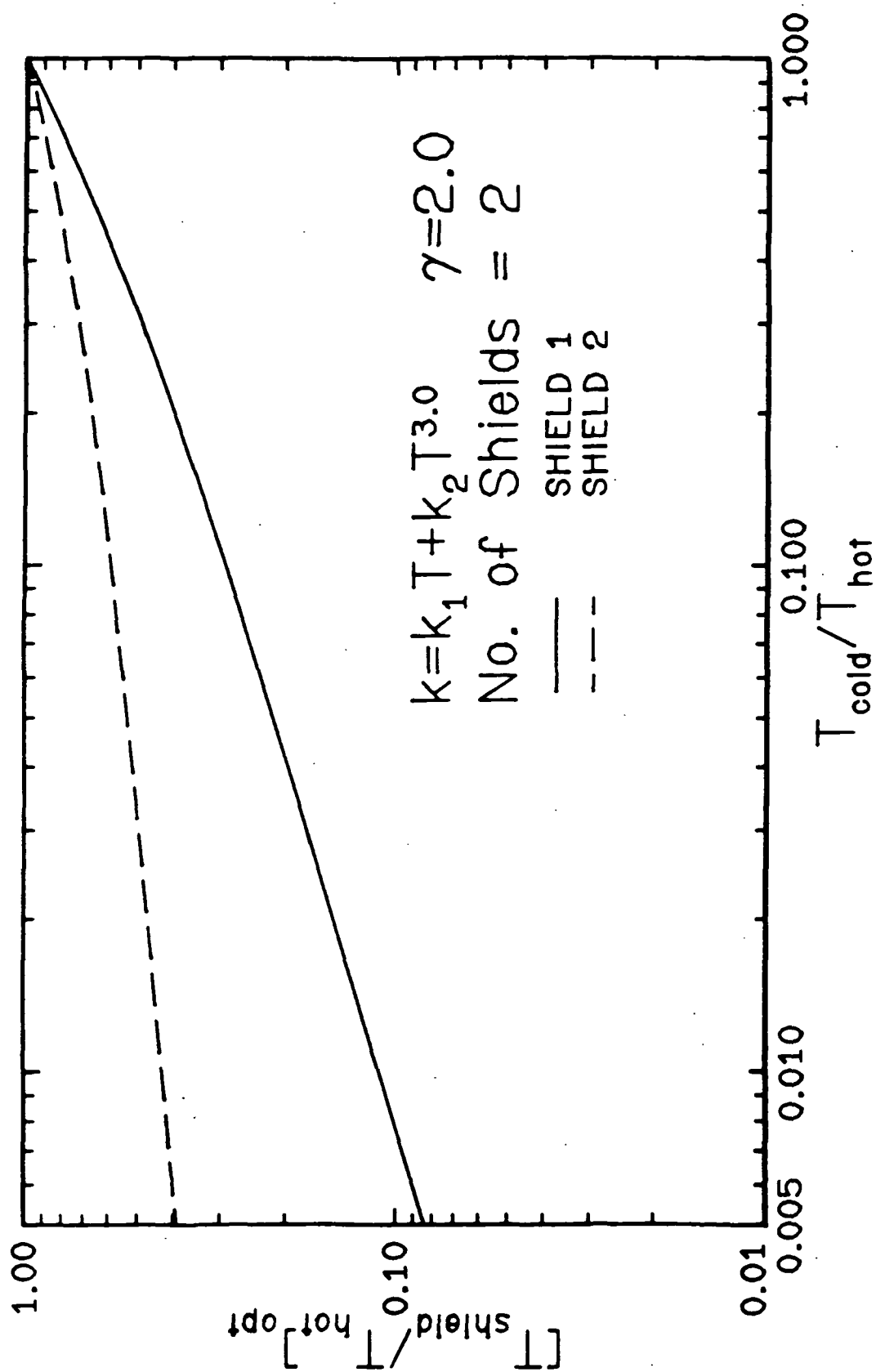


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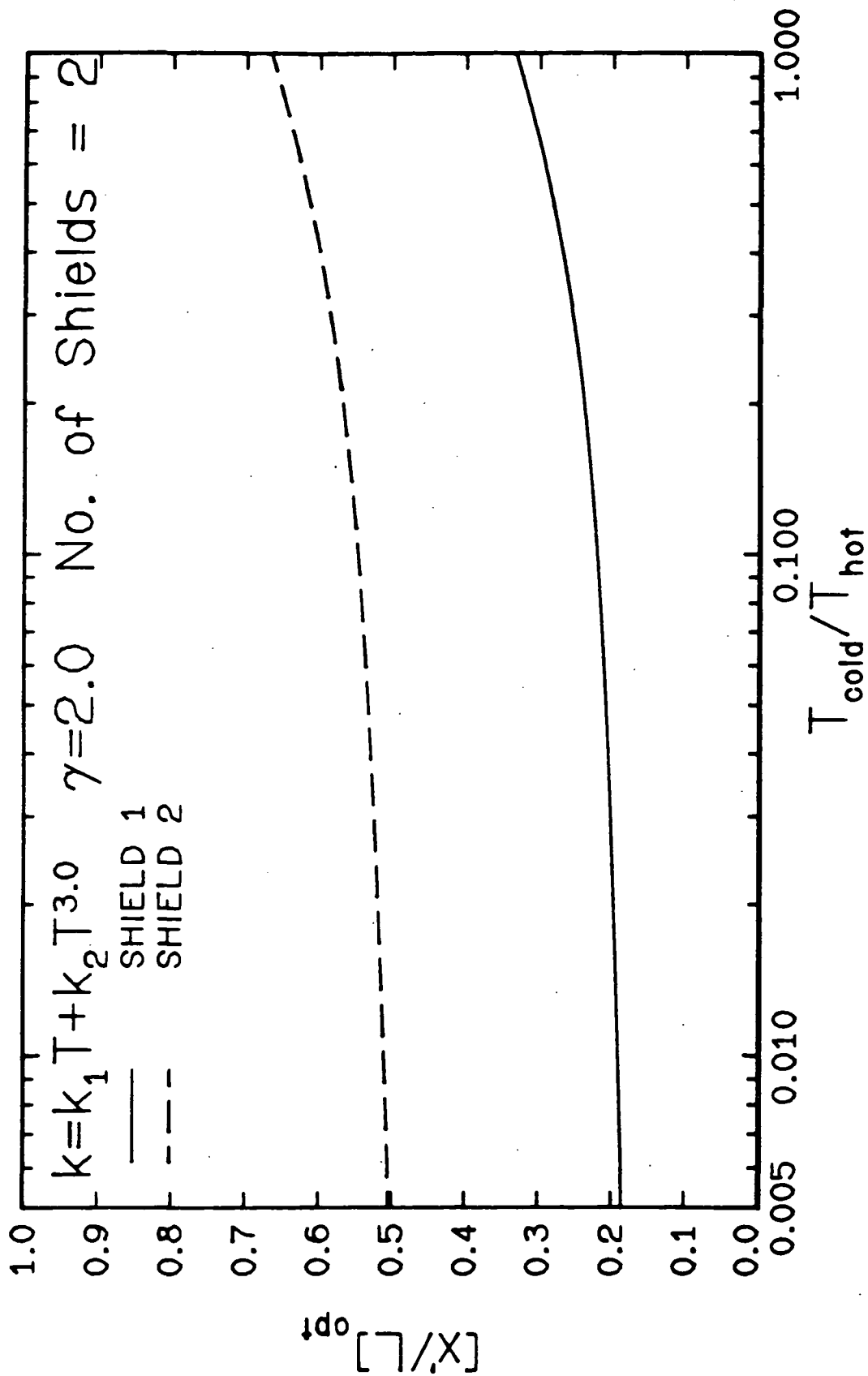


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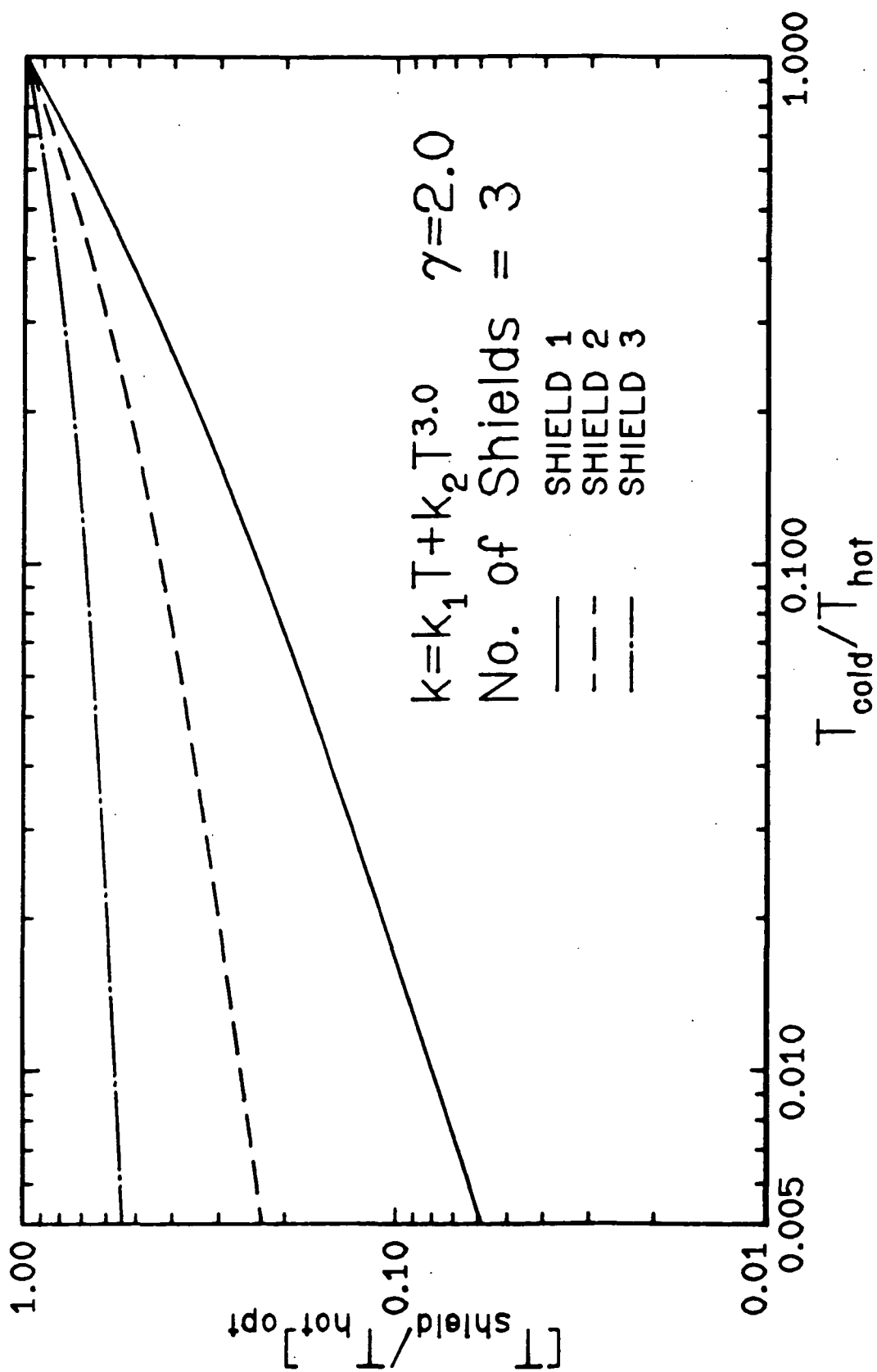


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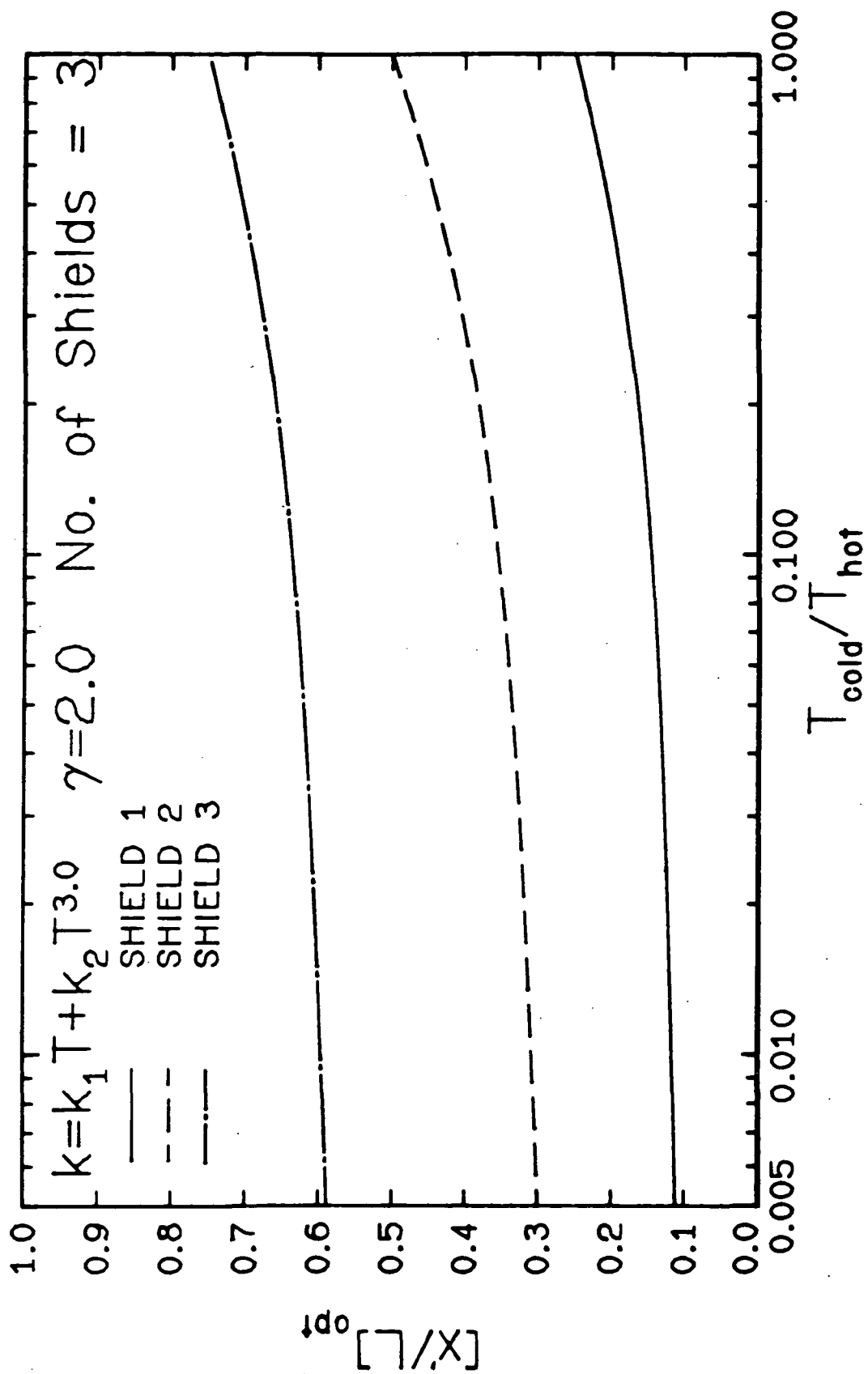


Figure 31

Curve Set 3: Figures 32 through 35

System sensitivity to deviations from the optimum shield
temperatures and locations for two overall temperature ratios
with one cooled shield

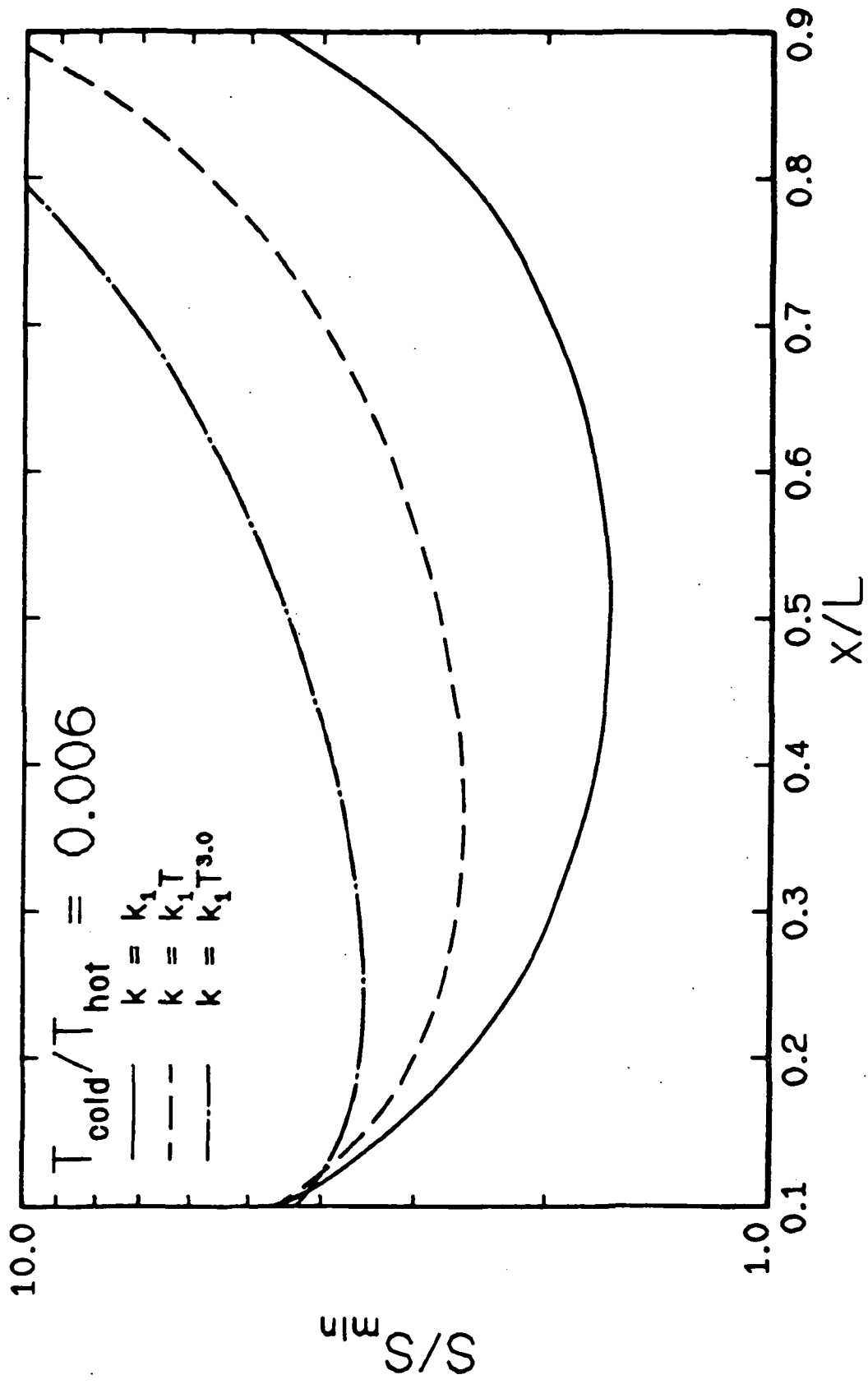


Figure 32

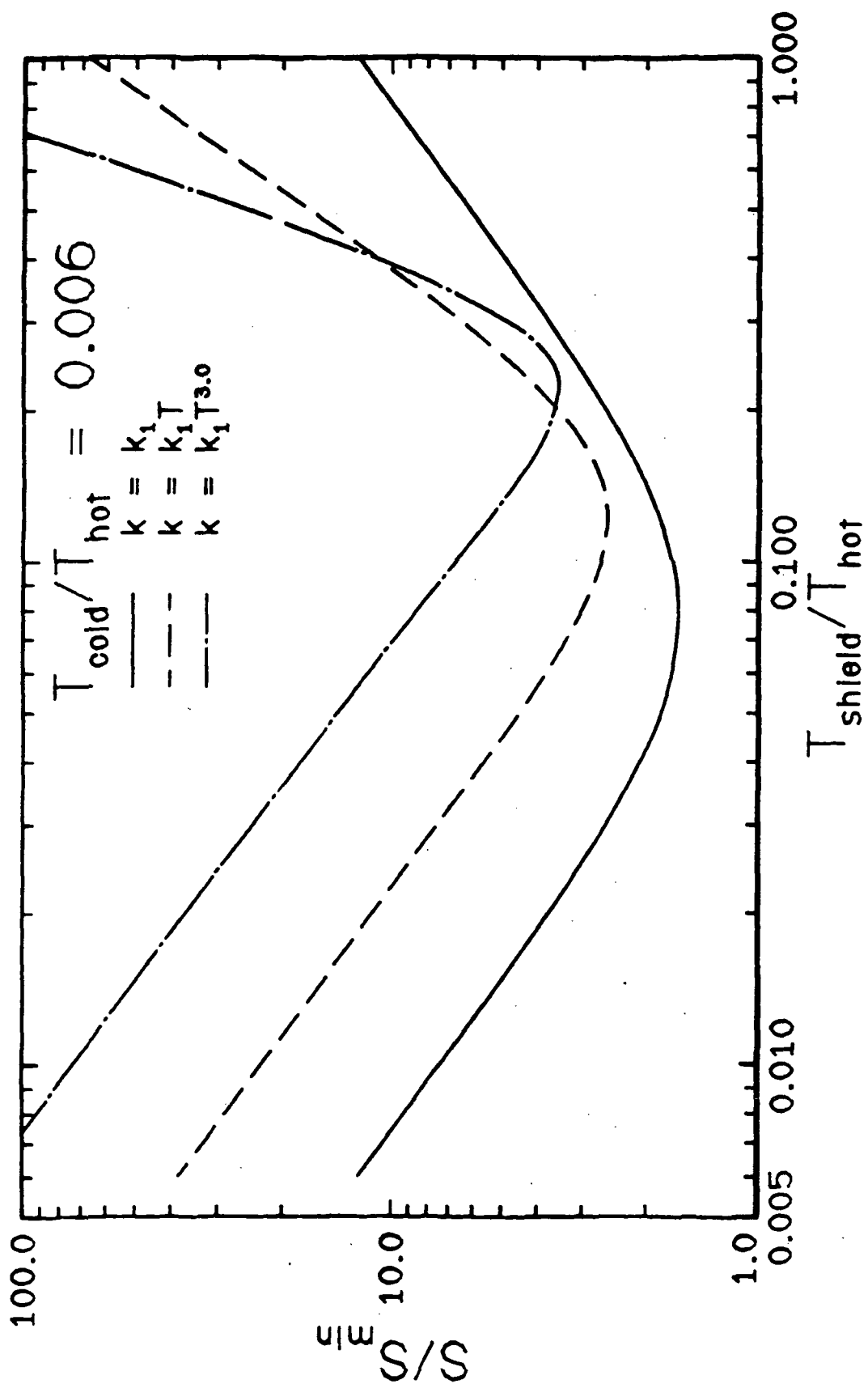


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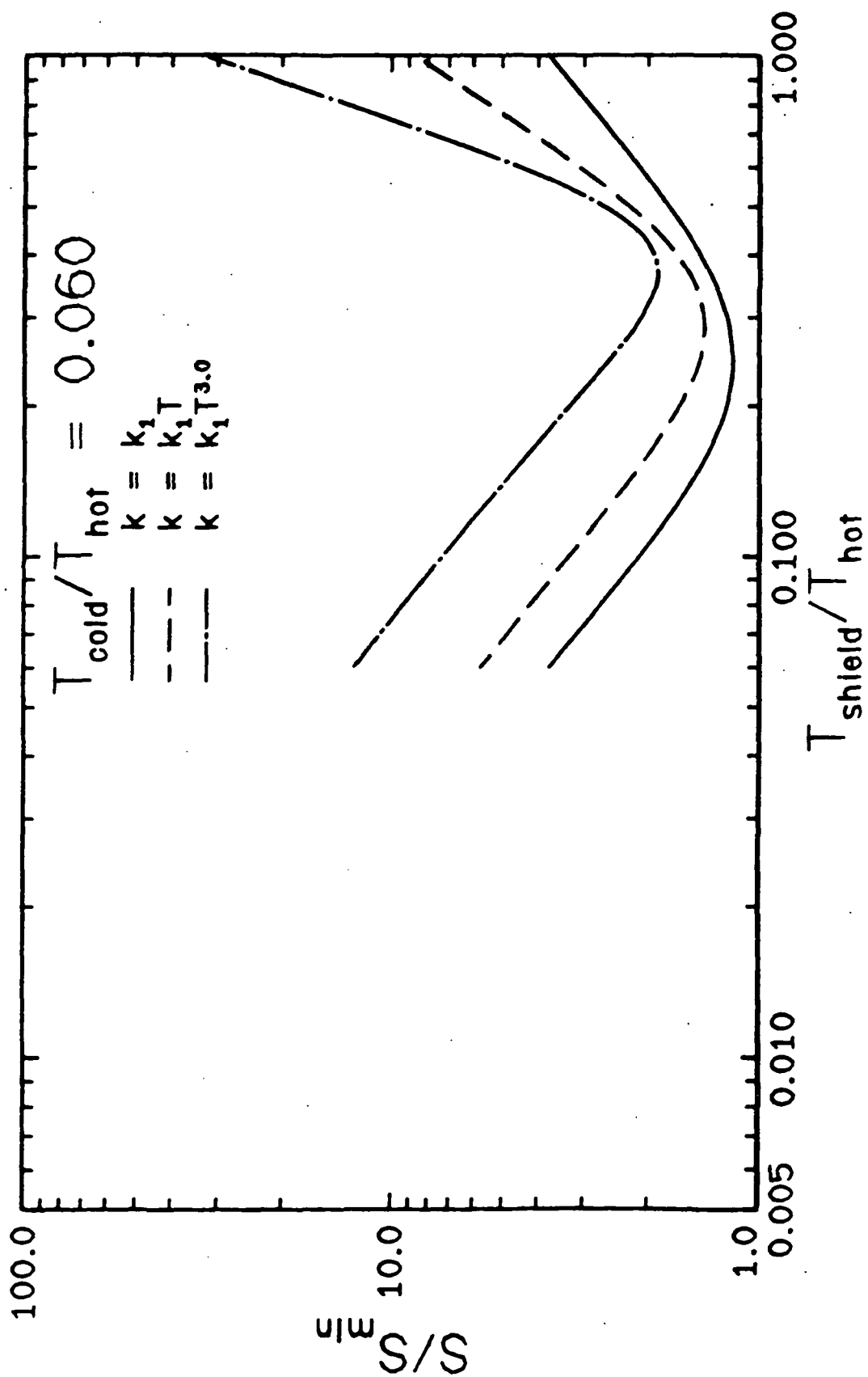


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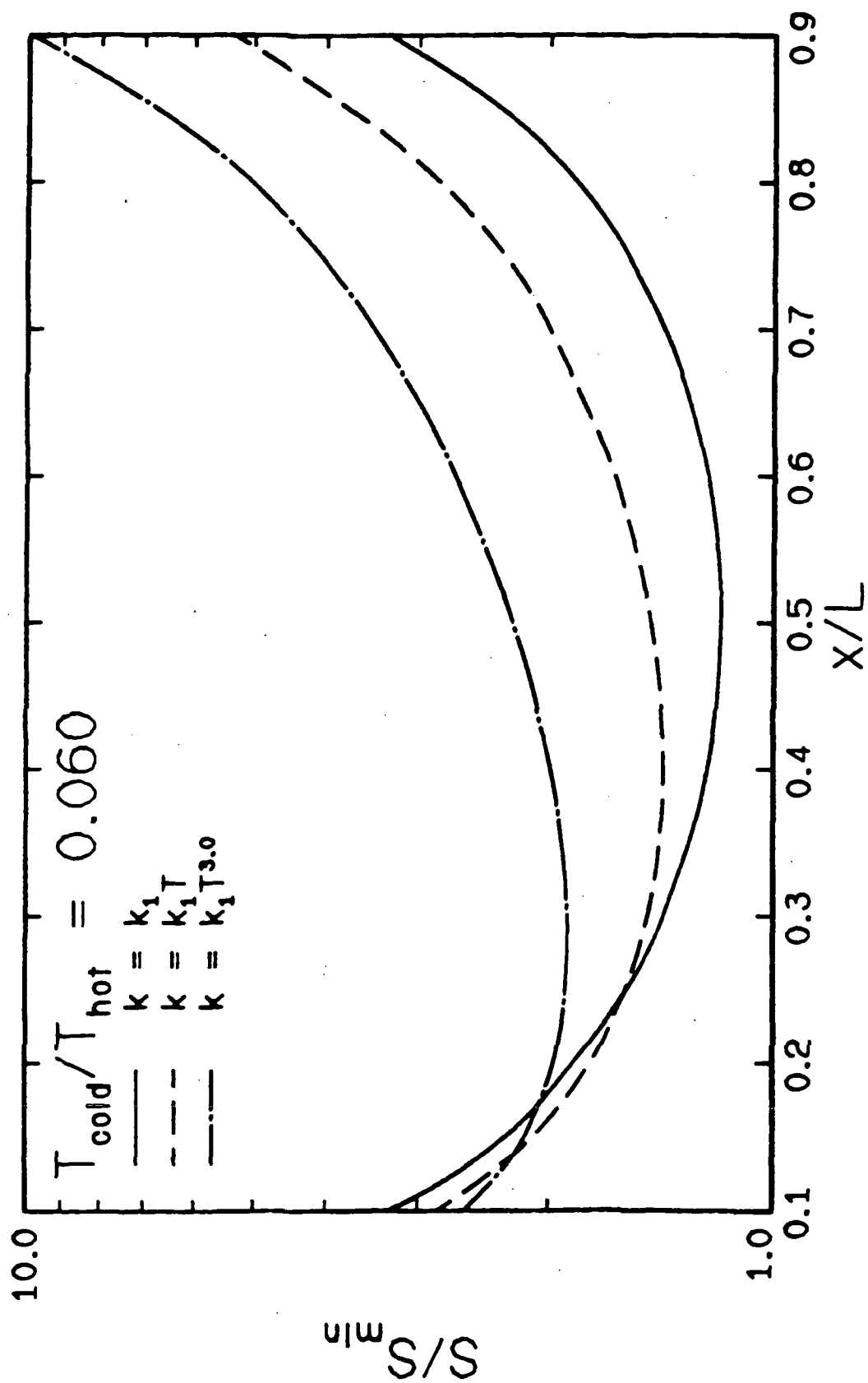


Figure 35

APPENDIX
COMPUTER PROGRAMS

SEPARS and SHIELD

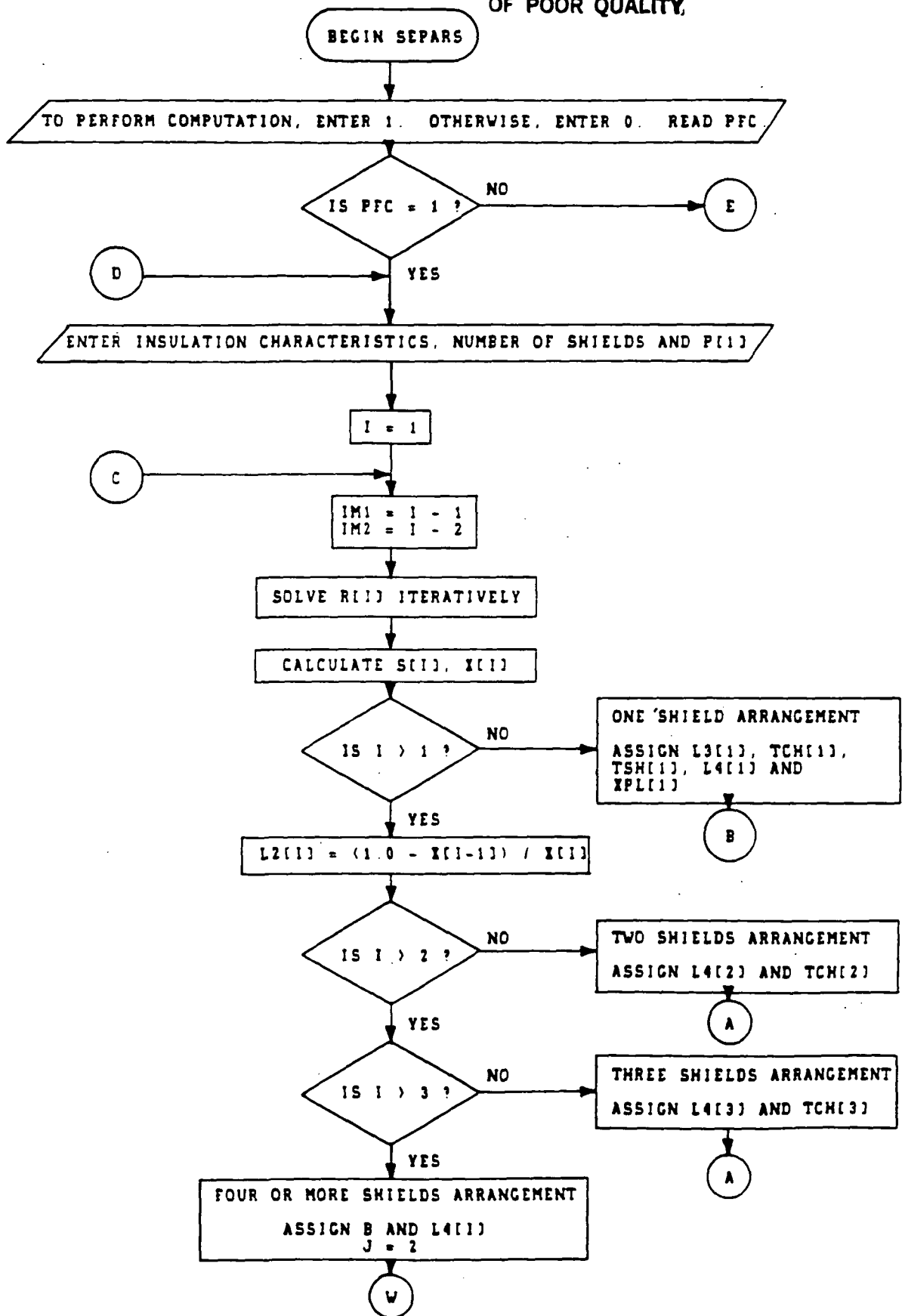
These two programs are essentially identical, but SEPARS is written in PASCAL whereas SHIELD is in BASIC.

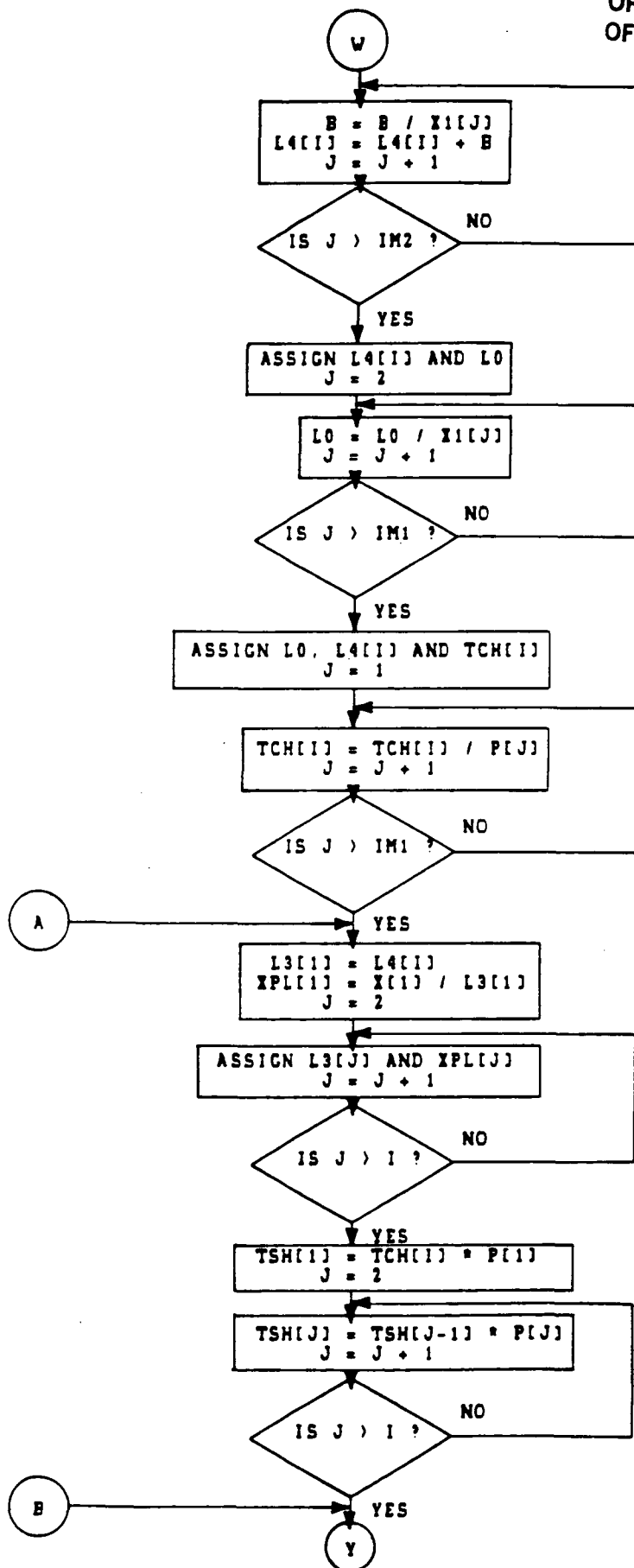
To allow for consecutive calculations of different systems, the program always recycles to the starting point. Consequently, the first input requested is either a 1, if a calculation is to be performed, or a 0, if no more work is to be done.

Next the program requests input of the insulation's characteristics, specifically, the two exponents of the temperatures in the two-term conductivity function, the maximum number of cooled shields (≤ 10) to evaluate, the value of γ , and the temperature ratio of the first shield to the cold wall, $P(1) = T_{S1}/T_C$. The program calculates and presents the characteristics of all optimal systems of cooled shields from one shield to the maximum number specified in the input.

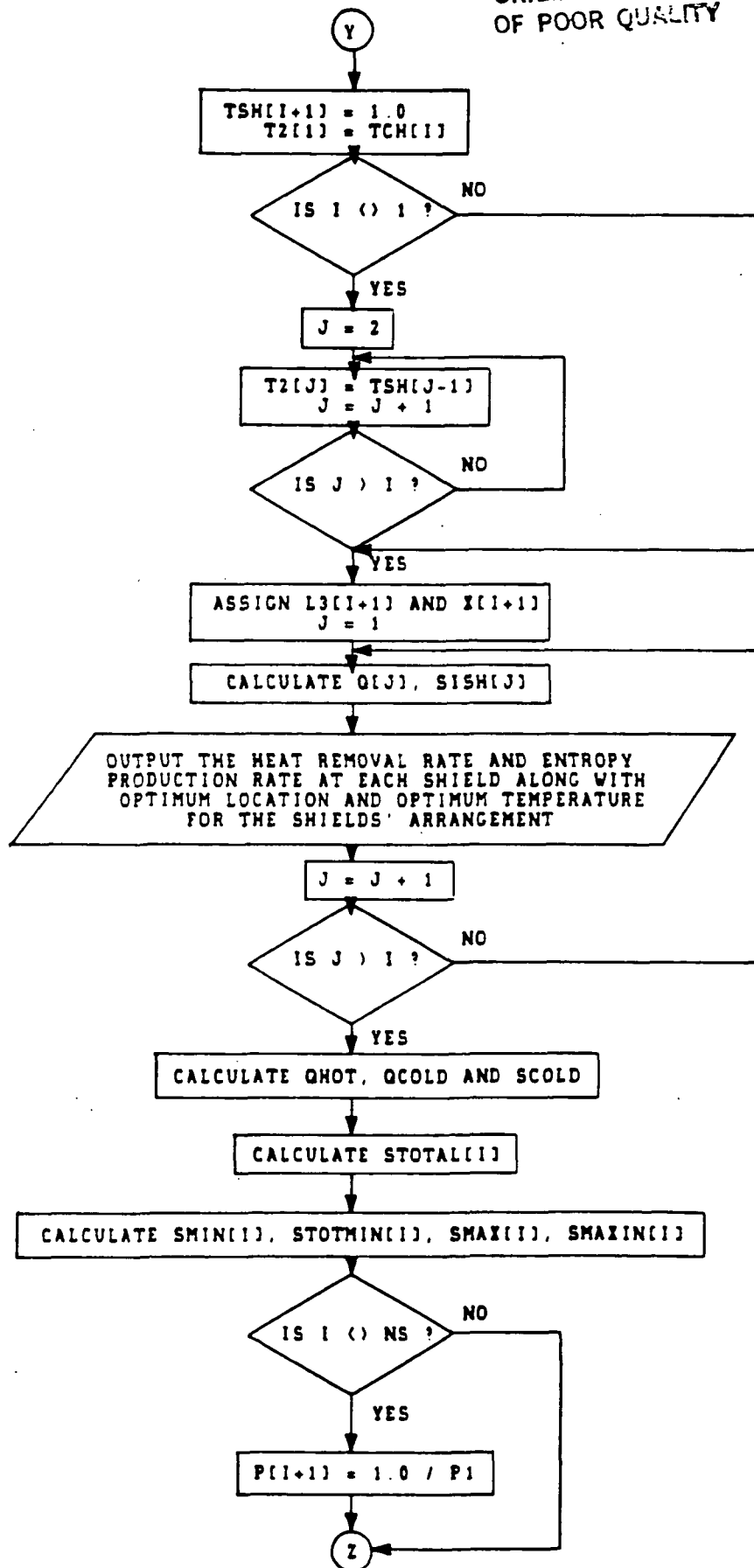
The flow chart and a program sample follows.

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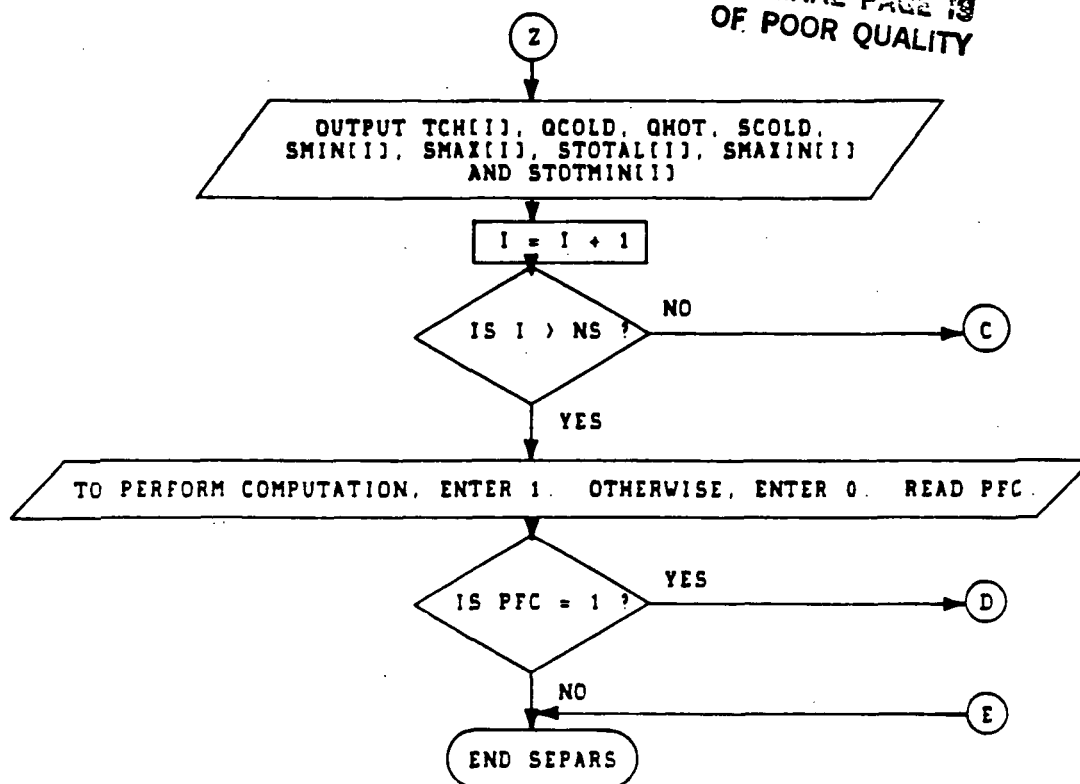


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ORIGINAL PAGE 19
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.....
.....          SEPARS      .....
.....
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UNIV OF ILLINOIS AT URBANA-CHAMPAIGN
1106 W GREEN STREET
URBANA, IL 61801
.....
JULY 1983
.....
.....
(.....)
(*)
(*) THIS PASCAL PROGRAM WAS DEVELOPED TO OPTIMIZE THE (*)
(*) LOCATION, TEMPERATURE AND HEAT DISSIPATION RATE (*)
(*) OF EACH COOLED SHIELD INSIDE AN INSULATION LAYER (*)
(*) THE THERMAL CONDUCTIVITY OF THE INSULATION HAS (*)
(*) THE GENERAL FORM. (*)
(*) (*)
(*) K = K1*(T**M) + K2*(T**N) (*)
(*) (*)
(*) THE METHOD IS BASED ON THE MINIMIZATION OF THE (*)
(*) ENTROPY PRODUCTION RATE WHICH IS PROPORTIONAL TO (*)
(*) THE HEAT LEAK ACROSS THE INSULATION (*)
(*) (*)
(.....)
(.....)
.....
LABEL      100
CAREER     200.

TYPE
ARRAYS=ARRAY: 101 OF REAL.    (*) THE SIZE OF ARRAYS DETERMINES THE MAXIMUM NUMBER OF SHIELDS *
ARRAYP=ARRAY: 111 OF REAL.    (*) THE SIZE OF ARRAYP IS EQUAL TO NS+1 *)

VAF
(.....)
(*) -- LET THICK(I) REPRESENT THE SPACING (-- *)
(*) -- BETWEEN (I-1)-TH & (I+1)-TH SHIELDS (-- *)
(.....)

12          ARRAYS.    (*) THICK(I) / THICK(I-1) *)
13          ARRAYP.    (*) BURNUP VARIABLE *)
14          ARRAYS.    (*) OVERALL INSULATION THICKNESS / THICK(I) RATIO *)
P           ARRAYS.    (*) 1-TH SHIELD / LOCAL COLD TEMPERATURE RATIO, ALWAYS > 1 *)
Q           ARRAYS.    (*) 1-TH SHIELD DIMENSIONLESS HEAT REMOVAL RATE *)
R           ARRAYS.    (*) 1-TH LOCAL COLD / LOCAL HOT TEMPERATURE RATIO, ALWAYS ( 1 *)
S           ARRAYS.    (*) DIMENSIONLESS ENTROPY PRODUCTION RATE FOR 1-TH LAYER *)
SI$H       ARRAYS.    (*) 1-TH SHIELD DIMENSIONLESS ENTROPY PRODUCTION RATE *)
SMAX       ARRAYS.    (*) MAXIMUM DIMENSIONLESS ENTROPY PRODUCTION RATE *)
SMIN       ARRAYS.    (*) MINIMUM DIMENSIONLESS ENTROPY PRODUCTION RATE *)
SMAXMIN    ARRAYS.    (*) SMAX(I) / SMIN(I) *)
STOTAL     ARRAYS.    (*) TOTAL DIMENSIONLESS ENTROPY PRODUCTION RATE *)
STOTMIN    ARRAYS.    (*) STOTAL(I) / SMIN(I) *)
TCH        ARRAYS.    (*) COLD WALL / HOT WALL TEMPERATURE RATIO, ALWAYS ( 1 *)
TSH        ARRAYS.    (*) 1-TH SHIELD / HOT WALL TEMPERATURE RATIO, ALWAYS ( 1 *)
TC         ARRAYS.    (*) BURNUP VARIABLE *)
I          ARRAYP.    (*) DISTANCE FROM LOCAL COLD SHIELD / THICK(I) RATIO *)
IPL        ARRAYS.    (*) DISTANCE FROM COLD WALL / OVERALL INSULATION THICKNESS *)
II         ARRAYS.    (*) X(I) / (1.8-X(I)) *)

```

```

75      B          : REAL,          (* DUMMY VARIABLE *)
76      CC         : REAL,          (* DUMMY VARIABLE *)
77      COUNT      : INTEGER,       (* NUMBER OF ITERATIONS NEEDED TO DETERMINE R(1) *)
78      DD         : REAL,          (* DUMMY VARIABLE *)
79      G,G1       : REAL,          (* DUMMY VARIABLES *)
80      GAMA        : REAL,          (*  $(K1*(M+1))/(K1*(M+1)) * THOT** (M-N)$ , ALWAYS = 0 *)
81                                     (* WHERE THOT IS THE HOT WALL TEMPERATURE (K) *)
82      I,IM1,IM2,J : INTEGER,       (* INDICES FOR LOOPS *)
83      JWK        : TEXT,          (* OUTPUT FILE TO BE USED IF DESIRED *)
84      L0         : REAL,          (* DUMMY VARIABLE *)
85      M          : REAL,          (* 1ST POWER IN THE THERMAL CONDUCTIVITY EQUATION *)
86      MP1        : REAL,          (* EQUALS M+1 *)
87      N          : REAL,          (* 2ND POWER IN THE THERMAL CONDUCTIVITY EQUATION *)
88      NP1        : REAL,          (* EQUALS N+1 *)
89      NS         : INTEGER,       (* NUMBER OF SHIELDS *)
90      PFC        : INTEGER,       (* PROGRAM FLOW CONTROLLER *)
91      P1         : REAL,          (* 1-TH SHIELD / LOCAL HOT TEMPERATURE RATIO, ALWAYS ( 1 *)
92      QCOLD      : REAL,          (* HEAT OUT AT COLD WALL *)
93      QHOT       : REAL,          (* HEAT IN AT HOT WALL *)
94      SCOLD      : REAL,          (* ENTROPY PRODUCTION RATE AT COLD WALL *)
95      U,V        : REAL,          (* DUMMY VARIABLES *)
96      W1,W2,W3   : REAL,          (* DUMMY VARIABLES *)
97      Z1,Z2      : REAL,          (* DUMMY VARIABLES *)
98
99
100
101
102  PROCEDURE INPUT.
103  BEGIN
104      WRITELN
105      WRITELN( 'ENTER ----) M N NS GAMA P1: (----)',
106      WRITELN( ' ),
107      WRITELN( 'WHERE M ---- 1ST POWER IN THE THERMAL CONDUCTIVITY EQUATION',
108      WRITELN( 'N ---- 2ND POWER IN THE THERMAL CONDUCTIVITY EQUATION',
109      WRITELN( 'NS ---- NUMBER OF SHIELDS',
110      WRITELN( 'GAMA -- =0 IF USING ONE TERM THERMAL CONDUCTIVITY EQUATION',
111      WRITELN( '          >0 IF USING TWO TERM THERMAL CONDUCTIVITY EQUATION',
112      WRITELN( 'P1: -- 1ST SHIELD / COLD WALL TEMPERATURE RATIO, ALWAYS > 1',
113      WRITELN( ' )
114  END
115
116
117
118  PROCEDURE PFC.
119  BEGIN
120      WRITELN
121      WRITELN( 'TO PERFORM COMPUTATION, ENTER 1. OTHERWISE, ENTER 0.',
122      WRITELN
123  END
124
125
126
127  PROCEDURE SINGLESPEAC.
128  BEGIN
129      WRITELN( ' )
130  END
131
132
133
134  FUNCTION PWR(X:REAL) REAL.
135  VAR
136      A          : REAL.
137  BEGIN
138      A = E*LN(X),
139      PWR = EXP(A)
140  END
141
142
143
144  FUNCTION D(E,X:REAL) REAL.
145  BEGIN
146      D = (E-1.0)*PWR(X,E)-E/(PWR(X,(1.0-E)))-(1.0/SQR(X))
147  END
148
149
150

```

```

151 FUNCTION F(E,XX:REAL):REAL,
152 BEGIN
153   (* FUNCTIONAL F *)
154   F:=(PWR(XX,(E+1.0))-PWR(XX,E)-1.0*(1.0/XX))
155 END,
156   (* FUNCTIONAL F *)
157
158 FUNCTION SIMPSON(TCHR:REAL):REAL,
159 TYPE
160   ARR=ARRAY[1: 101] OF REAL,
161
162 VAR
163   C,V      ARR,
164   DELTAT   REAL,
165   M        REAL,
166   K,L      INTEGER,
167
168 BEGIN
169   (* COMPUTE MINIMUM ENTROPY PRODUCTION RATE USING SIMPSON'S NUMERICAL INTEGRATION SCHEME *)
170   DELTAT:=(1.0-TCHR)/100.0,
171   FOR L:=1 TO 101 DO
172     BEGIN
173       C(L):=TCHR+DELTAT*(L-1);
174       V(L):=PWR((PWR(C(L),M)+CAMA*MP1/MP1)*PWR(C(L),M),0.5)/C(L)
175     END,
176   M:=V(1)+V(101),
177   FOR K:=2 TO 100 DO
178     BEGIN
179       IF K=((K DIV 2)*2) THEN
180         M:=M+4.0*V(K)
181       ELSE
182         M:=M+2.0*V(K)
183     END,
184   SIMPSON:=(SOR(DELTAT/3.0*M))/(1.0-CAMA*MP1/MP1)
185 END,
186   (* COMPUTE MINIMUM ENTROPY PRODUCTION RATE USING SIMPSON'S NUMERICAL INTEGRATION SCHEME *)
187
188
189
190
191
192   (* MAIN PROGRAM BODY *)
193
194 BEGIN
195   PFC:=1.0;
196   READLN;
197   READ(PFC);
198   WHILE PFC=1.0 DO
199     BEGIN
200
201       (* THIS BLOCK IS USED TO INPUT THE INSULATION THERMAL CONDUCTIVITY, NUMBER *)
202       (* OF SHIELDS AND 1ST. SHIELD / COLD WALL TEMPERATURE RATIO *)
203
204       INPUT M;
205       READLN;
206       READ(M,N,MS,CAMA,P11);
207       SINGLESPEACE;
208       IF CAMA=0.0 THEN
209         WRITELN(' THERMAL CONDUCTIVITY OF THE INSULATION IS K = K1*T**',M,3,1)
210       ELSE
211         BEGIN
212           WRITELN(' THERMAL CONDUCTIVITY OF THE INSULATION IS K = K1*T**',M,3,1, ' + K2*T**',M,3,1, ' ,',
213             WRITELN(' (K2*(M+1))/(K1*(M+1))*THOT**'(M-M) = ',CAMA,9,2)
214         END,
215       SINGLESPEACE,
216       SINGLESPEACE,
217
218       MP1:=M+1.0,
219       MP2:=N+1.0,
220       FOR I:=1 TO MS DO
221         BEGIN
222           IM1:=I-1,
223           IM2:=I-2,
224           R(I):=0.000001,
225           CC:=0.1,
226           DD:=1.0,
227           COUNT:=0,
228
229

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230      (* THIS BLOCK CALCULATES R(I) ITERATIVELY *)
231
232  REPEAT
233    P1 = P(I)*R(I),
234    W1 = PWR(R(I),M)*F(M,P(I))*CAMA*PWR(R(I),M)*F(M,P(I)),
235    W2 = SQRT(PWR(R(I),(M-1.0))*D(M,P(I))*CAMA*PWR(R(I),(M-1.0))*D(M,P(I))),
236    W3 = -SQRT(D(M,P1)*CAMA*D(M,P1))/(F(M,P1)*CAMA*F(M,P1)),
237    C = (W2/W1)*W3,
238    G1 = C*DD,
239    IF G1<0.0 THEN GOTO 100,
240    IF G1=0.0 THEN GOTO 200,
241    CC = (-0.1)*CC,
242    IF ABS(CC)<0.000001 THEN GOTO 200,
243    DD = -DD,
244    100 R(I) = R(I)+CC,
245    IF (R(I)<0.999999) OR (R(I)<0.000001) THEN
246      BEGIN
247        R(I) = R(I)-0.9*CC,
248        CC = 0.1*CC
249      END,
250    200 COUNT = COUNT+1,
251  UNTIL (G1=0.0) OR (ABS(CC)<0.000001),
252
253
254  U = -(PWR(R(I),(M-1.0))*D(M,P(I))*CAMA*PWR(R(I),(M-1.0))*D(M,P(I))),
255  X(I) = U/(D(M,P1)*CAMA*D(M,P1)),
256  X(I) = X(I)/(1.0-X(I)),
257  V = (F(M,P1)*CAMA*F(M,P1))/(1.0-X(I)),
258  S(I) = V*(PWR(R(I),M)*F(M,P(I))*CAMA*PWR(R(I),M)*F(M,P(I)))/X(I),
259  S(I) = S(I)/(1.0+CAMA*NP1/MP1)/MP1,
260
261      (* IN THIS BLOCK VARIABLES ARE ASSIGNED FOR DIFFERENT SHIELD CONFIGURATIONS *)
262
263  IF 101 THEN
264    BEGIN
265      L3(I) = (1.0-X(I))/X(I),
266      IF 102 THEN
267        IF 103 THEN
268          BEGIN
269            B = 1.0,
270            L4(I) = 0.0,
271            FOR J = 2 TO IM2 DO
272              BEGIN
273                B = B/X(I),
274                L4(J) = L4(I)+B
275              END,
276            L4(I) = L4(I)*(1.0-X(I))+1.0,
277            L0 = 1.0-X(I),
278            FOR J = 2 TO IM1 DO L0 = L0/X(I),
279            L0 = L0/X(I),
280            L4(I) = L4(I)+L0,
281            TCH(I) = R(I),
282            FOR J = 1 TO IM1 DO TCH(J) = TCH(I)/P(J),
283          END
284        ELSE
285          BEGIN
286            L4(I) = 1.0+(1.0-X(I))*(1.0-X(I))/(X(I)*X(I)),
287            TCH(I) = R(I)/(P(I)*P(I))
288          END
289        ELSE
290          BEGIN
291            L4(I) = X(I)+(1.0-X(I))/X(I),
292            TCH(I) = R(I)/P(I)
293          END,
294          L3(I) = L4(I),
295          XPL(I) = X(I)/L3(I),
296          FOR J = 2 TO I DO
297            BEGIN
298              L3(J) = L3(J-1)/L3(J),
299              XPL(J) = XPL(J-1)*X(J)/L3(J)
300            END,
301          TSH(I) = TCH(I)*P(I),
302          FOR J = 2 TO I DO TSH(J) = TSH(J-1)*P(J)
303        END
304      ELSE

```

```

305 BEGIN
306 L3(1) = 1.0.
307 TCH(1) = R(1).
308 TSH(1) = TCH(1)*P(1).
309 L4(1) = 1.0.
310 XPL(1) = X(1)
311 END.
312 TSH(I+1) = 1.0.
313 T2(I) = TCH(I).
314
315
316 SINGLESPEACE.
317 WRITELN(' NUMBER OF SHIELDS = ',I-2).
318 WRITELN(' NUMBER OF ITERATIONS = ',COUNT 1).
319 SINGLESPEACE.
320 SINGLESPEACE.
321 WRITELN('
322 HEAT REMOVAL ENTROPY PRODUCTION OPTIMUM OPTIMUM')
323 RATE RATE LOCATION TEMPERATURE')
324 WRITELN('
325 -----
326 SINGLESPEACE.
327 IF I(1) THEN
328 FOR J = 2 TO I DO T2(J) = TSH(J-1).
329 L3(I+1) = L3(I).
330 X(I+1) = 1.0-X(I).
331
332 (* IN THIS BLOCK DIMENSIONLESS HEAT REMOVAL AND ENTROPY PRODUCTION RATES *)
333 (* ARE CALCULATED FOR EACH SHIELD *)
334
335 FOR J = 1 TO I DO
336 BEGIN
337 Z1 = ((PWR(TSH(J-1),MP1)-PWR(TSH(J),MP1))*L3(J+1)/X(J+1)-(PWR(TSH(J),MP1)-PWR(T2(J),MP1))*L3(J)/X(J))/MP1.
338 Z2 = ((PWR(TSH(J-1),MP1)-PWR(TSH(J),MP1))*L3(J+1)/X(J+1)-(PWR(TSH(J),MP1)-PWR(T2(J),MP1))*L3(J)/X(J))/MP1.
339 Q(J) = (Z1+CAMA*Z2)/(1.0+CAMA*NP1/MP1).
340 SISH(J) = Q(J)/TSH(J).
341 WRITELN(' SHIELD ',J,2,' ',S,Q(J) 9.5,' ',11,SISH(J) 9.5,' ',9,XPL(J) 9.5,' ',5,TSH(J) 9.5).
342 END.
343
344 (* FINALLY, OTHER QUANTITIES OF INTEREST ARE CALCULATED IN THIS BLOCK *)
345
346 SINGLESPEACE.
347 QHOT = ((1.0-PWR(TSH(I),MP1)+CAMA-CAMA*PWR(TSH(I),MP1))*L3(I)/(X(I+1)*MP1))/(1.0+CAMA*NP1/MP1).
348 QCOLD = (PWR(TSH(I),MP1)-PWR(TCH(I),MP1)+CAMA*PWR(TSH(I),MP1)-CAMA*PWR(TCH(I),MP1))*L3(I)/(X(I)*MP1).
349 QCOLD = QCOLD/(1.0+CAMA*NP1/MP1).
350 SCOLD = QCOLD/TCH(I).
351 STOTAL(I) = SCOLD-QHOT.
352 FOR J = 1 TO I DO STOTAL(I) = STOTAL(I)+SISH(J).
353 SHMIN(I) = SIMPSON(TCH(I)).
354 STOTMIN(I) = STOTAL(I)/SHMIN(I).
355 SHMAX(I) = ((1.0-PWR(TCH(I),MP1)+CAMA-CAMA*PWR(TCH(I),MP1))*(1.0/TCH(I)-1.0)/MP1)/(1.0+CAMA*NP1/MP1).
356 SHMAX(I) = SHMAX(I)/SHMIN(I).
357
358 IF I(1) THEN P(1+1) = 1.0/P(1).
359 SINGLESPEACE.
360 WRITELN(' COLD WALL / HOT WALL TEMPERATURE RATIO = ',TCH(I) 14.6).
361 WRITELN(' HEAT OUT AT COLD WALL = ',QCOLD 14.6).
362 WRITELN(' HEAT IN AT HOT WALL = ',QHOT 14.6).
363 WRITELN(' ENTROPY PRODUCTION RATE AT COLD WALL = ',SCOLD 14.6).
364 WRITELN(' ENTROPY PRODUCTION RATE AT HOT WALL = ',-QHOT 14.6).
365 WRITELN(' MINIMUM ENTROPY PRODUCTION RATE = ',SHMIN(I) 14.6).
366 WRITELN(' MAXIMUM ENTROPY PRODUCTION RATE = ',SHMAX(I) 14.6).
367 WRITELN(' TOTAL ENTROPY PROD RATE WITH ',I-2,' SHIELDS = ',STOTAL(I) 14.6).
368 WRITELN(' MAXIMUM / MINIMUM ENTROPY PRODUCTION RATIO = ',SHMAX(I) 14.6).
369 WRITELN(' TOTAL / MINIMUM ENTROPY PRODUCTION RATIO = ',STOTMIN(I) 14.6).
370 SINGLESPEACE.
371 SINGLESPEACE.
372 SINGLESPEACE.
373 END.
374 PFCN.
375 READLN.
376 READ(PFC)
377 END
378 END
379 /EOP

```

TO PERFORM COMPUTATION, ENTER 1. OTHERWISE, ENTER 0.

? 1

ENTER ----- M N NS GAMA PC1J -----

WHERE: M ----- 1ST. POWER IN THE THERMAL CONDUCTIVITY EQUATION
N ----- 2ND. POWER IN THE THERMAL CONDUCTIVITY EQUATION
NS ----- NUMBER OF SHIELDS
GAMA -- =0 IF USING ONE TERM THERMAL CONDUCTIVITY EQUATION
 >0 IF USING TWO TERM THERMAL CONDUCTIVITY EQUATION
PC1J -- 1ST. SHIELD / COLD WALL TEMPERATURE RATIO, ALWAYS > 1

? 1

1.0 3.0 1 2.5 15.0

THERMAL CONDUCTIVITY OF THE INSULATION IS $K = K1 \cdot T^{1.0} + K2 \cdot T^{3.0}$
 $[K2 \cdot (M+1)] / [K1 \cdot (N+1)] \cdot THOT^{(N-M)} = 2.50$

NUMBER OF SHIELDS = 1
NUMBER OF ITERATIONS = 35

	HEAT REMOVAL RATE -----	ENTROPY PRODUCTION RATE -----	OPTIMUM LOCATION -----	OPTIMUM TEMPERATURE -----
SHIELD 1	0.43837	1.85659	0.36744	0.23611

COLD WALL / HOT WALL TEMPERATURE RATIO	=	0.015741
HEAT OUT AT COLD WALL	=	0.014350
HEAT IN AT HOT WALL	=	0.452719
ENTROPY PRODUCTION RATE AT COLD WALL	=	0.911631
ENTROPY PRODUCTION RATE AT HOT WALL	=	-0.452719
MINIMUM ENTROPY PRODUCTION RATE	=	1.000503
MAXIMUM ENTROPY PRODUCTION RATE	=	18.236148
TOTAL ENTROPY PROD. RATE WITH 1 SHIELDS	=	2.315503
MAXIMUM / MINIMUM ENTROPY PRODUCTION RATIO	=	18.226982
TOTAL / MINIMUM ENTROPY PRODUCTION RATIO	=	2.314340

TO PERFORM COMPUTATION, ENTER 1. OTHERWISE, ENTER 0.

? 1

ENTER ----- M N NS GAMA PC1J -----

WHERE: M ----- 1ST. POWER IN THE THERMAL CONDUCTIVITY EQUATION
N ----- 2ND. POWER IN THE THERMAL CONDUCTIVITY EQUATION
NS ----- NUMBER OF SHIELDS
GAMA -- =0 IF USING ONE TERM THERMAL CONDUCTIVITY EQUATION
 >0 IF USING TWO TERM THERMAL CONDUCTIVITY EQUATION
PC1J -- 1ST. SHIELD / COLD WALL TEMPERATURE RATIO, ALWAYS > 1

? 1

1.0 0.90 2 0.0 25.0

THERMAL CONDUCTIVITY OF THE INSULATION IS $K = K1 \cdot T^{1.0}$

NUMBER OF SHIELDS = 1
NUMBER OF ITERATIONS = 23

	HEAT REMOVAL RATE	ENTROPY PRODUCTION RATE	OPTIMUM LOCATION	OPTIMUM TEMPERATURE
SHIELD 1	0.75466	7.03151	0.35870	0.10732
COLD WALL / HOT WALL TEMPERATURE RATIO	=		0.004293	
HEAT OUT AT COLD WALL	=		0.016030	
HEAT IN AT HOT WALL	=		0.770687	
ENTROPY PRODUCTION RATE AT COLD WALL	=		3.734070	
ENTROPY PRODUCTION RATE AT HOT WALL	=		-0.770687	
MINIMUM ENTROPY PRODUCTION RATE	=		3.504633	
MAXIMUM ENTROPY PRODUCTION RATE	=		115.966533	
TOTAL ENTROPY PROD. RATE WITH 1 SHIELDS	=		9.994893	
MAXIMUM / MINIMUM ENTROPY PRODUCTION RATIO	=		33.089491	
TOTAL / MINIMUM ENTROPY PRODUCTION RATIO	=		2.851908	

NUMBER OF SHIELDS = 2
NUMBER OF ITERATIONS = 36

	HEAT REMOVAL RATE	ENTROPY PRODUCTION RATE	OPTIMUM LOCATION	OPTIMUM TEMPERATURE
SHIELD 1	0.05470	2.71297	0.17465	0.02016
SHIELD 2	0.88421	4.70678	0.48690	0.18786
COLD WALL / HOT WALL TEMPERATURE RATIO	=		0.000806	
HEAT OUT AT COLD WALL	=		0.001162	
HEAT IN AT HOT WALL	=		0.940073	
ENTROPY PRODUCTION RATE AT COLD WALL	=		1.440716	
ENTROPY PRODUCTION RATE AT HOT WALL	=		-0.940073	
MINIMUM ENTROPY PRODUCTION RATE	=		3.921467	
MAXIMUM ENTROPY PRODUCTION RATE	=		619.477774	
TOTAL ENTROPY PROD. RATE WITH 2 SHIELDS	=		7.920388	
MAXIMUM / MINIMUM ENTROPY PRODUCTION RATIO	=		157.970919	
TOTAL / MINIMUM ENTROPY PRODUCTION RATIO	=		2.019751	

TO PERFORM COMPUTATION, ENTER 1. OTHERWISE, ENTER 0.

? 0

0.175 CP SECS, 12415B CM USED.

PROGRAM SHIELD

```

1 00010 REM THIS IS A "BASIC" PROGRAM TO CALCULATE OPTIMUM TEMPERATURES,
2 00020 REM LOCATIONS, AND COOLING LOADS FOR COOLED SHIELDS IN A CRYOGENIC
3 00030 REM INSULATION SYSTEM WHOSE THERMAL CONDUCTIVITY FOLLOWS THE RELATION
4 00040 REM  $K=C_1 \cdot T^{M_0} + C_2 \cdot T^{N_0}$ 
5 00045 REM MODIFIED IN LATE NOV. 1982.
6 00050 REM
7 00060 REM DEFINITION OF SYMBOLS USED:
8 00070 REM
9 00080 REM COLD-SIDE WALL TEMPERATURE T0
10 00090 REM WARM-SIDE WALL TEMPERATURE T1
11 00100 REM SPACING BETWEEN SHIELDS AT I-1 AND I-1 L1(I)
12 00110 REM OVERALL THICKNESS OF INSULATION L
13 00120 REM LOCAL SPACING RATIO, L1(I)/L1(I-1), L2(I)
14 00130 REM OVERALL SPACING RATIO, L/L1(1), L4(I)
15 00140 REM (DISTANCE FROM COLD WALL)/L LS(I)
16 00150 REM I-TH SHIELD TEMPERATURE T(I)
17 00160 REM I-TH SHIELD POSITION RATIO X(I)
18 00170 REM I-TH SHIELD TEMPERATURE RATIO P(I) (ALWAYS >1)
19 00180 REM I-TH COLD-WARM TEMPERATURE RATIO R(I) (ALWAYS >1)
20 00190 REM I-TH DIMENSIONLESS ENTROPY PRODUCTION RATE S(I)
21 00195 REM I-TH DIMENSIONLESS HEAT REMOVAL RATE Q(I)
22 00210 REM TOTAL DIMENSIONLESS ENTROPY PROD. RATE S2(I)
23 00220 REM MINIMUM ENTROPY PRODUCTION RATE S0(I)
24 00230 REM ENTROPY PROD. RATE WITHOUT SHIELDS S9(I)
25 00240 REM ENTROPY PROD. RATE RATIOS S3=S2/S0 AND S4=S9/S0
26 00250 REM NUMBER OF SHIELDS M (= OR (10)
27 00260 REM
28 00265 DIM C(10),Y(10)
29 00270 PRINT " "
30 00280 PRINT "INPUT : IF MORE WORK IS TO BE DONE, 0 IF FINISHED"
31 00290 INPUT A
32 00300 IF A=0 THEN 01350
33 00310 PRINT "INPUT NO,NO,M,GAMMA & P(1)"
34 00320 INPUT NO,NO,M,G0,P(1)
35 00325 DEF FND(Y)=(NO+1)*Y*NO-NO/(Y*(1-NO))-1/(Y*Y)
36 00335 DEF FNE(Y)=(NO+1)*Y*NO-NO/(Y*(1-NO))-1/(Y*Y)
37 00335 DEF FNF(Y)=Y*(NO+1)-Y*NO+1/Y-1
38 00340 DEF FNG(Y)=Y*(NO+1)-Y*NO+1/Y-1
39 00350 PRINT " EXPONENT M0=","M0," EXPONENT N0=","N0," GAMMA=","G0
40 00355 M1=M0+1
41 00358 N1=N0+1
42 00360 FOR I=1 TO M
43 00370 L1=1
44 00380 L2=1-1
45 00390 R(I)=0.000001
46 00400 C=1
47 00410 D=1
48 00420 P1=P(1)*R(I)
49 00430 W1=(R(I)*M0)*FNE(P(1))+G0*R(I)*M0*FNC(P(1))
50 00435 W2=(R(I)*(M0-1)*FND(P(1))+G0*R(I)*(M0-1)*FNE(P(1)))^2
51 00438 W3=((FND(P1)+G0*FNE(P1))^2)/(FNE(P1)+G0*FNC(P1))
52 00439 C=W2/W1+W3
53 00440 G1=C*D
54 00450 IF G1=0 THEN 00500
55 00460 IF G1=0 THEN 00570
56 00470 C=-1°C
57 00480 IF ABS(C) 0.00001 THEN 00570
58 00490 D=D
59 00500 R(I)=R(I)+C
60 00510 IF R(I) 0.999999 THEN 00540
61 00520 IF R(I) 0.000001 THEN 00540
62 00530 GOTO 00420
63 00540 R(I)=R(I)-1°C
64 00550 C=1°C
65 00560 GOTO 00420
66 00570 U=((R(I)*(M0-1)*FND(P(1))+G0*R(I)*(M0-1)*FNE(P(1)))
67 00575 X1(I)=U/(FND(P1)+G0*FNE(P1))
68 00580 X(I)=X1(I)/(1+X1(I))
69 00590 V=(FNE(P1)+G0*FNC(P1))/(1-X1(I))
70 00595 S(I)=V*(R(I)*M0*FNE(P(1))+G0*R(I)*M0*FNC(P(1)))/X(I)
71 00596 S(I)=S(I)/(1+G0*M1/M1)/M1
72 00600 IF I=1 THEN 00470
73 00610 L3(I)=1
74 00620 R0(I)=R(I)

```

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```

75 00630 T1(I)=R0(I)*P(I)
76 00640 L4(I)=1
77 00650 L5(I)=X(I)
78 00660 GOTO 00930
79 00670 L2(I)=(1-X(I-1))/X(I)
80 00680 IF I>2 THEN 00720
81 00690 L4(2)=X(1)+(1-X(1))/X(2)
82 00700 R0(2)=R(2)/P(1)
83 00710 GOTO 00930
84 00720 IF I>3 THEN 00740
85 00730 L4(3)=1+(1-X(1))*X(2)/(X(2)*X(3))
86 00740 R0(3)=R(3)/(P(1)*P(2))
87 00750 GOTO 00930
88 00760 E=1
89 00770 L4(I)=0
90 00780 FOR J=2 TO 12
91 00790 B=B/X(I,J)
92 00800 L4(I)=L4(I)+B
93 00810 NEXT J
94 00820 L4(I)=L4(I)*(1-X(I))+1
95 00830 L0=1-X(I)
96 00840 FOR J=2 TO 11
97 00850 L0=L0/X(I,J)
98 00860 NEXT J
99 00870 L0=L0*X(I)
100 00880 L4(I)=L4(I)+L0
101 00890 R0(I)=R(I)
102 00900 FOR J=1 TO 11
103 00910 R0(I)=R0(I)/P(J)
104 00920 NEXT J
105 00930 L3(I)=L4(I)
106 00940 L5(I)=X(I)/L3(I)
107 00950 FOR J=2 TO 1
108 00960 L3(J)=L3(J-1)/L2(J)
109 00970 L5(J)=L5(J-1)+X(J)/L3(J)
110 00980 NEXT J
111 00990 T1(I)=R0(I)*P(I)
112 01000 FOR J=1 TO 1
113 01010 T1(J)=T1(J-1)*P(J)
114 01020 NEXT J
115 01030 T1(I+1)=1
116 01040 PRINT " "
117 01050 PRINT "I="I
118 01060 PRINT " "
119 01070 T2(I)=R0(I)
120 01080 FOR J=2 TO 1
121 01090 T2(J)=T1(J-1)
122 01100 NEXT J
123 01110 L3(I+1)=L3(I)
124 01120 X(I+1)=1-X(I)
125 01130 FOR J=1 TO 1
WIDE LINE
126 01120 Z1=((T1(J+1)*M1-T1(J)*M1)*L3(J+1)/X(J+1)-(T1(J)*M1-T2(J)*M1)*L3(J)/X(J))/M1
WIDE LINE
127 01125 Z2=((T1(J+1)*M1-T1(J)*M1)*L3(J+1)/X(J+1)-(T1(J)*M1-T2(J)*M1)*L3(J)/X(J))/M1
128 01128 Q(J)=Z1-G0*Z2/(1+G0*M1/M1)
129 01130 S1(J)=Q(J)/T1(J)
130 01140 PRINT " J=",J," Q=",Q(J)," S1=",S1(J)," L5=",L5(J)," T/T9=",T1(J)
131 01150 NEXT J
132 01152 Q9=(1-T1(I)*M1-G0-G0*T1(I)*M1)*L3(I)/(X(I+1)*M1)
133 01153 Q9=Q9/(1+G0*M1/M1)
134 01154 Q0=(T1(I)*M1-R0(I)*M1-G0*T1(I)*M1-G0*R0(I)*M1)*L3(I)/(X(I)*M1)
135 01155 Q0=Q0/(1+G0*M1/M1)
136 01154 S0=Q0/R0(I)
137 01160 S2(I)=S0-Q9
138 01162 REM CALCULATING DATA TO GET SMIN
139 01163 D=(1-R0(I))/100
140 01164 FOR L=1 TO 101
141 01165 C(L)=R0(I)*D*(L-1)
142 01166 Y(L)=(C(L)*M0-G0*M1/M1)*C(L)*M0)*0.5/C(L)
143 01167 NEXT L
144 01170 FOR J=1 TO 1
145 01180 S2(I)=S2(I)+S1(J)
146 01200 NEXT J
147 01201 REM OBTAIN SMIN USING SIMPSON'S RULE
148 01202 H=Y(1)+Y(101)

```

```

140 01203 FOR K=2 TO 100
150 01204 IF K/2=INT(K/2) THEN 01207
151 01205 H=H+2*Y(K)
152 01206 GO TO 01208
153 01207 H=H+4*Y(K)
154 01208 NEXT K
155 01210 S0(I)=(D/3*H)**2/(1+C0*N1/M1)
156 01212 S3(I)=S2(I)/S0(I)
157 01213 S9(I)=(1-R0(I)*M1+C0-C0*R0(I)*M1)*(1/R0(I)-1)/M1/(1+C0*N1/M1)
158 01240 S4(I)=S9(I)/S0(I)
159 01250 IF I=M THEN 01270
160 01260 P(I)=1/P1
161 01270 PRINT " "
162 01280 PRINT " P="P(I)," R="R(I)," X="X(I)," X1="X1(I)," S="S(I)
163 01290 PRINT " L2="L2(I)," L4="L4(I)
164 01291 PRINT " "
165 01292 PRINT " COLD WALL/HOT WALL TEMPERATURE RATIO, T0/T9="R0(I)
166 01293 PRINT " HEAT OUT AT COLD WALL="Q0," HEAT IN AT WARM WALL="Q9
167 01295 PRINT " ENTROPY PRODUCTION RATE AT COLD WALL="S0
168 01296 PRINT " ENTROPY PRODUCTION RATE AT WARM WALL="S9
169 01300 PRINT " MINIMUM ENTROPY PRODUCTION RATE, S0="S0(I)
170 01301 PRINT " ENTROPY PRODUCTION RATE FOR "I,"SHIELDS, S2="S2(I)
171 01304 PRINT " MAXIMUM ENTROPY PRODUCTION RATE, S9="S9(I)
172 01310 PRINT " ENTROPY PRODUCTION RATE RATIOS, S3=S2/S0 AND S4=S9/S0"
173 01320 PRINT " S3="S3(I)," S4="S4(I)
174 01330 NEXT I
175 01340 GOTO 00170
176 01350 END
177 1000

```

NEWRAF

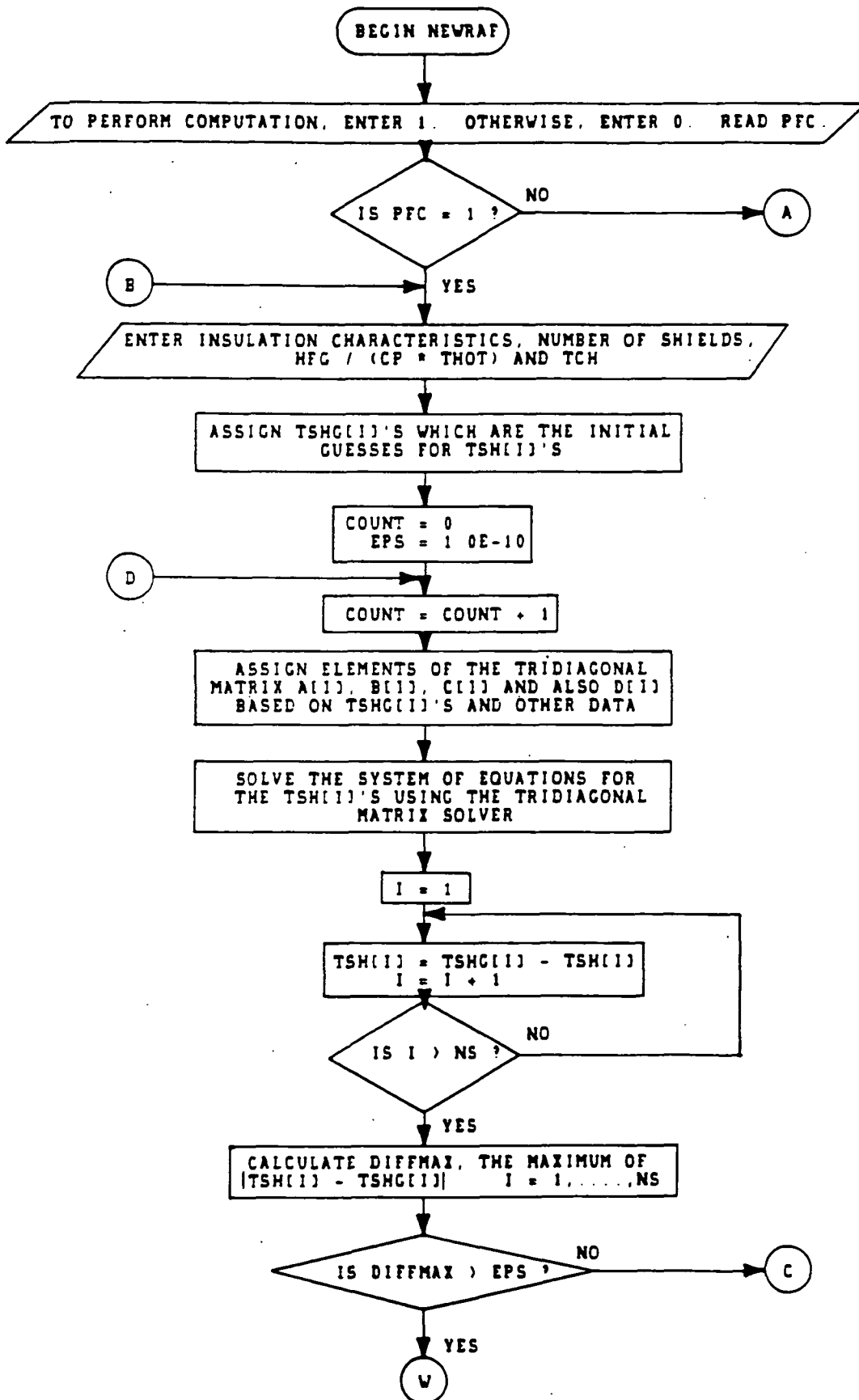
This program solves the original, complete, constrained optimization equations developed in Ref. [9] without the simplifying assumption suggested there which eliminated the dimensionless parameter, $h_{fg}/C_p T_H$. Only single-term thermal conductivity functions were considered in this analysis.

This program also recycles to the starting point. Consequently, the first input is either a 1, if a calculation is to be performed, or a 0, if no more work is to be done.

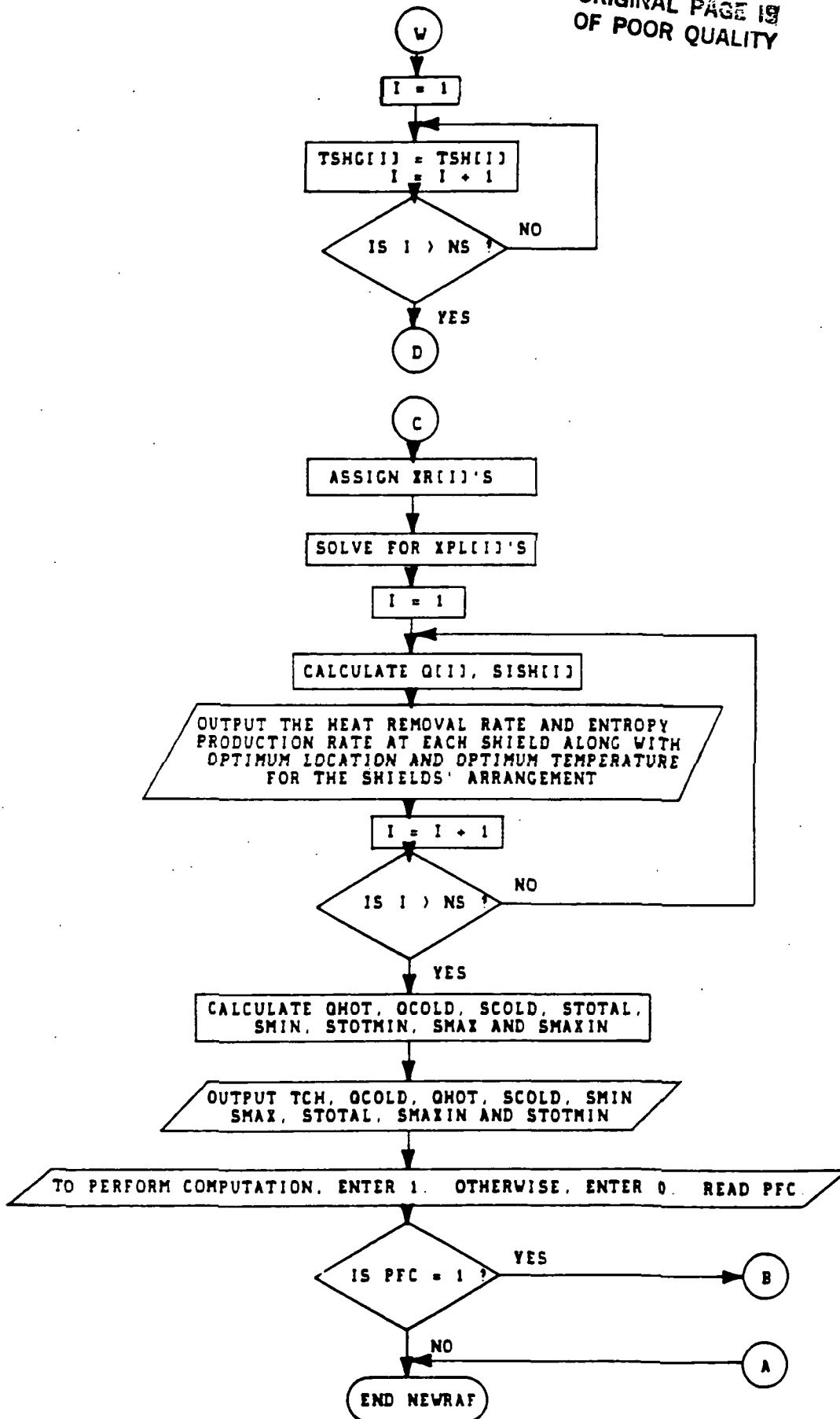
Next the program requests input of the insulation's characteristics, specifically, the exponent of temperature in the thermal conductivity function, the number of cooled shields, the dimensionless parameter $h_{fg}/C_p T_H$ for the boiloff from the insulated container, and $R = T_C/T_H$.

The output specifies the optimal characteristics of the given number of shields with the constraint that the cooling capacity is limited to the boil-off of the liquid due only to the heat leak through the insulation itself.

The flow chart and a program sample follows.



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```
(.....) NEWRAF (.....)
```

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```

(*****)
(1)
(2) THIS PASCAL PROGRAM WAS DEVELOPED TO OPTIMIZE THE
(3) LOCATION, TEMPERATURE AND HEAT DISSIPATION RATE
(4) OF EACH COOLED SHIELD INSIDE AN INSULATION LAYER
(5) THE THERMAL CONDUCTIVITY OF THE INSULATION HAS
(6) THE GENERAL FORM,
(7)
(8)  $K = K_0(T^m)$ 
(9)
(10) THE OBJECTIVE HAS BEEN TO SOLVE THE SET OF 2*MS+1
(11) NON-LINEAR EQUATIONS OBTAINED BY BEJAN, A. "DIS-
(12) CRETE COOLING OF LOW HEAT LEAK SUPPORTS TO 4.2 K,"
(13) CRYOGENICS, VOL 15, 1975, PP 290-292.
(14)
(15) SOLUTION IS BASED ON THE NEWTON-RAPHSON TECHNIQUE
(16) DISCUSSED BY STOECKER, W. F., DESIGN OF THERMAL
(17) SYSTEMS, 2ND EDITION, SECTION 6-11, PP 117-119,
(18) MCGRAW-HILL BOOK CO., NY, 1980
(19)
(*****)

```

TYPE

```

      ARRAY5=ARRAY5( 10) OF REAL
      ARRAY6=ARRAY5( 11) OF REAL
      ARRAY7=ARRAY5( 20) OF REAL

```

```
( * THE SIZE OF ARRAYS DETERMINES THE MAXIMUM NUMBER OF SHIELDS * )
( * THE SIZE OF ARRAYP IS MS+1 * )
( * THE SIZE OF ARRAYT SHOULD BE TWICE THE NUMBER OF SHIELDS * )
```

VAR

```

A      , ARRAYS,
B      , ARRAYS,
C      , ARRAYS,
D      , ARRAYS,
Q1     , ARRAYP,
S      , ARRAYS,
SMAX   , REAL,
SMIN   , REAL,
SMAXIN , REAL,
STOTAL , REAL,
STOTMIN, REAL,
SISH   , ARRAYS,
TSH    , ARRAYS,
TSHC   , ARRAYS,
WORK   , ARRAYT,
I      , ARRAYP,
IPL    , ARRAYS,
IR     , ARRAYS,

      ( LOWER-DIAGONAL ELEMENTS OF THE TRIDIAGONAL MATRIX *)
      ( DIAGONAL ELEMENTS OF THE TRIDIAGONAL MATRIX *)
      ( UPPER-DIAGONAL ELEMENTS OF THE TRIDIAGONAL MATRIX *)
      ( RIGHT-HAND SIDE OF THE SET OF EQUATIONS DURING ITERATIONS *)
      ( 1-TH DIMENSIONLESS HEAT REMOVAL RATE *)
      ( DIMENSIONLESS HEAT TRANSFER BETWEEN SHIELDS *)
      ( DIMENSIONLESS ENTROPY PRODUCTION RATE FOR 1-TH LAYER *)
      ( MAXIMUM DIMENSIONLESS ENTROPY PRODUCTION RATE *)
      ( MINIMUM DIMENSIONLESS ENTROPY PRODUCTION RATE *)
      ( SMAX / SMIN *)
      ( TOTAL DIMENSIONLESS ENTROPY PRODUCTION RATE *)
      ( STOTAL / SMIN *)
      ( 1-TH DIMENSIONLESS ENTROPY PRODUCTION RATE *)
      ( 1-TH SHIELD / HOT WALL TEMPERATURE RATIO, ALWAYS ( 1 *)
      ( GUESSED 1-TH SHIELD / HOT WALL TEMPERATURE RATIO, ALWAYS ( 1 *)
      ( DUMMY VARIABLES *)
      ( SPACING BETWEEN NEIGHBORING SHIELDS / INSULATION THICKNESS *)
      ( DISTANCE FROM COLD WALL / INSULATION THICKNESS *)
      ( X[I] / X[I-1]) *)

AKM    : TEXT,
BETA   , REAL,

      ( OUTPUT FILE TO BE USED IF DESIRED *)
      ( PARAMETER DEFINED IN PROCEDURE INPUTM *)

```

```

80      BOLD      REAL,      (* DUMMY VARIABLE USED IN SOLVING THE TRIDIAGONAL MATRIX *)
81      COUNT     INTEGER,    (* NUMBER OF ITERATIONS NEEDED TO DETERMINE TSH(I)'S *)
82      DELTATC,DEN REAL,      (* DUMMY VARIABLES *)
83      DIFF,DIFFMAX REAL,    (* DUMMY VARIABLES USED IN CHECKING CONVERGENCE *)
84      DIW,DMAX,DMIN REAL,    (* DUMMY VARIABLES USED IN SOLVING THE TRIDIAGONAL MATRIX *)
85      EPS        REAL,      (* A SMALL VALUE USED TO OBSERVE IF CONVERGENCE IS OBTAINED *)
86      CI,CIM1,CIP1 REAL,    (* DUMMY VARIABLES *)
87      COLD       REAL,      (* DUMMY VARIABLE USED IN SOLVING THE TRIDIAGONAL MATRIX *)
88      I,J         INTEGER,    (* INDICES FOR LOOPS *)
89      ITERIN      INTEGER,    (* INDEX USED TO TERMINATE ITERATIONS *)
90      M           REAL,      (* POWER OF THE THERMAL CONDUCTIVITY EQUATION *)
91      MM1         REAL,      (* EQUALS M-1 *)
92      MP1         REAL,      (* EQUALS M+1 *)
93      NS          INTEGER,    (* NUMBER OF SHIELDS *)
94      MSP1        INTEGER,    (* EQUALS NS+1 *)
95      PFC         INTEGER,    (* PROGRAM FLOW CONTROLLER *)
96      TCH         REAL,      (* COLD WALL / HOT WALL TEMPERATURE RATIO, ALWAYS ( 1 ) *)
97      T1,TIM      REAL,      (* DUMMY VARIABLES *)
98      QCOLD       REAL,      (* HEAT OUT AT COLD WALL *)
99      QHOT        REAL,      (* HEAT IN AT HOT WALL *)
100     SCOLD        REAL,      (* ENTROPY PRODUCTION RATE AT COLD WALL *)
101     XTOTAL       REAL,      (* SUM OF X(I)'S; SHOULD EQUAL 1 AFTER SUCCESSFUL COMPUTATION *)

```

```

102
103
104
105
106 PROCEDURE INPUTH.      (* INPUT OF DATA HEADING *)
107 BEGIN
108   WRITELN.
109   ENTER  ----)  M  NS  BETA  TCH  (----),
110   WRITELN.
111   WHERE  M ---- POWER IN THE THERMAL CONDUCTIVITY EQUATION),
112   NS ---- NUMBER OF SHIELDS),
113   BETA -- HFC / (CP*THOT),
114   HFC --- HEAT OF VAPORIZATION (J/KG),
115   CP --- SPECIFIC HEAT AT CONSTANT PRESSURE (J/KG K),
116   THOT -- HOT WALL TEMPERATURE (K),
117   TCH --- COLD WALL / HOT WALL TEMPERATURE RATIO, ALWAYS ( 1 ),
118   WRITELN.
119 END.      (* INPUT OF DATA HEADING *)

```

```

120
121
122
123 PROCEDURE PFC.      (* PFC *)
124 BEGIN
125   WRITELN.
126   TO PERFORM COMPUTATION, ENTER 1. OTHERWISE, ENTER 0 );
127   WRITELN.
128 END.      (* PFC *)

```

```

129
130
131
132 PROCEDURE SINGLESPACE.
133 BEGIN      (* SINGLE SPACE IN OUTPUT *)
134   WRITELN(' ')
135 END.      (* SINGLE SPACE IN OUTPUT *)

```

```

136
137
138
139 FUNCTION PWR(XI,E REAL) REAL.
140 VAR
141   A      REAL,
142 BEGIN      (* COMPUTE XI**E *)
143   A :=E*LN(XI),
144   PWR :=EXP(A)
145 END.      (* COMPUTE XI**E *)

```

```

146
147
148
149 FUNCTION MAXOF2(NO1,NO2 REAL) REAL.
150 BEGIN      (* DETERMINES THE LARGEST OF THE TWO GIVEN NUMBERS *)
151   IF NO1<NO2 THEN
152     IF NO1<NO2 THEN
153       MAXOF2:=NO1
154     ELSE
155       MAXOF2:=NO2
156   ELSE
157     MAXOF2:=NO1
158 END.      (* DETERMINES THE LARGEST OF THE TWO GIVEN NUMBERS *)

```

159

```

60
61
62 FUNCTION MINOF2(N01,N02,REAL):REAL;
63 BEGIN      (* DETERMINES THE SMALLEST OF THE TWO GIVEN NUMBERS *)
64   IF N01<N02 THEN
65     IF N01<N02 THEN
66       MINOF2:=N02
67     ELSE
68       MINOF2:=N01
69     ELSE
70       MINOF2:=N01
71   END,      (* DETERMINES THE SMALLEST OF THE TWO GIVEN NUMBERS *)
72
73
74
75
76
77
78
79       (* MAIN PROGRAM BODY *)
80
81 BEGIN
82   PFC:=1;
83   READLN;
84   READ(PFC);
85   WHILE PFC<=1 DO
86     BEGIN
87
88       (* THIS BLOCK IS USED TO INPUT THE INSULATION THERMAL CONDUCTIVITY, NUMBER *)
89       (* OF SHIELDS, HFC/(CP*THOT) AND COLD WALL / HOT WALL TEMPERATURE RATIO *)
90
91       INPUT
92       READLN
93       READ(M,NS,BETA,TCH);
94       SINGLESPACE;
95       WRITELN('      THERMAL CONDUCTIVITY OF THE INSULATION IS K = K1*T**',M 3-1),
96       WRITELN('      HFC / (CP*THOT) = ',BETA,9 5);
97       SINGLESPACE;
98       SINGLESPACE;
99
100
101       MP:=M-1 0;
102       MM:=M-1 0;
103
104       (* INITIAL GUESSED VALUES FOR TSHC(I)'S ARE ENTERED *)
105
106       DELTATG:=(1 0-TCH)/(NS+1 0);
107       FOR J:=1 TO NS DO TSHC(J):=J*DELTATG+TCH;
108
109       (* VARIABLE USED TO CHECK CONVERGENCE CRITERION IS SET AND THE ITERATIVE PROCEDURE *)
110       (* OF NEWTON-RAPHSON METHOD IS STARTED *)
111
112       EPS:=1 0E-10;
113       COUNT:=0;
114       ITERIN:=0;
115       REPEAT
116         COUNT:=COUNT+1;
117         FOR I:=1 TO NS DO
118           BEGIN
119             GI:=TSHC(I);
120             IF NS=1 THEN
121               IF I<1 THEN
122                 IF I<1 THEN
123                   BEGIN
124                     GI:=TSHC(I-1);
125                     GIP:=TSHC(I+1);
126                   END
127                 ELSE
128                   BEGIN
129                     GI:=TSHC(I-1);
130                     GIP:=1 0;
131                   END
132                 ELSE
133                   BEGIN
134                     GI:=TCH;
135                     GIP:=TSHC(I+1);
136                   END
137                 ELSE
138                   BEGIN
139                     GI:=TCH;

```

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```

40      CIP1 = 1.0
41      END,
42
43      (* ELEMENTS OF THE TRIAGONAL MATRIX ARE COMPUTED *)
44
45      A(1) = PWR(CIP1, NP1) - PWR(CI, N) * (-M * CI * NP1 * (TCH - BETA));
46      B(1) = MP1 * PWR(CI, NM1) * (M * CIM1 * (BETA - TCH + CI) * CI * (-2 * 0 * (BETA - TCH)));
47      B(1) = B(1) + MP1 * PWR(CI, NM1) * CI * (-M * (BETA - TCH) - CI * (M * 2 * 0));
48      C(1) = MP1 * PWR(CIP1, N) * (BETA - TCH + CIM1);
49      D(1) = CIM1 * (PWR(CIP1, NP1) - PWR(CI, NP1)) + BETA * MP1 * PWR(CI, N) - TCH * MP1 * PWR(CI, N) + MP1 * PWR(CI, NP1);
50      D(1) = D(1) - CI * (PWR(CI, N) * (TCH - BETA) - BETA * MP1 * PWR(CI, N) - TCH * MP1 * PWR(CI, N) - MP1 * PWR(CI, NP1));
51      D(1) = D(1) - CIP1 * (BETA * PWR(CIP1, N) - TCH * PWR(CIP1, N));
52      END,
53      A(1) = 0.0,
54      C(1) = 0.0,
55
56      (* THE TRIAGONAL MATRIX SOLVER IS SHOWN IN THIS BLOCK *)
57      (* SEE WESTLAKE, J. R., A HANDBOOK OF NUMERICAL MATRIX *)
58      (* INVERSION AND SOLUTION OF LINEAR EQUATIONS, SECTION *)
59      (* 2.7, PP. 34-35, JOHN WILEY & SONS, INC., NY, 1968 *)
60
61      IF B(1) = 0.0 THEN GOTO 100,
62      BOLD = B(1) / B(1);
63      GOLD = D(1) / B(1);
64      WORK(1) = GOLD;
65      WORK(NS-1) = BOLD;
66      DMAX = ABS(B(1));
67      DMIN = ABS(B(1));
68      FOR I = 2 TO NS DO
69          BEGIN
70              DIW = B(I) - A(I) * BOLD;
71              IF DIW = 0.0 THEN GOTO 100,
72              DMAX = MAXOF2(DMAX, ABS(DIW));
73              DMIN = MINOF2(DMIN, ABS(DIW));
74              GOLD = (D(I) - A(I) * GOLD) / DIW;
75              WORK(I) = GOLD;
76              BOLD = C(I) / DIW;
77              WORK(NS) = BOLD;
78          END;
79      TSH(NS) = GOLD;
80      I = NS;
81      FOR I = 1 TO NS DO
82          BEGIN
83              J = 0;
84              GOLD = WORK(I) - WORK(NS) * NS * GOLD;
85              TSH(I) = GOLD;
86          END;
87
88      (* NEWLY CALCULATED VALUES OF TSH(I)'S ARE COMPUTED *)
89
90      FOR I = 1 TO NS DO TSH(I) = TSHG(I) - TSH(I);
91
92      (* CONVERGENCE IS CHECKED. IF THE CRITERION IS SATISFIED, THE ITERATION IS *)
93      (* TERMINATED, OTHERWISE THE NEWLY CALCULATED TSH(I)'S ARE USED AS NEW *)
94      (* GUESSES FOR ANOTHER ROUND OF ITERATION *)
95
96      DIFFMAX = 1.0E-15;
97      FOR I = 1 TO NS DO
98          BEGIN
99              DIFF = ABS(TSH(I) - TSHG(I));
100             DIFFMAX = MAXOF2(DIFF, DIFFMAX);
101          END;
102      IF DIFFMAX < EPS THEN
103          ITERIN = 1;
104      ELSE
105          FOR I = 1 TO NS DO TSHG(I) = TSH(I);
106      UNTIL ITERIN = 1;
107
108      (* IN THIS BLOCK QUANTITIES USED IN DETERMINING THE SHIELDS' SPACINGS ARE COMPUTED *)
109
110      FOR I = 1 TO NS DO
111          BEGIN
112              T = TSH(I);
113              IF NS(I) THEN
114                  IF I(1) THEN
115                      IF I(ONS) THEN
116                          T(1) = TSH(I-1);
117                      ELSE
118                          T(1) = TSH(I-1);
119                  ELSE
120                      ELSE

```

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```

20     TIME=TCH
21     ELSE
22     TIME=TCH;
23     TR11=(MP1*PWR(TI,M)*(TI-TIME))/(PWR(TI,MP1)-PWR(TIME,MP1));
24     END.
25     DEN=1.0;
26     FOR I=1 TO NS DO DEN=DEN*TR11+1.0;
27     NSP1=NS+1;
28
29     (* FINALLY, SPACINGS BETWEEN SHIELDS AND OTHER QUANTITIES OF INTEREST ARE CALCULATED *)
30
31     X11=1.0/DEN;
32     XPL11=X11;
33     XTOTAL=X11;
34     FOR I=2 TO NSP1 DO
35     BEGIN
36     X11=X11-1)*XPL11-1;
37     IF I<NSP1 THEN XPL11=XPL11-1)*X11;
38     XTOTAL=XTOTAL+X11;
39     END.
40     IF (ABS(XTOTAL-1.0) > 1.0E-5) THEN GOTO 100;
41     Q111=(PWR(TSH11,MP1)-PWR(TCH,MP1))/(X11*MP1);
42     Q1NSP1=(1.0-PWR(TSH1NSP1,MP1))/(X1NSP1*MP1);
43     FOR I=2 TO NS DO Q111=(PWR(TSH11,MP1)-PWR(TSH11-1,MP1))/(X11*MP1);
44     SINGLESPACE;
45     WRITELN:      NUMBER OF SHIELDS      = 'NS 2';
46     WRITELN:      NUMBER OF ITERATIONS = 'COUNT 2';
47     SINGLESPACE;
48     SINGLESPACE;
49     WRITELN:
50     WRITELN:      HEAT REMOVAL      ENTROPY PRODUCTION      OPTIMUM      OPTIMUM
51     WRITELN:      RATE              RATE              LOCATION      TEMPERATURE
52     WRITELN:      -----
53     FOR I=1 TO NS DO
54     BEGIN
55     Q111=Q111+1)*Q111;
56     S1SH11=Q111/TSH11;
57     WRITELN:      SHIELD 1,1,2, 5, Q111 9 5, 11, S1SH11 9 5, 19, XPL11 9 5, 15, TSH11 9 5;
58     END.
59     SINGLESPACE;
60     SINGLESPACE;
61     QHOT=Q1NSP1;
62     QCOLD=Q111;
63     SCOLD=QCOLD/TCH;
64     STOTAL=SCOLD-QHOT;
65     FOR J=1 TO NS DO STOTAL=STOTAL+S1SH11;
66     IF MOD(0) THEN
67     SMIN=SOR((1.0-PWR(TCH,(M/2.0)))/(M/2.0))
68     ELSE
69     SMIN=SOR((1.0/TCH));
70     STOTMIN=STOTAL/SMIN;
71     SMAX=(1.0-PWR(TCH,MP1))/(1.0/TCH-1.0/MP1);
72     SMAXIN=SMAX/SMIN;
73     SINGLESPACE;
74     WRITELN:      COLD WALL / HOT WALL TEMPERATURE RATIO      = 'TCH 14 6);
75     WRITELN:      HEAT OUT AT COLD WALL                        = 'QCOLD 14 6);
76     WRITELN:      HEAT IN AT HOT WALL                          = 'QHOT 14 6);
77     WRITELN:      ENTROPY PRODUCTION RATE AT COLD WALL        = 'SCOLD 14 6);
78     WRITELN:      ENTROPY PRODUCTION RATE AT HOT WALL         = 'QHOT 14 6);
79     WRITELN:      MINIMUM ENTROPY PRODUCTION RATE              = 'SMIN 14 6);
80     WRITELN:      MAXIMUM ENTROPY PRODUCTION RATE              = 'SMAX 14 6);
81     WRITELN:      TOTAL ENTROPY PROD. RATE WITH 'NS 2' SHIELDS = 'STOTAL 14 6);
82     WRITELN:      MAXIMUM / MINIMUM ENTROPY PRODUCTION RATIO = 'SMAXIN 14 6);
83     WRITELN:      TOTAL / MINIMUM ENTROPY PRODUCTION RATIO    = 'STOTMIN 14 6);
84     100 SINGLESPACE;
85     IF (DIW=0.0) OR (BI1=0.0) THEN
86     BEGIN
87     SINGLESPACE;
88     WRITELN:      ---) CHECK THE ASSEMBLY OF COEFFICIENTS TO BE USED IN TRIDIAGONAL MATRIX (---);
89     WRITELN:      ---) CHECK THE TRIDIAGONAL MATRIX SOLVER (---);
90     END.
91     IF (ABS(XTOTAL-1.0) > 1.0E-5) THEN
92     BEGIN
93     SINGLESPACE;
94     WRITELN:      ---) XTOTAL IS NOT EQUAL TO 1.0 (---);
95     WRITELN:      ---) COMPUTATIONS ARE NOT CORRECT (---);
96     END.
97     SINGLESPACE;
98     SINGLESPACE;
99

```

CHARTERED BY THE
OF THE

00 PFCH.
01 READLN.
02 READ(PFC)
03 END
04 ENC
05 /EOP.

TO PERFORM COMPUTATION, ENTER 1. OTHERWISE, ENTER 0.

? 1

ENTER ----> M NS BETA TCH <----

WHERE: M ----- POWER IN THE THERMAL CONDUCTIVITY EQUATION
 NS ----- NUMBER OF SHIELDS
 BETA -- HFG / (CP*THOT)
 HFG --- HEAT OF VAPORIZATION [J/KG]
 CP ---- SPECIFIC HEAT AT CONSTANT PRESSURE [J/KG K]
 THOT -- HOT WALL TEMPERATURE [K]
 TCH --- COLD WALL / HOT WALL TEMPERATURE RATIO, ALWAYS 1

? 1.0 3 0.0145 0.001

THERMAL CONDUCTIVITY OF THE INSULATION IS $K = K1*T**1.0$
 $HFG / (CP*THOT) = 0.01450$

NUMBER OF SHIELDS = 3
 NUMBER OF ITERATIONS = 9

	HEAT REMOVAL RATE	ENTROPY PRODUCTION RATE	OPTIMUM LOCATION	OPTIMUM TEMPERATURE
	-----	-----	-----	-----
SHIELD 1	0.10438	1.56143	0.09719	0.06685
SHIELD 2	0.25983	1.12595	0.28870	0.23076
SHIELD 3	0.47781	0.89782	0.58568	0.53219

COLD WALL / HOT WALL TEMPERATURE RATIO = 0.001000
 HEAT OUT AT COLD WALL = 0.022985
 HEAT IN AT HOT WALL = 0.864998
 ENTROPY PRODUCTION RATE AT COLD WALL = 22.984544
 ENTROPY PRODUCTION RATE AT HOT WALL = -0.864998
 MINIMUM ENTROPY PRODUCTION RATE = 3.751018
 MAXIMUM ENTROPY PRODUCTION RATE = 499.499501
 TOTAL ENTROPY PROD. RATE WITH 3 SHIELDS = 25.704743
 MAXIMUM / MINIMUM ENTROPY PRODUCTION RATIO = 133.163725
 TOTAL / MINIMUM ENTROPY PRODUCTION RATIO = 6.852738

TO PERFORM COMPUTATION, ENTER 1. OTHERWISE, ENTER 0.

? 1

ENTER ----> M NS BETA TCH <----

WHERE: M ----- POWER IN THE THERMAL CONDUCTIVITY EQUATION
 NS ----- NUMBER OF SHIELDS
 BETA -- HFG / (CP*THOT)
 HFG --- HEAT OF VAPORIZATION [J/KG]
 CP ---- SPECIFIC HEAT AT CONSTANT PRESSURE [J/KG K]
 THOT -- HOT WALL TEMPERATURE [K]
 TCH --- COLD WALL / HOT WALL TEMPERATURE RATIO, ALWAYS 1

? 1.0 2 0.0154 0.000806

THERMAL CONDUCTIVITY OF THE INSULATION IS $K = K1 \cdot T^{.1}$
MFG / (CP*THOT) = 0.01540

NUMBER OF SHIELDS = 2
NUMBER OF ITERATIONS = 8

	HEAT REMOVAL RATE	ENTROPY PRODUCTION RATE	OPTIMUM LOCATION	OPTIMUM TEMPERATURE
	-----	-----	-----	-----
SHIELD 1	0.19732	1.97595	0.16252	0.09986
SHIELD 2	0.59037	1.48999	0.48495	0.39623

COLD WALL / HOT WALL TEMPERATURE RATIO	=	0.000806
HEAT OUT AT COLD WALL	=	0.030677
HEAT IN AT HOT WALL	=	0.818366
ENTROPY PRODUCTION RATE AT COLD WALL	=	38.061092
ENTROPY PRODUCTION RATE AT HOT WALL	=	-0.818366
MINIMUM ENTROPY PRODUCTION RATE	=	3.776103
MAXIMUM ENTROPY PRODUCTION RATE	=	619.846992
TOTAL ENTROPY PROD. RATE WITH 2 SHIELDS	=	40.708665
MAXIMUM / MINIMUM ENTROPY PRODUCTION RATIO	=	164.149921
TOTAL / MINIMUM ENTROPY PRODUCTION RATIO	=	10.780603

TO PERFORM COMPUTATION, ENTER 1. OTHERWISE, ENTER 0.

? 0

0.072 CP SECS, 11471B CM USED.

/BYE:

3KMUFTC COSTS: 255.028 SRUS AT \$.0059 = \$1.50

DESINS

This program optimizes the characteristics of a single cooled shield with different insulations on the two sides. Only one-term thermal conductivity functions are considered.

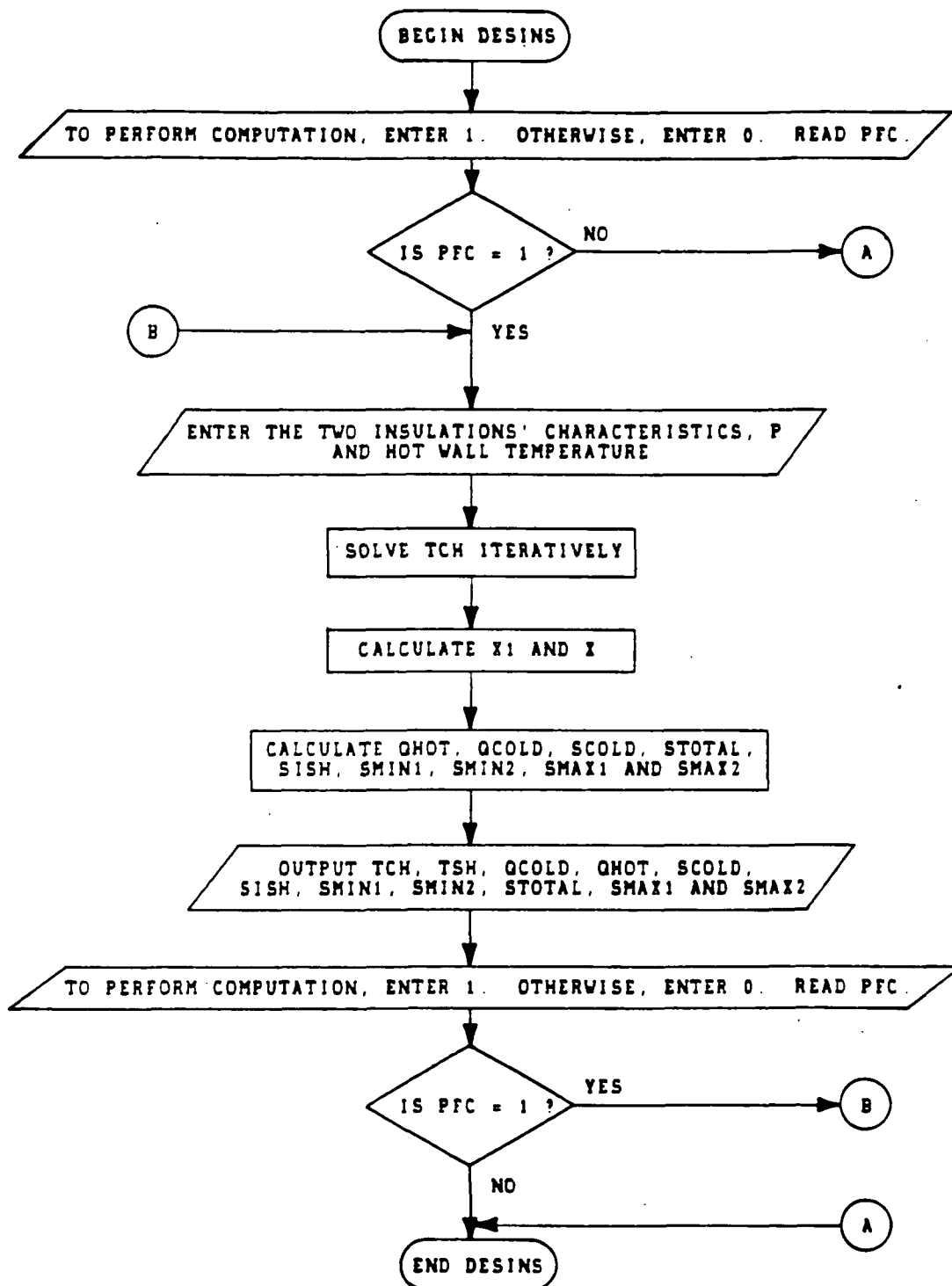
This program also recycles to the starting point; thus the first input is 1, if a calculation is to be performed, or 0 if no more work is to be done.

Next inputs are the characteristics of the two insulations, specifically, the exponents of temperature in the thermal conductivity functions on the hot and cold sides of the shield, a coefficient ratio ALFA (defined in the program), the shield to cold wall temperature ratio, $P = T_S/T_C$, and the hot wall temperature, T_H .

The output specifies the optimal characteristics of the cooled shield as well as other, related information.

The flow diagram and a program sample follows.

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PROGRAM DIFFCOND(INPUT,OUTPUT,SKM);

```

1  (.....)
2  (.....)
3  (.....)
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5  (.....)
6  (.....)
7  (.....)
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9  (.....)
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24 (.....)
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39 (.....)
40 (.....)

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41
42 LABEL 100.
43 LABEL 200.
44 LABEL 300.
45

```

VAR

```

46
47
48
49 P REAL (.....)
50 SMA1 REAL (.....)
51 SMA12 REAL (.....)
52 SMIN1 REAL (.....)
53 SMIN2 REAL (.....)
54 STOTAL REAL (.....)
55 S:SH REAL (.....)
56 TCH REAL (.....)
57 TSH REAL (.....)
58 X REAL (.....)
59 X1 REAL (.....)
60

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61
62 CC REAL (.....)
63 COUNT INTEGER (.....)
64 DD REAL (.....)
65 ALPHA REAL (.....)
66 S:CI REAL (.....)
67 IND INTEGER (.....)
68 M REAL (.....)
69 MP1 REAL (.....)
70 M REAL (.....)
71 MP1 REAL (.....)
72 PTC INTEGER (.....)
73 QCOLD REAL (.....)
74 QHOT REAL (.....)
75 SCOLD REAL (.....)
76 SKM TEXT (.....)
77 THOT REAL (.....)
78
79

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80
81
82 PROCEDURE INPUTH;
83 BEGIN
84   (* INPUT OF DATA HEADING *)
85   WRITELN;
86   WRITELN(' ENTER ---- M M ALFA P THOT (----)');
87   WRITELN(' WHERE M ---- POWER OF THE THERMAL CONDUCTIVITY EQUATION ON THE HOT SIDE');
88   WRITELN(' M ---- POWER OF THE THERMAL CONDUCTIVITY EQUATION ON THE COLD SIDE');
89   WRITELN(' ALFA -- (K2*(M+1))/(K1*(M+1))');
90   WRITELN(' P ---- SHIELD / COLD WALL TEMPERATURE RATIO, ALWAYS 1');
91   WRITELN(' THOT -- HOT WALL TEMPERATURE (K)');
92   WRITELN(' ');
93 END;
94
95
96
97 PROCEDURE PFCM;
98 BEGIN
99   (* PFCM *)
100  WRITELN;
101  WRITELN(' TO PERFORM COMPUTATION, ENTER 1 OTHERWISE, ENTER 0 ');
102  WRITELN;
103 END;
104
105
106 PROCEDURE SINGLESPEACE;
107 BEGIN
108   (* SINGLE SPACE IN OUTPUT *)
109   WRITELN(' ');
110 END;
111
112
113 FUNCTION PWR(X:REAL) REAL;
114 VAR
115   A
116   REAL;
117 BEGIN
118   (* COMPUTE X**E *)
119   A := E*LN(X);
120   PWR := EXP(A);
121 END;
122
123
124 FUNCTION D(E,X:REAL) REAL;
125 BEGIN
126   (* FUNCTIONAL D *)
127   D := (E-1.0)*PWR(X,E)-E/(PWR(X,(1.0-E)))-(1.0/SQR(X));
128 END;
129
130
131 FUNCTION F(E,X:REAL) REAL;
132 BEGIN
133   (* FUNCTIONAL F *)
134   F := (PWR(X,(E-1.0))-PWR(X,E)-1.0)/(1.0/X);
135 END;
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WRITELN(''
SINGLESPEACE,
SINGLESPEACE,

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MP1 = M + 1.0;
MP1 = M + 1.0;
TCH = 0.000001;
CC = 0.1;
DD = 1.0;
COUNT = 0;

(* THIS BLOCK CALCULATES TCH ITERATIVELY *)

REPEAT

TSH = P * TCH;
C = D(N,P) * D(N,P) / F(N,P) - PWR(TCH, (2.0 - N)) * D(M,TSH) * D(M,TSH) / F(M,TSH) / ALFA;
G1 = C * DD;
IF G1 < 0.0 THEN GOTO 100;
IF G1 = 0.0 THEN GOTO 200;
CC = (-0.1) * CC;
IF ABS(CC) < 0.000001 THEN GOTO 200;
DD = -DD;
100 TCH = TCH + CC;
IF TCH < 0.999999 OR (TCH < 0.000001) THEN
BEGIN
TCH = TCH - 0.9 * CC;
CC = 0.1 * CC;
IF ABS(CC) < 0.000001 THEN IND = 1
END;
200 COUNT = COUNT + 1;
UNTIL (G1 = 0.0) OR (ABS(CC) < 0.000001) OR (IND = 1);

IF IND = 1 THEN

BEGIN
SINGLESPEACE,
SINGLESPEACE,
SINGLESPEACE,
WRITELN('') OPTIMUM CRITERION CANNOT BE SATISFIED ('---'),
WRITELN('') USE SINGLE INSULATION WITH THE LOWER CONDUCTIVITY ('---'),
GOTO 300
END

(* OTHER QUANTITIES OF INTEREST ARE COMPUTED IN THIS SECTION *)

X1 = -ALFA * PWR(TCH, (N - 1.0)) * D(N,P) / D(M,TSH);
X = X1 / (1.0 - X1);
QHOT = (1.0 - PWR(TSH, MP1)) / ((1.0 - X) * MP1);
QCOLD = ALFA * PWR(TCH, MP1) * (PWR(P, MP1) - 1.0) / (PWR(THOT, (M - N)) * X * MP1);
SCOLD = QCOLD / TCH;
STOTAL = (F(M,TSH) * (1.0 - X) + ALFA * PWR(TCH, M) * F(N,P) / X) / MP1;
SISH = QHOT - QCOLD / TSH;
IF M = 0.0 THEN
SMIN1 = SQRT((1.0 - X) / TCH);
ELSE
SMIN1 = SQRT((1.0 - PWR(TCH, (M/2.0))) / (M/2.0));
IF N = 0.0 THEN
SMIN2 = SQRT((1.0 - X) / TCH);
ELSE
SMIN2 = SQRT((1.0 - PWR(TCH, (M/2.0))) / (M/2.0));
SMA11 = F(M,TCH) / MP1;
SMA12 = F(N,TCH) / MP1;

SINGLESPEACE,

WRITELN('')	NUMBER OF ITERATIONS	= 'COUNT 8);
WRITELN('')	COLD WALL / HOT WALL TEMPERATURE RATIO	= 'TCH 14.6);
WRITELN('')	SHIELD / HOT WALL TEMPERATURE RATIO	= 'TSH 14.6);
WRITELN('')	SHIELD LOCATION	= 'X 14.6);
WRITELN('')	HEAT OUT AT SHIELD	= 'QHOT-QCOLD 14.6);
WRITELN('')	HEAT OUT AT COLD WALL	= 'QCOLD 14.6);
WRITELN('')	HEAT IN AT HOT WALL	= 'QHOT 14.6);
WRITELN('')	ENTROPY PRODUCTION RATE AT COLD WALL	= 'SCOLD 14.6);
WRITELN('')	ENTROPY PRODUCTION RATE AT HOT WALL	= 'QHOT 14.6);
WRITELN('')	ENTROPY PRODUCTION RATE AT SHIELD	= 'SISH 14.6);
WRITELN('')	MINIMUM ENTROPY PRODUCTION RATE BASED ON K1*T**M	= 'SMIN1 14.6);
WRITELN('')	MINIMUM ENTROPY PRODUCTION RATE BASED ON K2*T**M	= 'SMIN2 14.6);
WRITELN('')	TOTAL ENTROPY PRODUCTION RATE	= 'STOTAL 14.6);
WRITELN('')	ENTROPY PROD. W/O SHIELD BASED ON K1*T**M	= 'SMA11 14.6);

240 WRITE(' ENTROPY PROD W/O SHIELD BASED ON K2-T**M = ' ,SHA22 14 6) .
241 300 SINGLESPEACE.
242 SINGLESPEACE.
243 SINGLESPEACE.
244 PFCN.
245 READEN.
246 READ(PFC)
247 END
248 END

83

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TO PERFORM COMPUTATION, ENTER 1. OTHERWISE, ENTER 0.

1

ENTER ----> M N ALFA P THOT ----

WHERE: M ----- POWER OF THE THERMAL CONDUCTIVITY EQUATION ON THE HOT SIDE
N ----- POWER OF THE THERMAL CONDUCTIVITY EQUATION ON THE COLD SIDE
ALFA -- $[K2*(M+1)]/[K1*(N+1)]$
P ----- SHIELD / COLD WALL TEMPERATURE RATIO, ALWAYS 1
THOT -- HOT WALL TEMPERATURE [K]

1.0 0.0 20.0 4.5 300.0

THERMAL CONDUCTIVITY OF THE INSULATION ON THE HOT SIDE IS $K = K1*(T**1.0)$.
THERMAL CONDUCTIVITY OF THE INSULATION ON THE COLD SIDE IS $K = K2*(T**0.0)$.
 $[K2*(M+1)]/[K1*(N+1)] = 20.00$
HOT WALL TEMPERATURE = 300.00 [K]

NUMBER OF ITERATIONS	=	36
COLD WALL / HOT WALL TEMPERATURE RATIO	=	0.001666
SHIELD / HOT WALL TEMPERATURE RATIO	=	0.007497
SHIELD LOCATION	=	0.390755
HEAT OUT AT SHIELD	=	0.820144
HEAT OUT AT COLD WALL	=	0.000497
HEAT IN AT HOT WALL	=	0.820641
ENTROPY PRODUCTION RATE AT COLD WALL	=	0.298568
ENTROPY PRODUCTION RATE AT HOT WALL	=	-0.820641
ENTROPY PRODUCTION RATE AT SHIELD	=	109.396253
MINIMUM ENTROPY PRODUCTION RATE BASED ON $K1*T**M$	=	3.680131
MINIMUM ENTROPY PRODUCTION RATE BASED ON $K2*T**N$	=	40.925828
TOTAL ENTROPY PRODUCTION RATE	=	178.307751
ENTROPY PROD. W/O SHIELD BASED ON $K1*T**M$	=	299.619216
ENTROPY PROD. W/O SHIELD BASED ON $K2*T**N$	=	598.241762

TO PERFORM COMPUTATION, ENTER 1. OTHERWISE, ENTER 0.

0

0.044 CP SECS, 10233B CM USED.

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16. Abstract <p>A relatively simple method has been developed to optimize the location, temperature, and heat dissipation rate of each cooled shield inside an insulation layer. The method is based on the minimization of the entropy production rate which is proportional to the heat leak across the insulation. The results show that the maximum number of shields to be used in most practical applications is three. However, cooled shields are useful only at low values of the overall, cold wall to hot wall absolute temperature ratio. The performance of the insulation system is relatively insensitive to deviations from the optimum values of the temperature and location of the cooling shields.</p> <p>Design curves are presented for rapid estimates of the locations and temperatures of cooling shields in various types of insulations, and an equation is given for calculating the cooling loads for the shields.</p>					
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